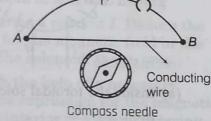
# 1.1 Magnetic Field

The space in the surroundings of a magnet or a current carrying conductor in which its magnetic influence can be experienced is called **magnetic field**. Its SI unit is **tesla** (T).

#### **Oersted Experiment**

Oersted experiment demonstrated that the current carrying conductor carrying moving charges produces magnetic field around it.



Battery

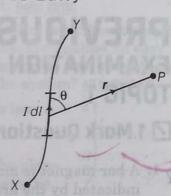
When key *K* is closed, then

deflection occurs in the compass needle and vice-versa.

# Magnetic Field due to a Current Element (Biot-Savart's Law)

According to this law, the magnetic field due to small current carrying element *dl* at any nearby point *P* is given by

$$dB = \frac{\mu_0}{4\pi} \cdot \frac{Idl \sin \theta}{r^2}$$
or 
$$d\mathbf{B} = \frac{\mu_0}{4\pi} \cdot \frac{Id\mathbf{l} \,\hat{\mathbf{r}}}{|\mathbf{r}|^2}$$



and direction is given by Ampere's swimming

rule or right hand thumb rule.

where, 
$$\frac{\mu_0}{4\pi} = 10^{-7} \text{ T-m/A} = 10^{-7} \text{ H/m}$$

and  $\mu_0$  = permeability of free space or vacuum and r = distance of point P from current carrying element.

## **Permittivity and Permeability**

The relation between  $\mu_0$ ,  $\varepsilon_0$  and c is

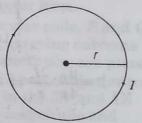
$$\frac{1}{\mu_0 \varepsilon_0} = c^2$$

where, c is velocity of light,  $\varepsilon_0$  is permittivity of free space and  $\mu_0$  is magnetic permeability.

#### Some Important Points Related to Magnetic Field

(i) Magnetic field at the centre of a circular current carrying conductor/coil.





where, r is the radius of a circular loop.

For *N* turns of coil,  $B = \frac{\mu_0 NI}{2r}$ 

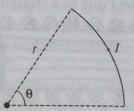
(ii) Magnetic field at the centre of semi-circular current carrying conductor

$$B = \frac{\mu_0 I}{4r}$$



(iii) Magnetic field at the centre of an arc of circular current carrying conductor which subtends an angle  $\theta$  at the centre

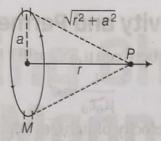
$$B = \frac{\mu_0}{4\pi} \cdot \frac{I\theta}{r}$$



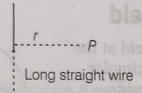
# SBG STUDY

(iv) Magnetic field at any point lies on the axis of circular current carrying conductor

$$B = \frac{\mu_0 I a^2}{2 (r^2 + a^2)^{3/2}}$$



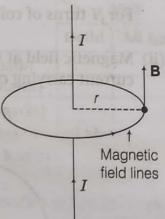
(v) Magnetic field due to straight current carrying conductor at any point *P* at a distance *r* from the wire is given by



$$B = \frac{\mu_0}{4\pi} \cdot \frac{2I}{r} \implies B \propto \frac{1}{r}$$

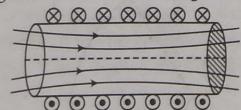
# 1.2 Ampere's Circuital Law

The line integral of the magnetic field  $\mathbf{B}$  around any closed path in vacuum is equal to  $\mu_0$  times of the total current I threading through the closed circuit i.e. loop. Mathematically,  $\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I$ 



# Important Points Related to Magnetic Field

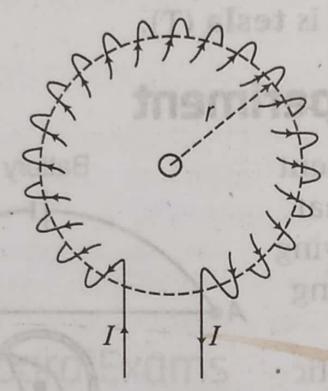
- Magnitude of magnetic field of a straight wire using Ampere's law  $B = \frac{\mu_0 I}{2\pi r}$ 
  - (i) Magnetic field due to a straight solenoid



- (a) At any point inside the solenoid,  $B = \mu_0 nI$  where, n = number of turns per unit length.
- (b) At points near the ends of air closed solenoid,

$$B = \frac{1}{2} \mu_0 nI$$

(ii) Magnetic field due to a toroidal solenoid



(a) Inside the toroidal solenoid,  $B = \mu_0 nI$ Here,  $n = \frac{N}{2\pi r}$ 

and N = total number of turns

(b) In the open space, interior or exterior of toroidal solenoid, B = 0

# 2.1 Force on moving charge in a uniform Magnetic and Electric Field (Lorentz Force)

Force experienced by a single charged particle q moving with speed v in a uniform magnetic field at an angle  $\theta$  with it is known as magnetic Lorentz force.

$$\mathbf{F} = q \ (\mathbf{v} \times \mathbf{B}) \qquad [\text{vector form}]$$

Magnitude of  $F = qvB \sin \theta$  and direction of force is given by right hand palm rule or Fleming's left hand rule.

### SI Unit of Magnetic Field

Magnetic lorentz force,  $F = qvB \sin \theta$ 

$$\Rightarrow B = \frac{F}{qv \sin \theta}$$

If 
$$F = 1 \text{ N}, q = 1 \text{ C}, v = 1 \text{ ms}^{-1}$$

$$\sin \theta = 1 = \sin 90^{\circ} \implies \theta = 90^{\circ}$$

: SI unit of 
$$B = \frac{1 \text{ N}}{(1 \text{ C}) (1 \text{ ms}^{-1})}$$
  
=  $1 \text{ NA}^{-1} \text{m}^{-1} = 1 \text{ T}$ 

SI unit of magnetic field, B = 1 tesla (T).

# Right Hand Palm Rule

If all four fingers of right hand together points in the direction of magnetic field and thumb points the direction of motion of positive charge, then the palm of right hand faces in the direction of force.

## Magnetic Force on a Charged Particle

- Work done by magnetic Lorentz force on charge particle is zero as F ⊥ v, hence F is perpendicular to displacement.
- Magnetic force cannot increase the kinetic energy of charge particle.
- The trajectory/path traversed by the charged particle is a
  - (*i*) straight line when angle between **v** and **B** is 0° or 180°.
- (ii) circle when angle between v and **B** is 90°.
- (iii) helix when angle between  $\mathbf{v} \times \mathbf{B}$  is an acute angle.
- When charge particle enter in a magnetic field perpendicularly, then

$$(i) \frac{mv^2}{r} = qvB \qquad (ii) \text{ rad}$$

(ii) radius, 
$$r = \frac{mv}{qB}$$

$$(iii) T = \frac{2\pi m}{qB}$$

$$(iv) f = \frac{qB}{2\pi m} = \frac{1}{T}$$

$$(v) KE = \frac{q^2 B^2 r^2}{2m}$$

- When angle between v and B is  $\theta$ , then
- (i) Radius of helical path,  $r = \frac{mv \sin \theta}{qB} = \frac{mv_{\perp}}{qB}$

where,  $v_{\perp} = v \sin \theta$  = perpendicular component of velocity.



$$T = \frac{2\pi r}{v_{\perp}} = \frac{2\pi r}{v \sin \theta} \cdot \frac{m v \sin \theta}{q B} = \frac{2\pi m}{q B}$$

(iii) Frequency, 
$$f = \frac{qB}{2\pi m}$$

(iv) Pitch = 
$$\frac{2\pi m v \cos \theta}{qB} = \frac{2\pi m v_{\parallel}}{qB}$$

where,  $v_{\parallel} = v \cos \theta = \text{parallel component of}$ velocity.

· Net force on a charged particle when both electric and magnetic fields are present.

$$\mathbf{F} = q \left[ \mathbf{E} + (v \times \mathbf{B}) \right]$$

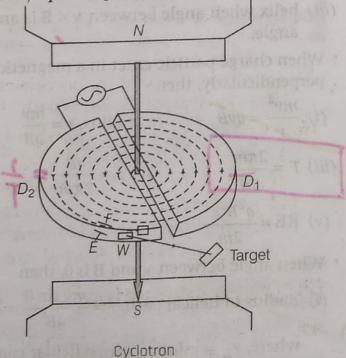
 If a charged particle q accelerated by potential difference V and speed changes from 0 to v, then,

Work done = Change in KE  

$$qV = \frac{1}{2} mv^2 \Rightarrow v = \sqrt{\frac{2qV}{m}}$$

# 2.2 Cyclotron

A compact device used to accelerate the positively charged ion or particles (like protons, deuterons, α-particles) upto very high speed.



Based on the principle of magnetic resonance, a charge particle can be accelerated to high speed by passing it again and again through small region of oscillating electrical field by making the use of strong normal magnetic field.

· KEmax of charge particle accelerated by

cyclotron is 
$$KE_{max} = \frac{q^2 B^2 R^2}{2m}$$

where, R = radius of circular track of charged particle.

 Cyclotron cannot accelerate electron and electrically neutral particles.

# 3.1 Force on a Current Carrying Conductor in a Uniform Magnetic Field

The **magnetic force** experienced by a current-carrying conductor placed in a uniform magnetic field is given by

$$\mathbf{F} = I (\mathbf{l} \times \mathbf{B})$$
 [vector form]

where,  $\mathbf{l} = \mathbf{a}$  vector whose magnitude is equal to length of the conductor and has identical direction in the flow of electric current I and  $\mathbf{B} = \text{magnetic}$  field.

Magnetic force,  $F = IBl \sin \theta$  where,  $\theta$  is the angle between current and magnetic field.

The direction of force is given by Fleming's left hand rule.

# Magnetic Force between Two Parallel Current Carrying Conductor

Magnetic force between two straight parallel current-carrying conductors is given by

$$\frac{F}{L} = \frac{\mu_0}{4\pi} \cdot \frac{2I_1I_2}{r}$$

Force will be of attractive nature, if direction of flow of currents are in the same direction i.e. parallel.

The force of repulsion will act when direction of flow of currents are in opposite directions.

(antiparallel)

If both wires are of length  $l_1$  and  $l_2$  (if  $l_1 > l_2$ ), then magnetic force between two straight current carrying wires/conductors is given by

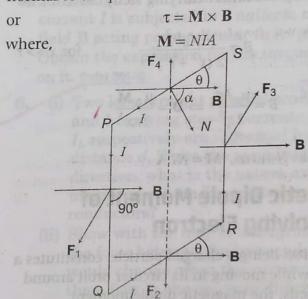
$$F = \frac{\mu_0}{4\pi} \frac{2I_1I_2}{r} \qquad l_2$$
small length

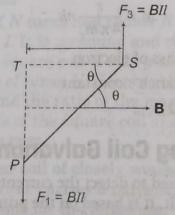
# 3.2 Torque Experienced by a Current Carrying Loop in Uniform Magnetic Field (Magnetic Dipole)

Torque experienced by a current-carrying loop placed in a uniform magnetic field *B* is given by

$$\tau = NIAB \sin \theta$$

where,  $\theta$  is the angle between the direction of magnetic field **B** and that of vector **N** drawn normal to the plane of the coil.

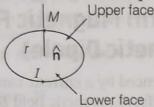




and **M** is known as magnetic dipole moment of coil. Its SI unit is A-m<sup>2</sup>.

## 3.3 Circular Current Loop as a Magnetic Dipole

A current loop behaves as a magnetic dipole. If we look at the upper face, current is anti-clockwise, so it has North polarity. If we look at lower face, then current is clockwise, so it has South polarity so.



Magnetic dipole moment of the loop, M = IA

$$\Rightarrow$$
  $|\mathbf{M}| = I\pi r^2$ 

The magnitude of magnetic field on axis of a circular loop of radius *r* carrying stedy current *I* is given by

$$B = \frac{\mu_0 I r^2}{2 (x^2 + r^2)^{3/2}} \qquad \text{for } x >> r$$

$$B = \frac{\mu_0 I r^2}{2x^3} \implies \mathbf{B} = \frac{\mu_0 \mathbf{M}}{2\pi x^3}$$

If loop has N turns,  $\mathbf{M} = NI \mathbf{A}$ 

## Magnetic Dipole Moment of a Revolving Electron

An electron being a charged particle, constitutes a current while moving in its circular orbit around the nucleus, the magnetic dipole moment

$$M = \frac{e}{4\pi m_e} nh$$

where,  $m_e$  = mass of electron h = Planck's constant and n = 1, 2, 3, ...

## 3.4 Moving Coil Galvanometer

It is a device used to detect the current in electrical circuit. It is based on the principle that a current carrying loop placed in a uniform magnetic field experiences torque, the magnitude of which depends on the strength of current.

The current sensitivity and voltage sensitivity of galvanometer depends on number of turns of coil magnetic field *B*, area *A* of the coil and torsion constant *k* of the spring or suspension wire.

Restoring torque = Deflecting torque

$$k\alpha = NIBA$$

[Torque  $\tau$  = Force × perpendicular distance =  $NIbB \times a \sin 90^{\circ} = NIBA1$ 

Current sensitivity, 
$$I_s = \frac{\theta}{I} = \frac{NBA}{k}$$

Its SI unit is rad/A or div/A.

Voltage sensitivity, 
$$V_s = \frac{\theta}{V} = \frac{1}{R} = \frac{I_s}{R} = \frac{NBA}{kR}$$

Its SI unit is rad/V or div/V.

Torque or moment of galvanometer

$$G = \frac{\Theta}{I} = \frac{NBA}{k}$$

Clearly 
$$V_s = \frac{I_s}{R}$$

#### Conversion of Galvanometer into an Ammeter and Voltmeter

A galvanometer can be converted into an ammeter by connecting a very low resistance (shunt S) in parallel with galvanometer whose value is given by

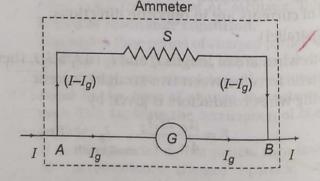
$$S = \frac{I_g G}{I - I_g}$$

where, G = resistance of galvanometer

 $I_g$  = current through galvanometer

I = total current in circuit and

S = resistance of the shunt (low resistance).



# Conversion of a Galvanometer to Voltmeter

A galvanometer can be converted into voltmeter by connecting a very high resistance *R* in series with galvanometer which is given by

$$R = \frac{V}{I_g} - G$$

where,  $I_g$  = current through the galvanometer

G = resistance of galvanometer and

V = potentials difference across the terminal A and B.

# $A \bullet \longrightarrow I_g G \longrightarrow R \longrightarrow B$

NOTE The resistance of an ideal ammeter is zero and an ideal voltmeter is infinite. Ammeter is always connected in series with electrical circuit, whereas voltmeter is connected in parallel with the circuit.