

'ATOMIC STRUCTURE'

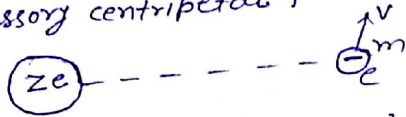
Spectrum of a matter.
 When a body is heated it emits radiation, which consist of various wave length, when these wavelength are plotted against a calibrated scale then, this part is called spectrum of matter.
 In case of Hydrogen radiation of 6562 \AA & then radiation 4860 \AA was observed, these lines denoted the spectrum of Hydrogen.

Bohr Model of Hydrogen-like atom → This model was developed specifically for hydrogenic atom which const of $1e^-$.
 Ex → H-atom, He^+ , Li^{++}

NOTE → Although bohr model seems appropriate for hydrogen like atom & it is able to explain line of spectrum but still it doesn't give the true picture of even H-atom.
 The true picture is derived from quantum mechanics affair which is different from Bohr model in 2 fundamental way.

* 1st postulate →

- * Mass of nucleus is very large.
- * e^- is orbiting in circular orbit.
- * Necessary centripetal force is given by Coulombing attraction.



$$\frac{1}{4\pi\epsilon_0} \frac{Ze^2}{r^2} = \frac{mv^2}{r} \quad \text{--- (1)}$$

$$* mv^2 = \frac{Ze^2}{4\pi\epsilon_0 r} *$$

* 2nd postulate →

* Angular momentum of e^- is integral multiple of $\frac{h}{2\pi}$ or \hbar .

For nth orbit,
$$mvr = \frac{nh}{2\pi} \quad \text{--- (2)}$$

orbital angular momentum of e^- could not have any value. A/c to this postulate: HE While moving around these stable orbit charged particle does not emit any kind of electromagnetic radiation. Energy of e^- is const.

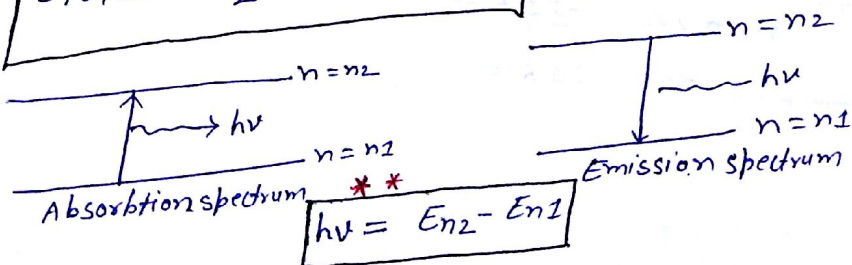
* 3rd postulate →

$$P.E = \frac{1}{4\pi\epsilon_0} \frac{Ze^2}{r} \quad (\text{For nth orbit})$$

$$K.E = \frac{1}{2} mv^2$$

$$E_{\text{total}} = K.E + P.E = \text{const. for a stable orbit.}$$

$$E_{\text{total}} = \frac{1}{2} mv^2 - \frac{Ze^2}{4\pi\epsilon_0 r}$$



* Radius of orbit \rightarrow

$$r = \frac{n^2 h^2 \epsilon_0}{\pi m z e^2} = 0.53 \frac{n^2}{z} \text{ \AA}$$

* velocity of e^- in n th orbit \rightarrow

$$v = 2.18 \times 10^6 \frac{z}{n} \text{ m/sec}$$

- ii) \rightarrow current in n th orbit $\propto z^2/n^3$
- iii) \rightarrow Time period of n th orbit $\propto n^3/z^2$
- iiii) \rightarrow Angular momentum (ω) $\propto z^2/n^3$
- liv) \rightarrow Magnetic Induction (B) $\propto z^3/n^5$
- lv) \rightarrow Magnetic moment (μ) $\propto n$

* current = $i = z \frac{v}{2\pi r} e$

* Time period = $T = \frac{2\pi r}{v}$

* $\omega = \frac{v}{r}$

* $B = \frac{\mu_0 i}{2r} \propto \mu_0 \frac{z^2}{n^3} \times \frac{z}{n^2}$

* $\mu = iA = i \times \pi r^2 \propto \frac{z^2}{n^3} \times \frac{n^4}{n^2} \propto n$

Total energy in n th orbit

$$PE = -\frac{1}{4\pi\epsilon_0} \frac{ze^2}{r}$$

$$K.E = \frac{1}{2} m v^2 = \frac{1}{2} \frac{z e^2}{4\pi\epsilon_0 r}$$

$$K.E = \frac{1}{2} |PE| = -\frac{1}{2} PE$$

$$E_n = \text{Total energy} = K.E + PE = \frac{PE}{2} = -\frac{z e^2}{8\pi\epsilon_0 r}$$

$$E_n = -13.6 \frac{z^2}{n^2} \text{ eV}$$

$$= 13.6 = R h c$$

$$1 \text{ Rydberg Energy} = 13.6 \text{ eV} \Rightarrow R = \frac{2\pi^2 m k^2 e}{ch^3}$$

$$\text{Rydberg const} = R = \frac{2\pi^2 m k^2 e^4}{ch^3} = 1.09 \times 10^7 \text{ m}^{-1}$$

Different Energy level:

_____ $n=3, E_3 = -\frac{13.6 z^2}{9}$

_____ $n=2, E_2 = -\frac{13.6 z^2}{4}$

_____ $n=1, E_1 = -13.6 z^2$

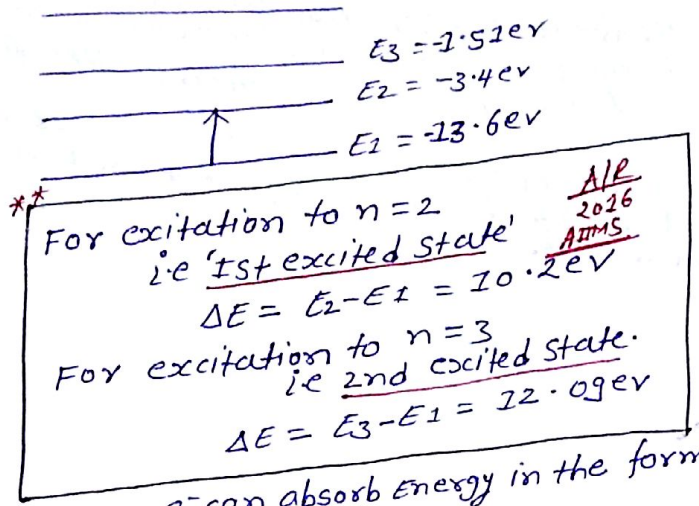
** → For H-atom →

AIMS

$$\begin{aligned}
 E_1 &= -13.6 \text{ eV} \\
 E_2^* &= -3.4 \text{ eV} \\
 E_4 &= -0.85 \text{ eV} \\
 E_5 &= -0.54 \text{ eV}
 \end{aligned}$$

Excitation of e^- in an atom → Whenever an e^- in lower energy state or ground state get some energy from external source, it may make a transition to a energy level, this process is called excitation & the upper or, higher energy state of e^- is termed as excited state.

For Ex - Hydrogen atom



e^- can absorb energy in the form of photon or, form of colliding particle -

- ii) → From photon → An e^- will absorb photon only of the energy $10.2 \text{ eV}, 12.09 \text{ eV}, 12.75 \text{ eV}$ - - - for its excitation.
- iii) → From colliding particle → The collision with the colliding particle must be inelastic so that K.E lost during the collision can be used to excite the atom.

We can use following Law -

- 1a) → conservation of Linear momentum.
- 1b) → conservation of Energy.

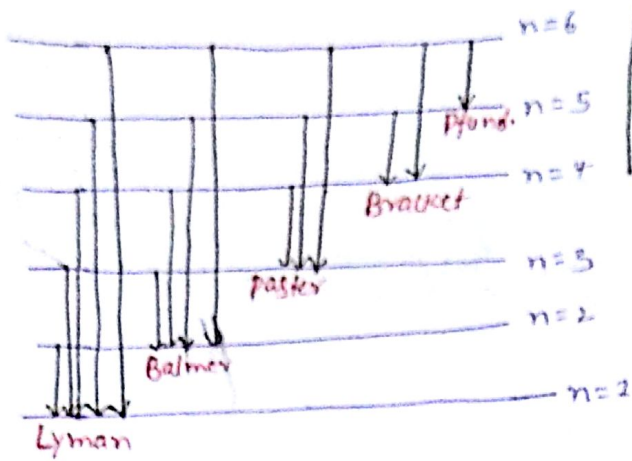
Ionisation Energy or, Ionisation potential : → For H-atom.
 Min energy needed to remove the e^- from

ground state.

$E = 13.6 \text{ eV} \Rightarrow \text{B.E of } e^-$

Ionisation pot. is the min pot. through which an e^- must accelerate before making collision with the e^- of H-atom to knock out it.

Spectral line of H-atom



NOTE →
* For e^- in n th state, spectral line = $n-1$
* Max no. of photon emitted = $n-1$

NOTE → * No two elements will have identical spectral lines, since no two elements have identical energy levels. Therefore they are described as fingerprints of atoms, differing from each other like fingerprints of humans.
* In H-atom an e^- jumps from six energy levels to 1st excited state. The no. of lines corresponding to the Lyman series are → zero, because e^- is not jumping in ground state.