

SBG STUDY

1. Let $A + 2B = \begin{bmatrix} 1 & 2 & 0 \\ 6 & -3 & 3 \\ -5 & 3 & 1 \end{bmatrix}$ and $2A - B = \begin{bmatrix} 2 & -1 & 5 \\ 2 & -1 & 6 \\ 0 & 1 & 2 \end{bmatrix}$, then $\text{Tr}(A) - \text{Tr}(B)$ has the value equal to

- (A) 0 (B) 1 (C) 2 (D) none

2. If $\begin{bmatrix} x & 3x-y \\ zx+z & 3y-w \end{bmatrix} = \begin{bmatrix} 3 & 2 \\ 4 & 7 \end{bmatrix}$, then

- (A) $x=3, y=7, z=1, w=14$ (B) $x=3, y=-5, z=-1, w=-4$
 (C) $x=3, y=6, z=2, w=7$ (D) None of these

3. The matrix $A^2 + 4A - 5I$, where I is identity matrix and $A = \begin{bmatrix} 1 & 2 \\ 4 & -3 \end{bmatrix}$ equals: [JEE-MAIN Online 2013]

- (A) $32 \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$ (B) $4 \begin{bmatrix} 2 & 1 \\ 2 & 0 \end{bmatrix}$ (C) $4 \begin{bmatrix} 0 & -1 \\ 2 & 2 \end{bmatrix}$ (D) $32 \begin{bmatrix} 2 & 1 \\ 2 & 0 \end{bmatrix}$

4. If $M = \begin{bmatrix} 0 & 2 \\ 5 & 0 \end{bmatrix}$ and $N = \begin{bmatrix} 0 & 5 \\ 2 & 0 \end{bmatrix}$, then M^{2011} is -

- (A) $10^{1005} M$ (B) $10^{1005} N$ (C) $10^{2010} M$ (D) $10^{2011} M = 10^{1005} \cdot M$

5. If $A = \begin{bmatrix} 1 & 2 \\ 2 & 3 \end{bmatrix}$ and $A^2 - kA - I_2 = 0$, then value of k is -

- (A) 4 (B) 2 (C) 1 (D) -4

6. Let three matrices are $A = \begin{bmatrix} 2 & 1 \\ 4 & 1 \end{bmatrix}$; $B = \begin{bmatrix} 3 & 4 \\ 2 & 3 \end{bmatrix}$ and $C = \begin{bmatrix} 3 & -4 \\ -2 & 3 \end{bmatrix}$, then

$\text{tr}(A) + \text{tr}\left(\frac{ABC}{2}\right) + \text{tr}\left(\frac{A(BC)^2}{4}\right) + \text{tr}\left(\frac{A(BC)^3}{8}\right) + \dots + \infty$ is equal to -

- (A) 6 (B) 9 (C) 12 (D) none

7. For a matrix $A = \begin{bmatrix} 1 & 2r-1 \\ 0 & 1 \end{bmatrix}$, the value of $\prod_{r=1}^{50} \begin{bmatrix} 1 & 2r-1 \\ 0 & 1 \end{bmatrix}$ is equal to -

- (A) $\begin{bmatrix} 1 & 100 \\ 0 & 1 \end{bmatrix}$ (B) $\begin{bmatrix} 1 & 4950 \\ 0 & 1 \end{bmatrix}$ (C) $\begin{bmatrix} 1 & 5050 \\ 0 & 1 \end{bmatrix}$ (D) $\begin{bmatrix} 1 & 2500 \\ 0 & 1 \end{bmatrix}$

Handwritten notes:
 $M^{2011} = M^{1005 \cdot 2} \cdot M$
 $(M^2)^{1005} \cdot M$
 $= 10^{1005} \cdot 2^{1005} \cdot M$
 $= 10^{1005} \cdot 10^5 \cdot M$
 $= 10^{1005} \cdot 10^5 \cdot M$

Handwritten notes:
 $M^4 = M^2 \cdot M^2 = 10^2 \cdot 2^2 = 10^2 \cdot 4 = 4 \cdot 10^2 I$
 $M^6 = M^4 \cdot M^2 = 4 \cdot 10^2 \cdot 2 = 8 \cdot 10^2 I$

Handwritten notes:
 $-1 - 2 - 4 - 8 + \dots + \infty$
 $\frac{1}{1-r}$

Handwritten notes:
 $3 + \frac{1}{2} \cdot 3 + \frac{1}{4} \cdot 3 + \dots$
 $\text{Tr}(\lambda A) = \lambda \text{Tr}(A)$ Not

8. A and B are two given matrices such that the order of A is 3×4 , if $A'B$ and BA' are both defined then

(A) order of B' is 3×4

(B) order of $B'A$ is 4×4

(C) order of $B'A$ is 3×3

(D) $B'A$ is undefined

9. If the product of n matrices $\begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 3 \\ 0 & 1 \end{bmatrix} \dots \begin{bmatrix} 1 & n \\ 0 & 1 \end{bmatrix}$ is equal to the matrix $\begin{bmatrix} 1 & 378 \\ 0 & 1 \end{bmatrix}$ then

the value of n is equal to -

(A) 26

(B) 27

(C) 377

(D) 378

10. Consider a matrix $A(\theta) = \begin{bmatrix} \sin \theta & \cos \theta \\ -\cos \theta & \sin \theta \end{bmatrix}$ then

(A) $A(\theta)$ is symmetric

(B) $A(\theta)$ is skew symmetric

(C) $A^{-1}(\theta) = A(\pi - \theta)$

(D) $A^2(\theta) = A\left(\frac{\pi}{2} - 2\theta\right)$

$$\frac{n(n-1)}{2} = 378$$

$$n(n-1) = 756$$

$$n^2 - n = 756$$

11. If p, q, r are 3 real number satisfying the matrix equation, $\begin{bmatrix} p & q & r \\ 3 & 4 & 1 \\ 3 & 2 & 3 \\ 2 & 0 & 2 \end{bmatrix} = \begin{bmatrix} 3 & 0 & 1 \end{bmatrix}$, then

$2p + q - r$ equals :-

(A) -1

(B) 4

(C) -3

(D) 2

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12. If A, B and C are $n \times n$ matrices and $\det(A) = 2, \det(B) = 3$ and $\det(C) = 5$, then the value of the $\det(A^2BC^{-1})$ is equal to

(A) $\frac{6}{5}$

(B) $\frac{12}{5}$

(C) $\frac{18}{5}$

(D) $\frac{24}{5}$

13. Which of the following is an orthogonal matrix -

(A) $\begin{bmatrix} 6/7 & 2/7 & -3/7 \\ 2/7 & 3/7 & 6/7 \\ 3/7 & -6/7 & 2/7 \end{bmatrix}$

(B) $\begin{bmatrix} 6/7 & 2/7 & 3/7 \\ 2/7 & -3/7 & 6/7 \\ 3/7 & 6/7 & -2/7 \end{bmatrix}$

(C) $\begin{bmatrix} -6/7 & -2/7 & -3/7 \\ 2/7 & 3/7 & 6/7 \\ -3/7 & 6/7 & 2/7 \end{bmatrix}$

(D) $\begin{bmatrix} 6/7 & -2/7 & 3/7 \\ 2/7 & 2/7 & -3/7 \\ -6/7 & 2/7 & 3/7 \end{bmatrix}$

14. Matrix $A = \begin{bmatrix} x & 3 & 2 \\ 1 & y & 4 \\ 2 & 2 & z \end{bmatrix}$, if $xyz = 60$ and $8x + 4y + 3z = 20$, then $A(\text{adj } A)$ is equal to -

(A) $\begin{bmatrix} 64 & 0 & 0 \\ 0 & 64 & 0 \\ 0 & 0 & 64 \end{bmatrix}$

(B) $\begin{bmatrix} 88 & 0 & 0 \\ 0 & 88 & 0 \\ 0 & 0 & 88 \end{bmatrix}$

(C) $\begin{bmatrix} 68 & 0 & 0 \\ 0 & 68 & 0 \\ 0 & 0 & 68 \end{bmatrix}$

(D) $\begin{bmatrix} 34 & 0 & 0 \\ 0 & 34 & 0 \\ 0 & 0 & 34 \end{bmatrix}$

15. The matrix $\begin{bmatrix} 2 & -2 & -4 \\ -1 & 3 & 4 \\ 1 & -2 & -3 \end{bmatrix}$ is a

- (A) non-singular (B) Idempotent (C) Nilpotent (D) Orthogonal

16. If $A = \begin{bmatrix} ab & b^2 \\ -a^2 & -ab \end{bmatrix}$, then A is

- (A) Involutory matrix (B) Idempotent matrix (C) Nilpotent matrix (D) none of these

17. If A and B are symmetric matrices, then ABA is -

- (A) symmetric matrix (B) skew symmetric matrix
(C) diagonal matrix (D) scalar matrix

18. Let $A = \begin{pmatrix} 0 & \sin \alpha & \sin \alpha \sin \beta \\ -\sin \alpha & 0 & \cos \alpha \cos \beta \\ -\sin \alpha \sin \beta & -\cos \alpha \cos \beta & 0 \end{pmatrix}$, then -

- (A) $|A|$ is independent of α and β (B) A^{-1} depends only on α
(C) A^{-1} depends only on β (D) none of these

19. Number of real values of λ for which the matrix $A = \begin{bmatrix} \lambda-1 & \lambda & \lambda+1 \\ 2 & -1 & 3 \\ \lambda+3 & \lambda-2 & \lambda+7 \end{bmatrix}$ has no inverse

- (A) 0 (B) 1 (C) 2 (D) infinite

20. If $A = [a_{ij}]_{2 \times 2}$ where $a_{ij} = \begin{cases} i+j & i \neq j \\ i^2 - 2j & i = j \end{cases}$, then A^{-1} is equal to -

- (A) $\frac{1}{9} \begin{bmatrix} 0 & 3 \\ 3 & 1 \end{bmatrix}$ (B) $\frac{1}{9} \begin{bmatrix} 0 & -3 \\ 3 & -1 \end{bmatrix}$ (C) $\frac{1}{9} \begin{bmatrix} 0 & -3 \\ -3 & -1 \end{bmatrix}$ (D) $\frac{1}{3} \begin{bmatrix} 0 & 3 \\ 3 & 1 \end{bmatrix}$

$$\begin{bmatrix} -1 & 3 \\ 3 & 0 \end{bmatrix}$$

$$\frac{1}{9} \begin{bmatrix} -1 & -3 \\ -3 & 0 \end{bmatrix} = \text{---}$$