

SBG STUDY

Chapter 1:-

Q. Write any two basic properties of charges?

Ans. (i) Conservation of charges

(ii) Quantization of charges

(iii) Charge is Additive in nature.

\therefore Charges possessed by a body is always equal to the internal multiple of charge over one electron i.e.

$$Q = ne$$

\therefore Where $n = 1, 2, 3, \dots$ or any other integer.

$$e = 1.6 \times 10^{-19} \text{ C}$$

Suppose, $1 \text{ C} = Ne$

$$N = \frac{1}{e} = \frac{1}{1.6 \times 10^{-19}}$$

$$= 6.25 \times 10^{18}$$

Coulomb's Law of Electrostatics:-

$$F \propto q_1 q_2$$

$$F \propto \frac{1}{r^2}$$

$$F \propto \frac{q_1 q_2}{r^2}$$

$$F = k \frac{q_1 q_2}{r^2}$$

$$F = \left(\frac{1}{4\pi\epsilon_0} \right) \frac{q_1 q_2}{r^2} \rightarrow \textcircled{1}$$

\therefore Where $\epsilon =$ Permittivity of a medium.

$$\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ N m}^2 \text{ C}^{-2}$$

$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2 \text{ N}^{-1} \text{ m}^2 =$ Permittivity of free space.

Force experienced in a medium.

$$F' = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} \rightarrow (2)$$

Dividing (1) by (2)

$$\frac{F}{F'} = \frac{C}{\epsilon_0} = K = \text{Di-electric constant of the medium}$$

Q. Find out the distance b/w 2 protons between which the electrostatic force is equal to the weight of either of them.

Ans. \checkmark $F = mg = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$

$$F = \frac{q_1 q_2}{4\pi\epsilon_0} \frac{1}{mg}$$

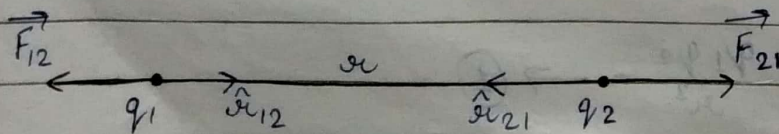
$$= \sqrt{\frac{9 \times 10^9 \times 1.6 \times 10^{-19} \times 1.6 \times 10^{-19}}{1.6 \times 10^{-27} \times 10}}$$

$$= \sqrt{\frac{9 \times 10^9 \times 1.6 \times 1.6 \times 10^{-27}}{1.6 \times 10^{18} \times 10^{18} \times 10}} = \frac{3 \times 1.6^{0.4} \times \sqrt{10^{-2}}}{4}$$

$$= 3 \times 0.04 = 0.12$$

$$= 120 \text{ mm.}$$

Coulomb's Law in Vector form :-



$$|\vec{F}_{12}| = |\vec{F}_{21}| = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

$$\vec{F}_{12} = \left(\frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r_{21}^2} \right) \hat{r}_{21}$$

$$\vec{F} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r_{21}^2} \hat{r}_{12}$$

Q. How will the force between ² charges change if they are kept in water?

Ans. Force will become $\frac{1}{81}$ times

$$F_v = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

$$F_w = \frac{1}{4\pi\epsilon_0 K} \frac{q_1 q_2}{r^2}$$

∴ Where $K = 81$ for water

$$\therefore \frac{F_v}{F_w} = 81.$$

Q. Define 'di-electric' constant of a medium?

Ans. It is defined as the ratio of force b/w two point charges separated by a distance kept in vacuum to the force b/w same two point charges kept in medium separated by the same distance. For metals $K = \text{infinite}$ & for water $K = 81$ & for vacuum, $K = 1$.

$$\frac{F_v}{F_m} = K \text{ or } \epsilon$$

Principle of Superposition:-

Acc. to this principle the net force acting over

a point charge due to a cluster of charges is equal to the vector sum of the forces experienced by the first charge due to all other individual charges.

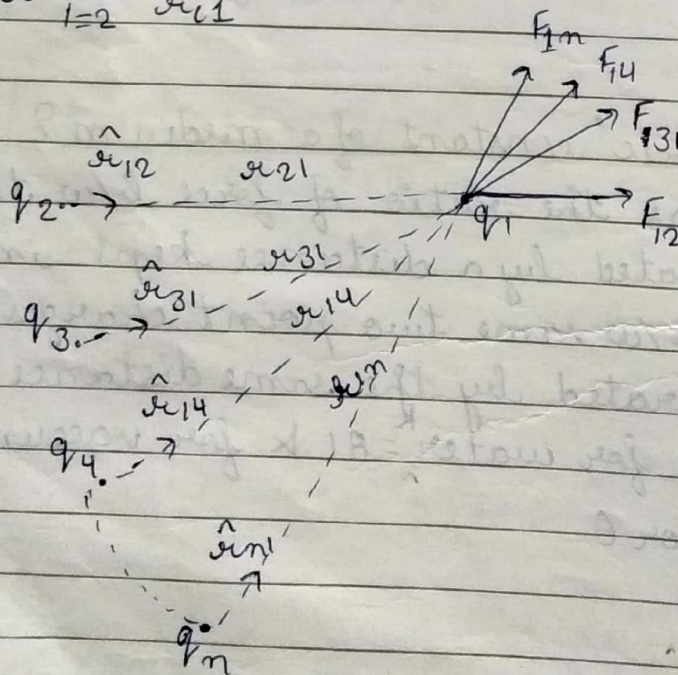
Mathematically, Force experienced by q_1 due to all other charges can be written as $\vec{F}_1 = \vec{F}_{12} + \vec{F}_{13} + \dots + \vec{F}_{1n}$

$$= \frac{1}{4\pi\epsilon_0} \cdot \frac{q_1 q_2}{r_{21}^2} \hat{r}_{21} + \frac{1}{4\pi\epsilon_0} \cdot \frac{q_1 q_3}{r_{31}^2} \hat{r}_{31} + \dots$$

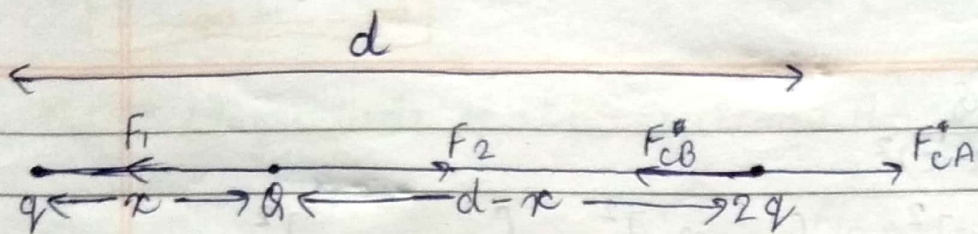
$$\frac{1}{4\pi\epsilon_0} \cdot \frac{q_1 q_n}{r_{n1}^2} \hat{r}_{n1}$$

$$= \frac{q_1}{4\pi\epsilon_0} \left[\frac{q_2}{r_{21}^2} \hat{r}_{21} + \frac{q_3}{r_{31}^2} \hat{r}_{31} + \dots + \frac{q_n}{r_{n1}^2} \hat{r}_{n1} \right]$$

$$= \frac{q_1}{4\pi\epsilon_0} \sum_{i=2}^n \frac{q_i}{r_{i1}^2} \hat{r}_{i1}$$



Q. State's principle of superposition? Explain it by taking an example of n charge system?



$$F_1 = \frac{1}{4\pi\epsilon_0} \frac{Q \cdot 2q}{(d-x)^2}$$

$$F_2 = \frac{1}{4\pi\epsilon_0} \frac{q \cdot Q}{x^2}$$

For equilibrium we must have $F_1 = F_2$

$$\frac{1}{4\pi\epsilon_0} \frac{Q \cdot 2q}{(d-x)^2} = \frac{1}{4\pi\epsilon_0} \frac{q \cdot Q}{x^2}$$

$$\frac{2}{(d-x)^2} = \frac{1}{x^2}$$

$$2x^2 = (d-x)^2$$

$$x\sqrt{2} = d-x$$

$$x + x\sqrt{2} = d$$

$$x(\sqrt{2}+1) = d$$

$$x = \frac{d}{\sqrt{2}+1}$$

$$= \frac{d}{\sqrt{2}+1} \times \frac{\sqrt{2}-1}{\sqrt{2}-1}$$

$$= d(\sqrt{2}-1) = 0.41d$$

On the basis of above fig.

$$F_{ca} = F_{cb}$$

$$\frac{1}{4\pi\epsilon_0} \frac{q \cdot 2q}{d^2} = \frac{1}{4\pi\epsilon_0} \frac{Q \cdot 2q}{(d-x)^2}$$

$$\frac{q}{d^2} = \frac{Q}{(d-x)^2}$$

$$Q = q \left[\frac{d-x}{d} \right]^2 = q \left[1 - \frac{x}{d} \right]^2 = q \left[1 - \frac{1+\sqrt{2}}{2} \right]^2$$

$$Q = 2q$$

~~Find the force on the charge kept at A~~

$$Q = q \left[1 - \frac{x}{d} \right]^2$$

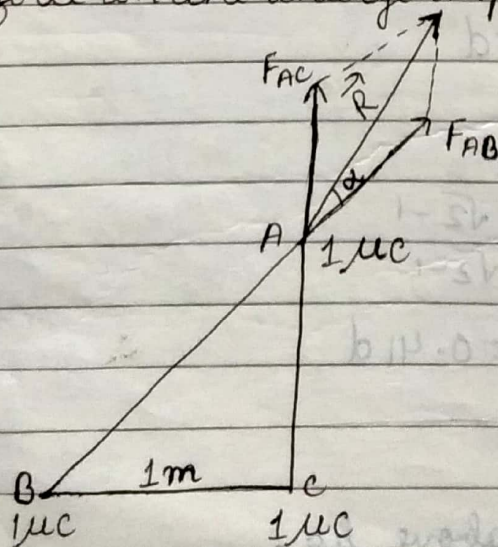
$$Q = q \left[1 - (1+\sqrt{2}) \right]^2$$

$$Q = q \left[1 + 1 - \sqrt{2} \right]^2$$

$$Q = q \left[2 - \sqrt{2} \right]^2$$

$$Q = q \left[0.35 \right]^2 \Rightarrow Q = 0.36q$$

Q. Find out the force on the charge kept at A in fig:-



$$\text{Ans. } F_{AC} = 9 \times 10^9 \times \frac{1 \times 1 \times 10^{-6} \times 10^{-6}}{(1)^2} = 9 \times 10^{-3} \text{ N}$$

$$F_{AB} = 9 \times 10^9 \times \frac{10}{(\sqrt{2})^2} = 4.5 \times 10^{-3} \text{ N}$$

∴ Magnitude of the resultant $R = \sqrt{F_{AC}^2 + F_{AB}^2 + 2F_{AB} \cdot F_{AC} \cos 45^\circ}$

$$= \sqrt{9^2 + 4.5^2 + 2 \times 9 \times 4.5 \times \frac{1}{\sqrt{2}}} \times 10^{-3}$$

$$= \sqrt{81 + 20.25 + \frac{81}{\sqrt{2}}} \times 10^{-3}$$

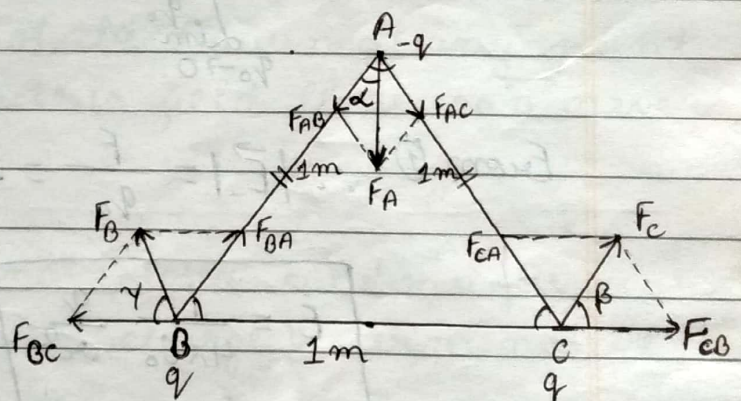
=

$$\tan \alpha = \frac{F_{AC} \sin 45^\circ}{F_{AB} + F_{AC} \cos 45^\circ}$$

$$= \frac{9 \times 10^{-3} \times \frac{1}{\sqrt{2}}}{4.5 \times 10^{-3} + 9 \times 10^{-3} \times \frac{1}{\sqrt{2}}}$$

Q Example 1.7 (NCERT)

Ans.



Note:- Direction of electric field of any field of line can be determined by drawing the tangent on point.

Electric Fields:-

The space around a charge in which an infinitesimally small test charge (q_0) experiences an electro-static force is known as electric field.

$$F = \frac{1}{4\pi\epsilon_0} \frac{qq_0}{r^2}$$

Electric Field Strength or Electric field intensity:-

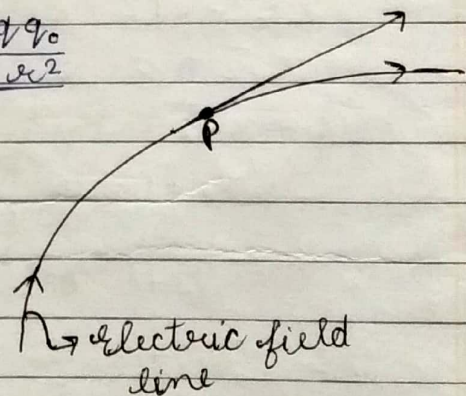
Electric field intensity at a point is defined as the force per unit charge experienced by a very small test charge in the electric field of source charge.

(It is a vector quantity)

$$\vec{E} = \lim_{q_0 \rightarrow 0} \frac{\vec{F}}{q_0} \rightarrow \textcircled{1}$$

From $\textcircled{1}$ $\therefore |\vec{E}| = \frac{F}{q_0} = \frac{\frac{1}{4\pi\epsilon_0} \frac{qq_0}{r^2}}{q_0}$

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$



Electric Lines of Forces:-

It can be defined as the imaginary path along which a very small test charge tends to move or start moving.

Properties of electric field lines:-

(i) Electric field lines are always directed away from

isolated (+)ve charge & isolated (-)ve charge.

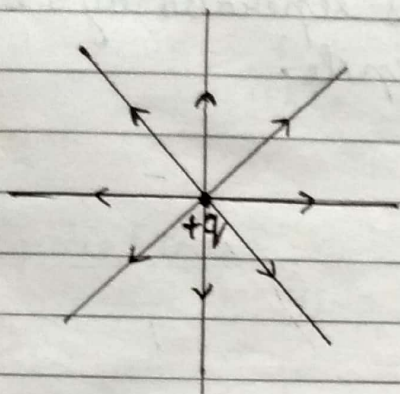


Fig. (a)

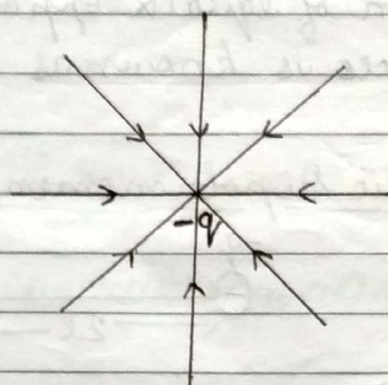


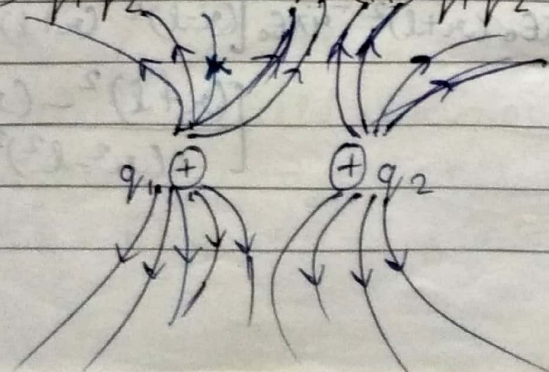
Fig. (b)

- (ii) The tangent drawn at any point of an electric field lines gives the direction of electric field at that point
- (iii) As two tangents cannot be drawn at any point of a curve therefore electric field lines can never intersect each other.
- (iv) Electric field lines are not closed continuous curves because they originate (+)ve charge & terminative (-)ve charge.
- (v) Electric field lines always emerged ^{center} in the normal direction from any charged surface.

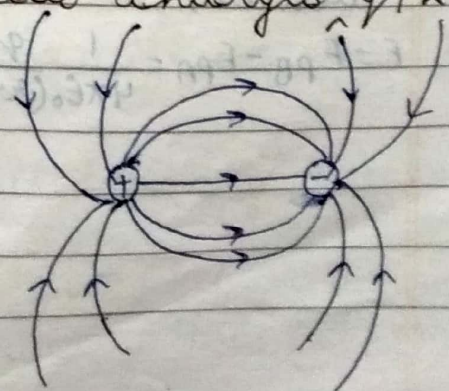
Q. Draw electric field lines for a two charges q_1 & q_2 consisting of

if (i) $q_1 q_2 > 0$ & (ii) $q_1 q_2 < 0$

Ans (i)



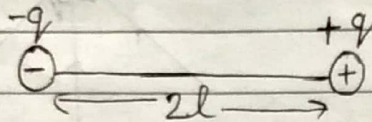
(ii)



Electric Dipole:-

A system of equal & opposite charges separated by a small distance is known as electric dipole.

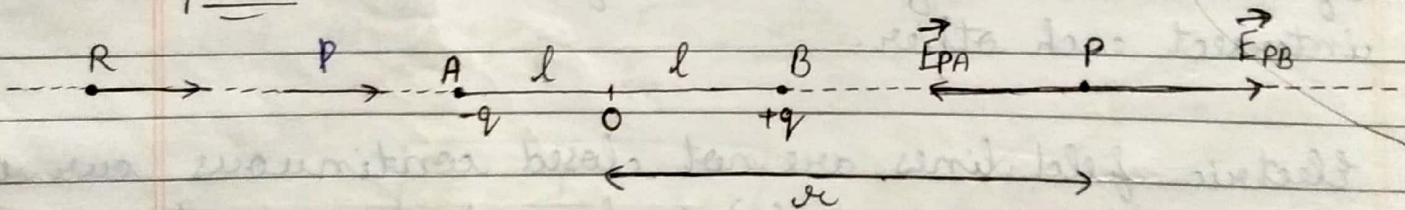
Electric Dipole moment :-



$$\vec{p} = q \cdot 2\vec{l}$$

It is a vector quantity.

Electric field strength due to an dipole on an axial point :-



$$|\vec{E}_{PA}| = \frac{1}{4\pi\epsilon_0} \frac{q}{AP^2} = \frac{1}{4\pi\epsilon_0} \frac{q}{(r+l)^2}$$

$$|\vec{E}_{PB}| = \frac{1}{4\pi\epsilon_0} \frac{q}{BP^2} = \frac{1}{4\pi\epsilon_0} \frac{q}{(r-l)^2}$$

\therefore Net electric field at point P due to the electric dipole will be,

$$E = E_{PB} - E_{PA} = \frac{1}{4\pi\epsilon_0} \frac{q}{(r-l)^2} - \frac{1}{4\pi\epsilon_0} \frac{q}{(r+l)^2} = \frac{q}{4\pi\epsilon_0} \left[\frac{1}{(r-l)^2} - \frac{1}{(r+l)^2} \right] = \frac{q}{4\pi\epsilon_0} \left[\frac{(r+l)^2 - (r-l)^2}{(r^2 - l^2)^2} \right]$$

$$= \frac{q}{4\pi\epsilon_0} \left[\frac{4xl}{(x^2-l^2)^2} \right] = \frac{1}{4\pi\epsilon_0} \frac{2(q2l) \cdot x}{(x^2-l^2)^2} = \frac{1}{4\pi\epsilon_0} \frac{2px}{(x^2-l^2)^2}$$

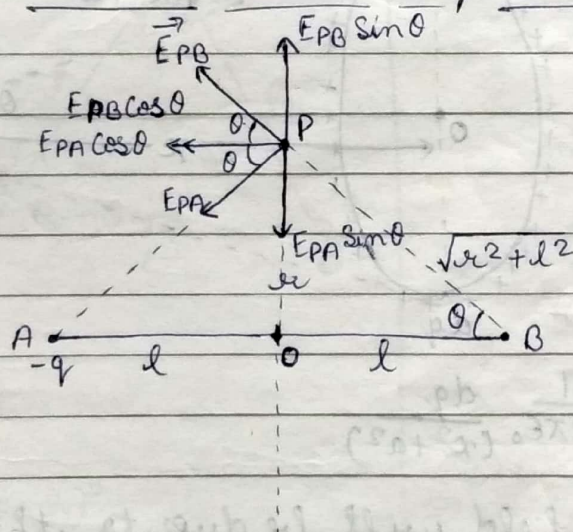
$$E = \frac{1}{4\pi\epsilon_0} \frac{2px}{(x^2-l^2)^2}$$

Special Case :-

(i) If, $x \gg l$, ~~intended~~

$$E = \frac{1}{4\pi\epsilon_0} \frac{2p}{x^3}$$

(ii) Electric field due to an electric dipole at an equatorial point :-



$$|\vec{E}_{PA}| = \frac{1}{4\pi\epsilon_0} \frac{q}{AP^2}$$

$$|\vec{E}_{PB}| = \frac{1}{4\pi\epsilon_0} \frac{q}{BP^2}$$

As, $AP = BP$

$\therefore |\vec{E}_{PA}| = |\vec{E}_{PB}|$ \therefore Vertical components will cancel out the effects of each other.

Net electric field at a point P will be only due to the horizontal components.

$$\therefore E = E_{PA} \cos \theta + E_{PB} \cos \theta = 2 E_{PA} \cos \theta = 2 \times \frac{1}{4\pi\epsilon_0} \frac{q}{(x^2+l^2)} \times \frac{l}{(x^2+l^2)}$$

Note: $2\pi a \rightarrow q$
 $1 \rightarrow \frac{q}{2\pi a}$
 $dl \rightarrow \frac{q}{2\pi a} dl = dq$

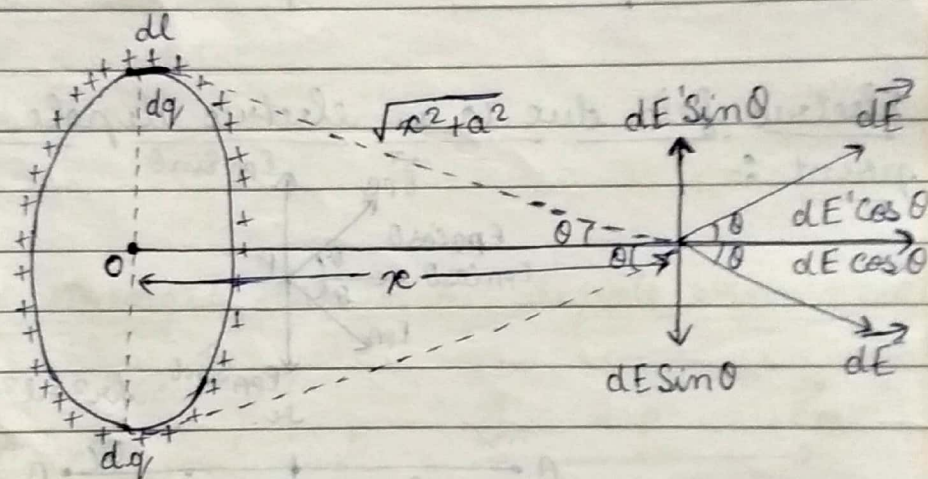
$$E = \frac{1}{4\pi\epsilon_0} \frac{p}{(x^2 + l^2)^{3/2}}$$

Anti-parallel to the dipole moment

Special Case:- If $x \gg l$

$$E = \frac{1}{4\pi\epsilon_0} \frac{p}{x^3}$$

* Electric field at a point on the axis of a uniformly charged ring:-



$$dE = \frac{1}{4\pi\epsilon_0} \frac{dq}{(x^2 + a^2)}$$

Net electric field will be due to the horizontal components only.

$$\begin{aligned} \therefore \oint dE \cos\theta &= \oint \frac{1}{4\pi\epsilon_0} \frac{dq}{(x^2 + a^2)} \times \frac{x}{\sqrt{x^2 + a^2}} \\ &= \oint \frac{1}{4\pi\epsilon_0} \frac{x}{(x^2 + a^2)^{3/2}} \frac{q}{2\pi a} dl \\ &= \frac{qx}{4\pi\epsilon_0 (x^2 + a^2)^{3/2}} \frac{q}{2\pi a} \oint dl \end{aligned}$$

$$E = \frac{qx}{4\pi\epsilon_0 (x^2 + a^2)^{3/2}} \frac{q}{2\pi a} \times 2\pi a$$

$$E = \frac{q \cdot x}{4\pi\epsilon_0 (x^2 - a^2)^{3/2}}$$

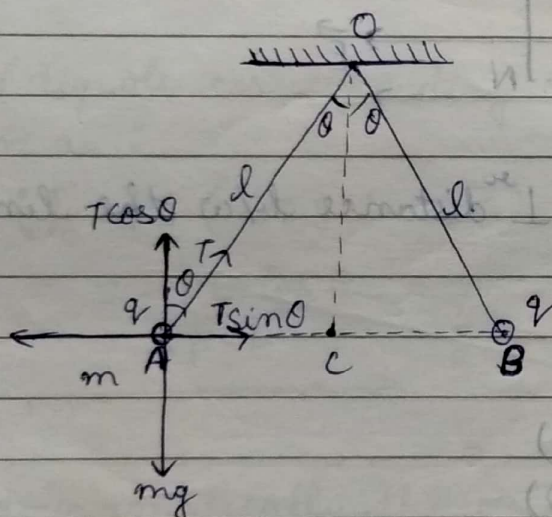
Special Case :- For $x \gg a$

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{x^2}$$

∴ The uniformly charge ring is behaving like a point charge for the point for which $x \gg a$

Q. To find out if the system in the following is in equilibrium?

Ans.



$$F = \frac{1}{4\pi\epsilon_0} \frac{q^2}{(2l \sin \theta)^2}$$

$$\left(\frac{F}{AC} = \frac{mg}{l \cos \theta} \right) = \frac{T}{OA}$$

$$\frac{F}{l \sin \theta} = \frac{mg}{l \cos \theta}$$

$$F = mg \tan \theta$$

$$\frac{1}{4\pi\epsilon_0} \frac{q^2}{4l^2 \sin^2 \theta} = mg \tan \theta$$

$$q^2 = 4\pi\epsilon_0 \cdot 4l^2 \sin^2 \theta \cdot mg \tan \theta$$

$$q = 4l \sin \theta (\pi\epsilon_0 mg \tan \theta)^{1/2}$$

$$q = ?$$

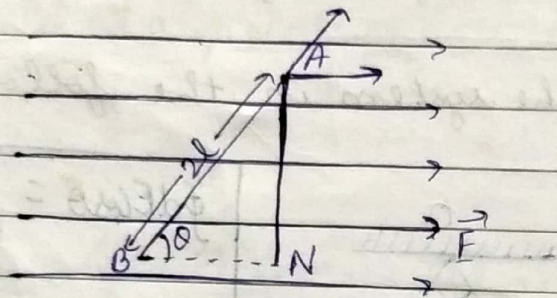
$$l, \theta, m$$

$$\oint dE \cos \theta = \oint \frac{1}{4\pi\epsilon_0} \frac{dq}{(x^2 + a^2)^{3/2}} \times \frac{x^2}{\sqrt{x^2 + a^2}}$$

$$\frac{T \sin \theta = F}{T \cos \theta = mg}$$

$$mg \tan \theta = mg \tan \theta = F$$

✓ Torque acting on uniform electric dipole placed in a uniform electric field:



$\tau =$ Either force \times \perp distance b/w the lines of action of forces.

$$= qE (BN)$$

$$= qE (AB \sin \theta)$$

$$= qE (2l \sin \theta)$$

$$= q \cdot 2l \cdot E \sin \theta$$

$$= q \cdot p E \sin \theta$$

$$\Rightarrow \tau = p E \sin \theta$$

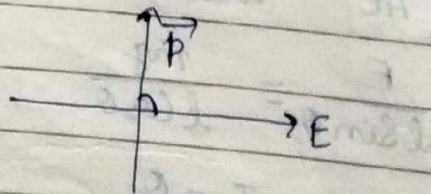
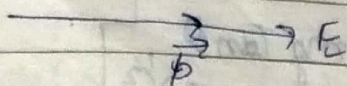
In vector form $\vec{\tau} = \vec{p} \times \vec{E}$

τ_{\max} when $\sin \theta$ max.

$$\theta = 90^\circ$$

$$\tau_{\max} \sin \theta = 0 \quad \boxed{\theta = 0}$$

$$\theta = 0$$



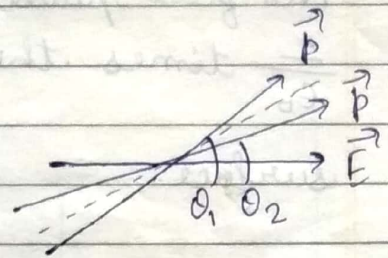
✓ Electrostatic Potential of an electric Dipole placed in a uniform electric field:

$$dW = \tau d\theta$$

$$dW = pE \sin \theta d\theta$$

$$\therefore W = \int dW = \int_{\theta_1}^{\theta_2} pE \sin \theta d\theta$$

$$W = pE [-\cos \theta]_{\theta_1}^{\theta_2}$$



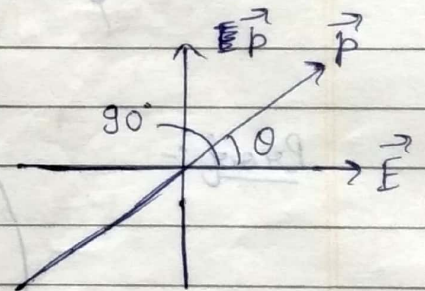
$$E p E = \boxed{U = pE [\cos \theta_1 - \cos \theta_2]}$$

EPE of dipole corresponding to the orientation θ can be given as:

$$U_0 = pE (\cos 90^\circ - \cos \theta)$$

$$= -pE \cos \theta$$

$$= -\vec{p} \cdot \vec{E}$$



- Q₂. Show diagrammatically the orientation of an electric dipole placed in an electric field corresponding to
- Stable equilibrium.
 - unstable equilibrium.

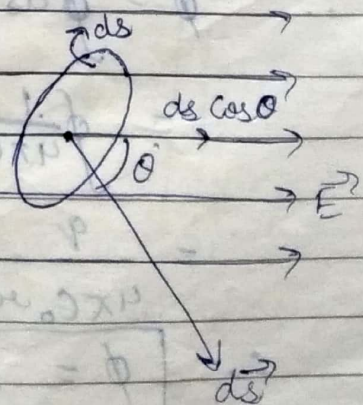
✓ Electric flux:

$$d\phi = \vec{E} \cdot d\vec{s}$$

$$d\phi = E (ds \cos \theta) \text{ or } (E \cos \theta) ds$$

$$\phi = \int ds$$

$$\phi = \int \vec{E} \cdot d\vec{s}$$



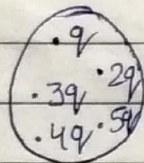
Electric flux is a scalar quantity.
SI unit $\rightarrow \text{Nm}^2 \text{C}^{-1}$

* Gauss' Theorem

Net flux passing through a closed surface is equal to $\frac{1}{\epsilon_0}$ times the total charge enclosed within the surface.

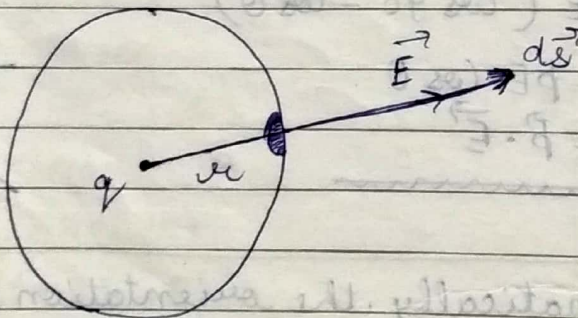
Mathematically, $\phi = \frac{q}{\epsilon_0}$ → Charge enclosed

Ex.



$$\phi = \frac{q + 2q + 3q + 4q + 5q}{\epsilon_0}$$

Proof:-



$$d\phi = \vec{E} \cdot d\vec{s}$$
$$= E ds \cos \theta$$

$$d\phi = E ds$$

$$\therefore \phi = \oint ds = \oint E ds$$

$$= \oint \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \cdot ds$$

$$= \frac{q}{4\pi\epsilon_0 r^2} \oint ds = \frac{q}{4\pi\epsilon_0 r^2} (4\pi r^2) = \frac{q}{\epsilon_0}$$

$$\therefore \boxed{\phi = \frac{q}{\epsilon_0}}$$

Applications of Gauss's Theorem:

Electric field at a point ~~due to~~ near an infinitely large plane sheet of charge:

$$d\vec{s} \cdot \vec{\phi} = \vec{E} \cdot \vec{A}$$

$$= EA \cos \theta$$

$$\theta = 90^\circ$$

$$\phi = 0$$

$$\theta = 0$$

$$\phi = EA$$

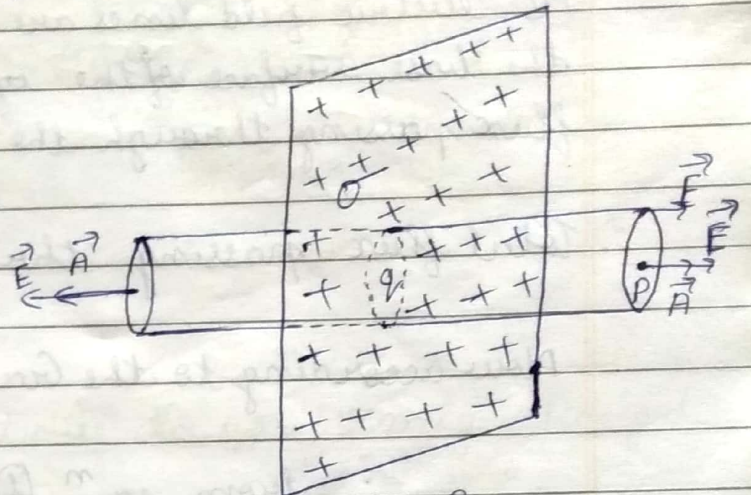
$$\phi = \frac{q}{\epsilon_0} \Rightarrow 2EA = \frac{q}{\epsilon_0} \Rightarrow 2EA = \frac{\sigma A}{\epsilon_0}$$

$$E = \frac{q}{2A\epsilon_0} = \frac{q/A}{2\epsilon_0} = \frac{\sigma}{2\epsilon_0}$$

$$E = \frac{\sigma}{2\epsilon_0}$$

where $\sigma =$ Surface charge density.

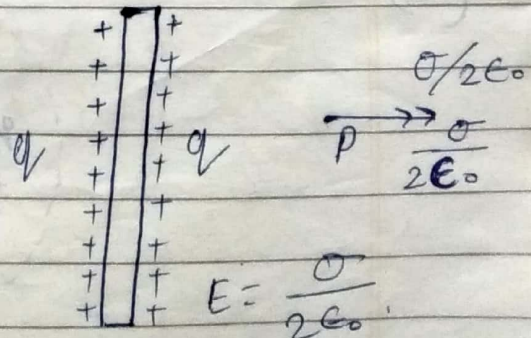
$$E = \frac{\sigma}{2\epsilon_0}$$



Special Case: If the plane sheet is of finite thickness then:

$$E = \frac{\sigma}{2\epsilon_0} + \frac{\sigma}{2\epsilon_0} = \frac{\sigma}{\epsilon_0}$$

$$E = \frac{\sigma}{\epsilon_0}$$



(ii) Electric field at a point due to a line charge:

Gaussian Surface An imaginary surface in ^{inside which} which charge is enclosed is called Gaussian Surface.

$$\phi = \frac{q}{\epsilon_0}$$

As electric field lines are just touching tangentially the base surface of the cylinder, therefore, the electric flux passing through the base surface is zero.

∴ Total flux passing through curved surface = $E \times (2\pi r l)$ → ①

Now according to the Gauss Theorem $\phi = \frac{q}{\epsilon_0}$

∴ from eqⁿ ① we have.

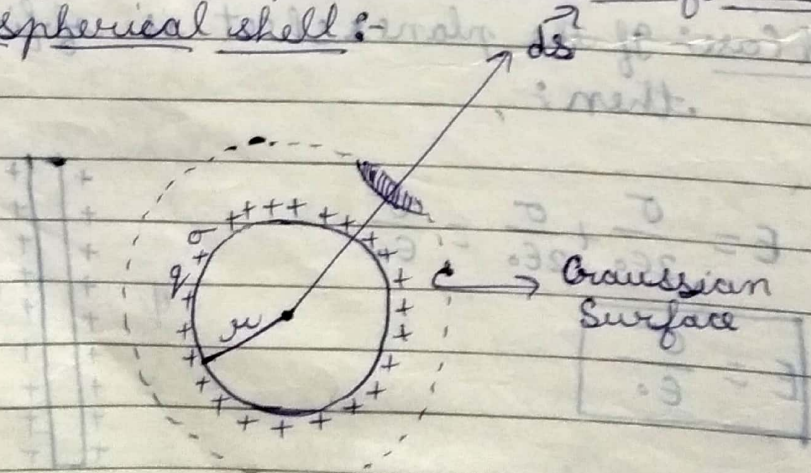
$$E \times (2\pi r l) = \frac{q}{\epsilon_0}$$

$$E = \frac{1}{2\pi\epsilon_0} \frac{q}{r l} = \frac{1}{2\pi\epsilon_0} \frac{q}{r} \rightarrow \text{linear charge density.}$$

$$E = \frac{1}{2\pi\epsilon_0} \frac{q}{r}$$

(iii) Electric field at a point due to uniformly charged hollow spherical shell:-

(a)



At a point outside the sphere:-

$$d\phi = E ds = E ds \cos \theta = E ds$$

some

$$\therefore \phi = \oint d\phi = \oint E ds = E \oint ds = E(4\pi r^2) \rightarrow (1)$$

Acc. to the Gauss Th. $\phi = \frac{q}{\epsilon_0}$

$$\therefore \text{From (1) } E(4\pi r^2) \frac{\epsilon_0}{\epsilon_0} = \frac{q}{\epsilon_0}$$

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} = \frac{1}{4\pi\epsilon_0} \frac{\sigma \cdot 4\pi R^2}{r^2}$$

$$\therefore q = \sigma \cdot 4\pi R^2$$

$$\boxed{E = \frac{\sigma R^2}{\epsilon_0 r^2}}$$

(iii) Electric field at a point due to uniformly charged hollow spherical shell:-

(a) At a point on the surface

$$r = R \therefore \boxed{E = \frac{\sigma}{\epsilon_0}}$$

(c) At a point inside the shell:-

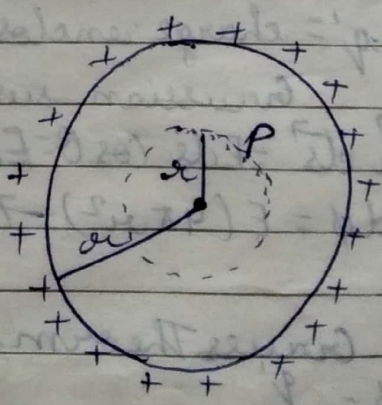
$$\phi = \frac{q}{\epsilon_0}$$

$$\text{OR, } \oint \vec{E} d\vec{s} = \frac{q}{\epsilon_0}$$

$$= \frac{0}{\epsilon_0}$$

$$\oint \vec{E} d\vec{s} = 0$$

$$E = 0$$



(iv) Electric field at a point due to a uniform spherical charge distribution:-

(a) At a point outside the sphere:-

$$\text{Small flux } \phi = \vec{E} \cdot d\vec{s} = E ds \cos \theta = E ds$$

$$\phi = \oint d\phi = \oint E ds = E(4\pi r^2) \rightarrow (1)$$

Acc. to the Gauss Theorem
 ~~$\phi = \frac{q}{\epsilon_0}$~~

$$\phi = \frac{q}{\epsilon_0}$$

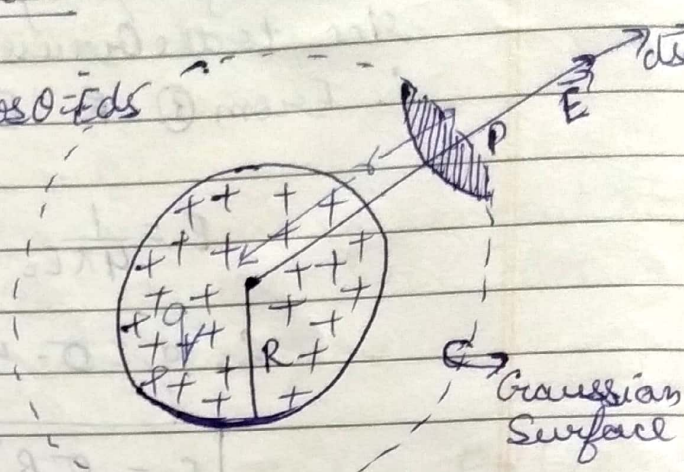
\therefore from eqⁿ (1)

$$E(4\pi r^2) = \frac{q}{\epsilon_0}$$

$$E = \frac{q}{\epsilon_0(4\pi r^2)} = \frac{1}{4\pi\epsilon_0} \cdot \sigma \frac{R^2}{r^2}$$

$$\therefore q = \sigma 4\pi R^2$$

$$E = \frac{\sigma}{\epsilon_0} \frac{R^2}{r^2}$$



(b) At a point inside the sphere:-

Let q' = charge enclosed inside the Gaussian surface.

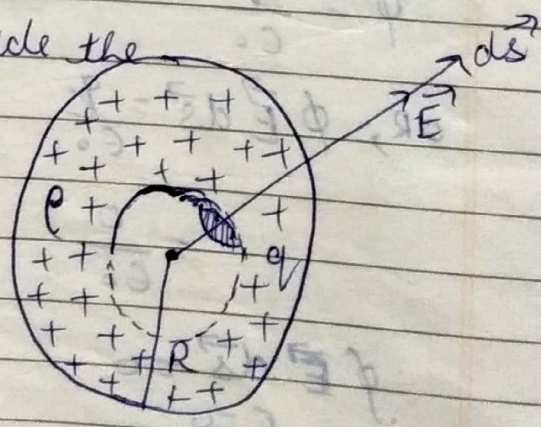
$$\therefore d\phi = \vec{E} \cdot d\vec{s} = E ds \cos \theta = E ds$$

$$\therefore \phi = \oint d\phi = E(4\pi r^2) \rightarrow (1)$$

Acc. to Gauss Theorem.

$$\phi = \frac{q'}{\epsilon_0}$$

$$\therefore E(4\pi r^2) = \frac{q'}{\epsilon_0}$$



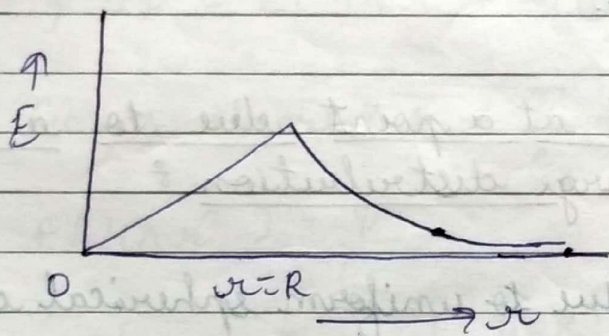
$$E = \frac{4}{4\pi\epsilon_0} \frac{q'}{r^2} \rightarrow \textcircled{2} \quad \frac{4\pi R^3 \rho}{3}$$

$$\therefore E = \frac{1}{4\pi\epsilon_0} \times \frac{4\pi r^3 \rho / 3}{r^2} \quad 1 \rightarrow \frac{q}{4/3 \pi R^3}$$

$$= \frac{1}{4\pi\epsilon_0} \frac{q r}{R^3} \quad \frac{4}{3} \pi r^3 \rho \rightarrow \frac{q}{4/3 \pi R^3} \times \frac{4}{3} \pi r^3$$

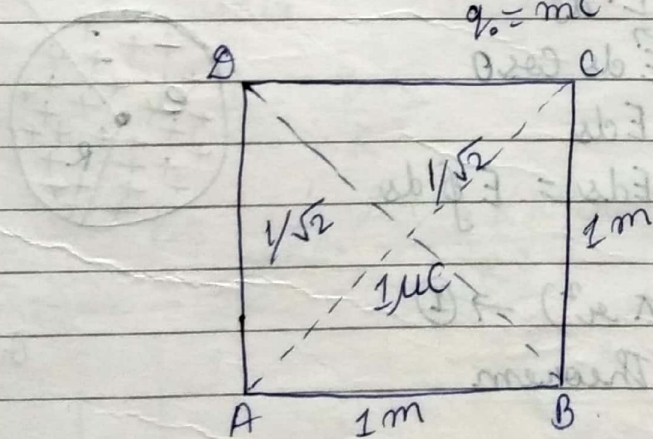
$$4\pi R^2 \quad = \frac{q r^3}{R^3} = R q$$

$$\therefore E = \frac{1}{4\pi\epsilon_0} \frac{\rho \frac{4}{3} \pi R^3}{R^3} = \frac{\rho}{3\epsilon_0}$$



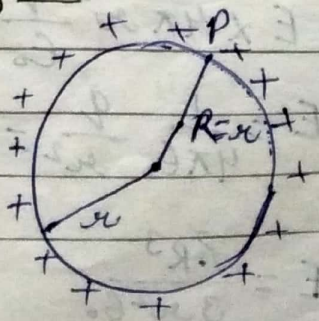
$$W_{e\theta} = q_0 (V_B - V_C) = 0$$

$$q_0 = mc$$



At a point on the surface:-

$$E = \frac{\sigma}{\epsilon_0}$$



At a point outside the shell:

$$\phi = \frac{q}{\epsilon_0}$$

$$\oint \vec{E} \cdot d\vec{s} = \frac{q}{\epsilon_0}$$

$$= \frac{0}{\epsilon_0} = 0$$

$$\oint \vec{E} \cdot d\vec{s} = 0$$

$$\therefore \vec{E} = 0 \quad d\vec{s} \neq 0$$

Electric field inside an uniformly charged spherical shell is zero.

Electric field at a point due to a uniformly spherical charge distribution:

(a) At a point due to uniform spherical charge distribution.

$$\text{Small flux } \phi = \vec{E} \cdot d\vec{s}$$

$$= E \, ds \, \cos \theta$$

$$= E \, ds$$

$$\therefore \phi = \oint d\phi = \oint E \, ds = E \oint ds$$

$$\phi = E (4\pi r^2) \rightarrow \textcircled{1}$$

Acc. to Gauss Theorem

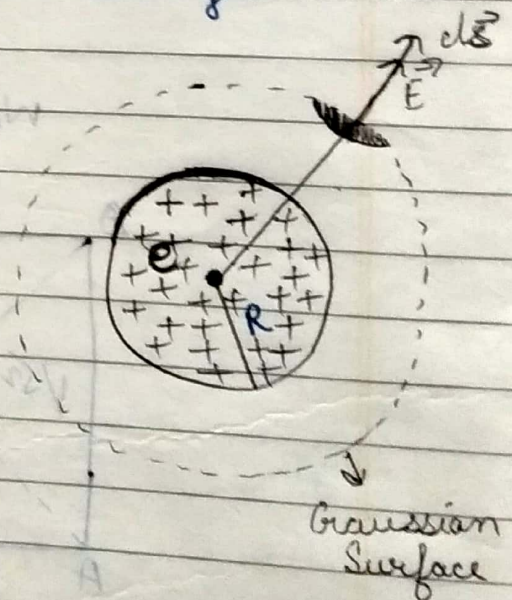
$$\phi = \frac{q}{\epsilon_0}$$

\therefore From eqⁿ ①

$$E \times 4\pi r^2 = \frac{q}{\epsilon_0}$$

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} = \frac{1}{4\pi\epsilon_0} \frac{\rho \cdot \frac{4}{3}\pi R^3}{r^2} \quad \left[\begin{array}{l} \rho = \frac{q}{V} \\ q = \rho V \\ = \rho \cdot \frac{4}{3}\pi R^3 \end{array} \right.$$

$$E = \frac{\rho \cdot R^3}{3\epsilon_0 r^2}$$



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(b)

$$r = R$$

$$\therefore E = \frac{\rho R^3}{3\epsilon_0 R^2}$$

$$E = \frac{\rho R}{3\epsilon_0}$$

(c)

At a point inside the sphere

Let q' = charge enclosed inside the Gaussian surface

$$\therefore d\phi = \vec{E} \cdot d\vec{s} = E ds \cos 0 = E ds$$

$$\therefore \phi = \oint d\phi = E(4\pi r^2) \rightarrow \textcircled{1}$$

$$\therefore \text{From Gauss theorem } \phi = \frac{q'}{\epsilon_0}$$

$$\therefore E(4\pi r^2) = \frac{q'}{\epsilon_0}$$

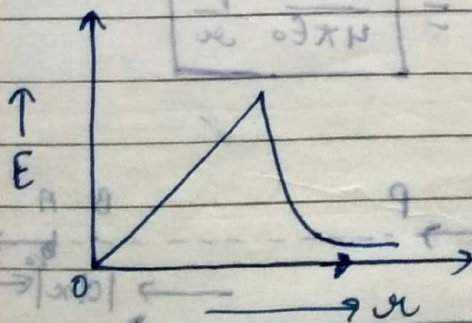
$$E = \frac{1}{4\pi\epsilon_0} \cdot \frac{q'}{r^2} \rightarrow \textcircled{2}$$

$$\therefore E = \frac{1}{4\pi\epsilon_0} \times \frac{\rho \cdot \frac{4}{3}\pi r^3}{R^3 \cdot r^2}$$

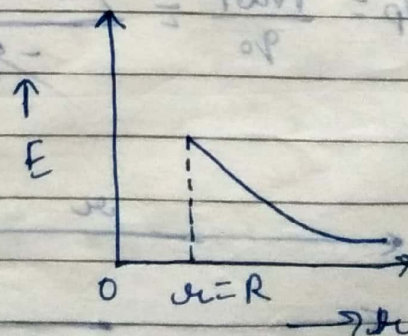
$$= \frac{1}{4\pi\epsilon_0} \cdot \frac{\rho r}{R^3}$$

$$\therefore E = \frac{1}{4\pi\epsilon_0} \cdot \frac{\rho \cdot \frac{4}{3}\pi R^3 r}{R^3} = \frac{\rho r}{3\epsilon_0}$$

$$\left[\begin{array}{l} \frac{4\pi R^3}{3} \rightarrow q \\ 1 \rightarrow \frac{3q}{4\pi R^3} \\ \frac{4\pi}{3} = \frac{3q}{4\pi R^3} \times \frac{4\pi r^3}{3} = \frac{q r^3}{R^3} \\ = q' \end{array} \right.$$



E vs r graph for uniform spherical charge.



E vs r graph for uniformly charged hollow sphere.