

SBG STUDY

1. Let 'E' be the ellipse $\frac{x^2}{9} + \frac{y^2}{4} = 1$ & 'C' be the circle $x^2 + y^2 = 9$. Let P & Q be the points (1, 2) and (2, 1) respectively. Then :

- (A) Q lies inside C but outside E (B) Q lies outside both C & E
(C) P lies inside both C & E (D) P lies inside C but outside E.

2. The eccentricity of the ellipse $(x - 3)^2 + (y - 4)^2 = \frac{y^2}{9}$ is

- (A) $\frac{\sqrt{3}}{2}$ (B) $\frac{1}{3}$ (C) $\frac{1}{3\sqrt{2}}$ (D) $\frac{1}{\sqrt{3}}$

3. The equation, $2x^2 + 3y^2 - 8x - 18y + 35 = K$ represents

- (A) no locus if $K > 0$ (B) an ellipse if $K < 0$ (C) a point if $K = 0$ (D) a hyperbola if $K > 0$

4. If the ellipse $\frac{(x-h)^2}{M} + \frac{(y-k)^2}{N} = 1$ has major axis on the line $y = 2$, minor axis on the line $x = -1$,

major axis has length 10 and minor axis has length 4. The number h,k,M,N (in this order only) are-

- (A) -1,2,5,2 (B) -1,2,10,4 (C) 1,-2,25,4 (D) -1,2,25,4

5. A circle has the same centre as an ellipse & passes through the foci F_1 & F_2 of the ellipse, such that the two curves intersect in 4 points. Let 'P' be any one of their point of intersection. If the major axis of the ellipse is 17 & the area of the triangle PF_1F_2 is 30, then the distance between the foci is :

- (A) 11 (B) 12 (C) 13 (D) none

6. The latus rectum of a conic section is the width of the function through the focus. The positive difference between the length of the latus rectum of $3y = x^2 + 4x - 9$ and $x^2 + 4y^2 - 6x + 16y = 24$ is-

- (A) $\frac{1}{2}$ (B) 2 (C) $\frac{3}{2}$ (D) $\frac{5}{2}$

7. Imagine that you have two thumbtacks placed at two points, A and B. If the ends of a fixed length of string are fastened to the thumbtacks and the string is drawn taut with a pencil, the path traced by the pencil will be an ellipse. The best way to maximise the area surrounded by the ellipse with a fixed length of string occurs when

- I the two points A and B have the maximum distance between them.
II two points A and B coincide.
III A and B are placed vertically.
IV The area is always same regardless of the location of A and B.

- (A) I (B) II (C) III (D) IV

8. Let S(5,12) and S'(-12,5) are the foci of an ellipse passing through the origin. The eccentricity of ellipse equals -

- (A) $\frac{1}{2}$ (B) $\frac{1}{\sqrt{3}}$ (C) $\frac{1}{\sqrt{2}}$ (D) $\frac{2}{3}$

9. The y-axis is the directrix of the ellipse with eccentricity $e = 1/2$ and the corresponding focus is at (3, 0), equation to its auxiliary circle is

- (A) $x^2 + y^2 - 8x + 12 = 0$ (B) $x^2 + y^2 - 8x - 12 = 0$
(C) $x^2 + y^2 - 8x + 9 = 0$ (D) $x^2 + y^2 = 4$

10. Equation of the common tangent to the ellipses, $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ and $\frac{x^2}{a^2} + \frac{y^2}{a^2 + b^2} = 1$ is -
- (A) $ay = bx + \sqrt{a^4 - a^2b^2 + b^4}$ (B) $by = ax - \sqrt{a^4 + a^2b^2 + b^4}$
 (C) $ay = bx - \sqrt{a^4 + a^2b^2 + b^4}$ (D) $by = ax + \sqrt{a^4 - a^2b^2 + b^4}$
11. $x - 2y + 4 = 0$ is a common tangent to $y^2 = 4x$ & $\frac{x^2}{4} + \frac{y^2}{b^2} = 1$. Then the value of b and the other common tangent are given by :
- (A) $b = \sqrt{3}$; $x + 2y + 4 = 0$ (B) $b = 3$; $x + 2y + 4 = 0$
 (C) $b = \sqrt{3}$; $x + 2y - 4 = 0$ (D) $b = \sqrt{3}$; $x - 2y - 4 = 0$
12. If α & β are the eccentric angles of the extremities of a focal chord of an standard ellipse, then the eccentricity of the ellipse is :
- (A) $\frac{\cos \alpha + \cos \beta}{\cos(\alpha + \beta)}$ (B) $\frac{\sin \alpha - \sin \beta}{\sin(\alpha - \beta)}$ (C) $\frac{\cos \alpha - \cos \beta}{\cos(\alpha - \beta)}$ (D) $\frac{\sin \alpha + \sin \beta}{\sin(\alpha + \beta)}$
13. An ellipse is inscribed in a circle and a point within the circle is chosen at random. If the probability that this point lies outside the ellipse is $\frac{2}{3}$ then the eccentricity of the ellipse is :
- (A) $\frac{2\sqrt{2}}{3}$ (B) $\frac{\sqrt{5}}{3}$ (C) $\frac{8}{9}$ (D) $\frac{2}{3}$
14. Consider the particle travelling clockwise on the elliptical path $\frac{x^2}{100} + \frac{y^2}{25} = 1$. The particle leaves the orbit at the point $(-8, 3)$ and travels in a straight line tangent to the ellipse. At what point will the particle cross the y -axis?
- (A) $\left(0, \frac{25}{3}\right)$ (B) $\left(0, \frac{23}{3}\right)$ (C) $(0, 9)$ (D) $\left(0, \frac{26}{3}\right)$
15. The locus of the middle point of chords of an ellipse $\frac{x^2}{16} + \frac{y^2}{25} = 1$ passing through $P(0, 5)$ is another ellipse E . The coordinates of the foci of the ellipse E , is
- (A) $\left(0, \frac{3}{5}\right)$ and $\left(0, \frac{-3}{5}\right)$ (B) $(0, -4)$ and $(0, 1)$
 (C) $(0, 4)$ and $(0, 1)$ (D) $\left(0, \frac{11}{2}\right)$ and $\left(0, \frac{-1}{2}\right)$
16. (a) Which of the following is an equation of the ellipse with centre $(-2, 1)$, major axis running from $(-2, 6)$ to $(-2, -4)$ and focus at $(-2, 5)$?
- (A) $\frac{(x-2)^2}{25} + \frac{(y+1)^2}{16} = 1$ (B) $\frac{(x+2)^2}{25} + \frac{(y-1)^2}{9} = 1$
 (C) $\frac{(x-2)^2}{9} + \frac{(y+1)^2}{25} = 1$ (D) $\frac{(x+2)^2}{9} + \frac{(y-1)^2}{25} = 1$
- (b) Which of the following statement(s) is/are correct for the ellipse of 8(a) ?
- (A) auxiliary circle is $(x+2)^2 + (y-1)^2 = 25$
 (B) director circle is $(x+2)^2 + (y-1)^2 = 34$
 (C) Latus rectum = $\frac{18}{5}$ (D) eccentricity = $\frac{4}{5}$

17. The normal at a variable point P on an ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ of eccentricity e meets the axes of the ellipse in Q and R then the locus of the mid-point of QR is a conic with an eccentricity e' such that :

- (A) e' is independent of e (B) $e' = 1$
 (C) $e' = e$ (D) $e' = 1/e$

18. The area of the rectangle formed by the perpendiculars from the centre of the standard ellipse to the tangent and normal at its point whose eccentric angle is $\pi/4$, is :

- (A) $\frac{(a^2 - b^2) ab}{a^2 + b^2}$ (B) $\frac{(a^2 - b^2)}{(a^2 + b^2) ab}$ (C) $\frac{(a^2 - b^2)}{ab(a^2 + b^2)}$ (D) $\frac{a^2 + b^2}{(a^2 - b^2) ab}$

19. If P is any point on ellipse with foci S_1 & S_2 and eccentricity is $\frac{1}{2}$ such that

$\angle PS_1S_2 = \alpha$, $\angle PS_2S_1 = \beta$, $\angle S_1PS_2 = \gamma$, then $\cot \frac{\alpha}{2}$, $\cot \frac{\gamma}{2}$, $\cot \frac{\beta}{2}$ are in

- (A) A.P. (B) G.P.
 (C) H.P. (D) *NOT* A.P., G.P. & H.P.