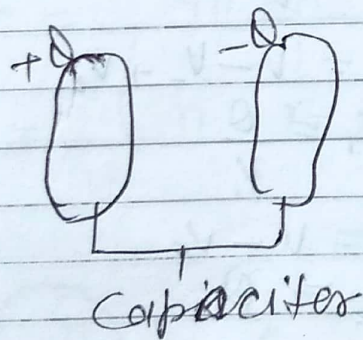


# SBG STUDY

27/06/17

## Capacitor or Condenser

- \* It is a device which stores electrical energy
- \* Generally It is a combination of two conductors both the conductors are called plates of capacitor whatever be the shape of conductor
- \* Generally both the plates have equal and opposite charge hence net charge on capacitor is zero.



$$Q_{\text{net}} = 0$$

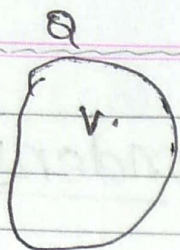
Charge on capacitor =

$$= \text{Charge on } + \text{ve plate} \\ = Q.$$

\* Capacitance of capacitor = (C) :  
unit Farad (F)

It is the capacity of a capacitor to store electrostatic energy or electric charge





$$Q \propto V$$

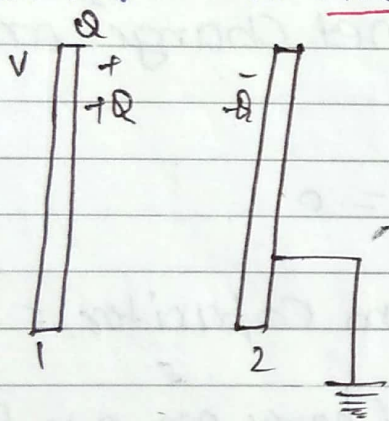
$$Q = CV$$

$$C = \frac{Q}{V} \quad \text{C/volts} = \text{F}$$

\* It is independent of charge and potential.

## \* Principle of Capacitor

Every Conductor have a maximum Capacity to store charge. To increase capacitance two conductors are used and one of the conductor is grounded.



$$C = \frac{Q}{V}$$

$$V_1 = V - V_- + V_2$$

$$C_1 = \frac{Q}{V_1}$$

$$V_2 = V - V_-$$

$$C_2 = \frac{Q}{V_2}$$

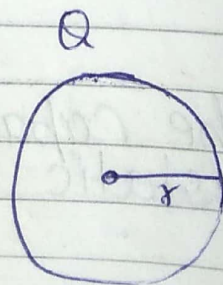
## \* Types of Capacitors

1. Spherical capacitor:

(i) Isolated sphere

$$V = \frac{Q}{4\pi\epsilon_0 r}$$

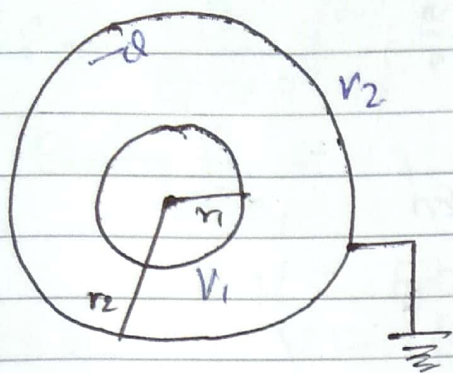
$$C = \frac{Q}{V}$$



$$C = 4\pi\epsilon_0 r$$



(ii)



$$V_1 = \frac{+Q}{4\pi\epsilon_0 r_1} - \frac{-Q}{4\pi\epsilon_0 r_2}$$

$$V_2 = 0$$

$$V = \frac{+Q}{4\pi\epsilon_0 r_1} - \frac{-Q}{4\pi\epsilon_0 r_2}$$

$$V = \frac{Q}{4\pi\epsilon_0} \left( \frac{1}{r_1} - \frac{1}{r_2} \right)$$

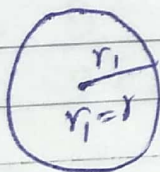
$$V = \frac{Q}{4\pi\epsilon_0} \left( \frac{r_2 - r_1}{r_1 r_2} \right)$$

$$C = \frac{Q}{V}$$

$$C = 4\pi\epsilon_0 \left( \frac{r_1 r_2}{r_2 - r_1} \right)$$

$$C = \frac{4\pi\epsilon_0}{\left( \frac{1}{r_1} - \frac{1}{r_2} \right)}$$

\*

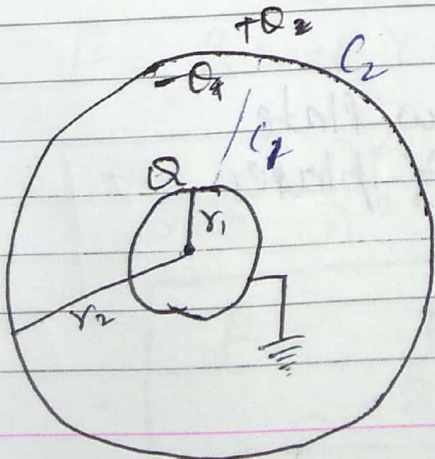


$$r_2 = \infty$$

$$C = \frac{4\pi\epsilon_0}{\frac{1}{r} - \frac{1}{\infty}}$$

$$C = 4\pi\epsilon_0 r$$

\*



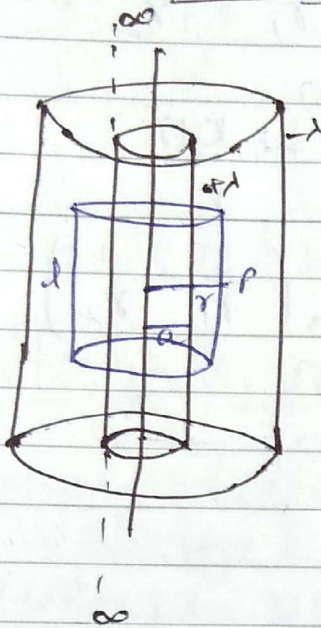
$$C_1 = 4\pi\epsilon_0 \left( \frac{r_1 r_2}{r_2 - r_1} \right)$$

$$C_2 = 4\pi\epsilon_0 r_2$$

$$C = C_1 + C_2$$



## \* Cylindrical Capacitor



$$E = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$C = \frac{Q}{V}$$

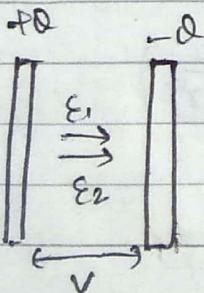
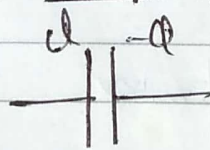
$$V = \int_a^b E dr$$

$$V = \frac{\lambda}{2\pi\epsilon_0} \ln\left(\frac{b}{a}\right)$$

$$\frac{\lambda}{V} = \frac{2\pi\epsilon_0}{\ln\left(\frac{b}{a}\right)}$$

Capacitance / length =  $\frac{2\pi\epsilon_0}{\ln\left(\frac{b}{a}\right)}$

## \* parallel plates capacitor



$d \rightarrow$  Sep. b/w plate  
 $A \rightarrow$  Area of plates

$$E = \frac{Q}{\epsilon_0 A}$$



$$\epsilon_2 = \frac{Q}{2\epsilon_0 A}$$

$$E = \frac{Q}{2\epsilon_0 A} = E = \frac{Q}{\epsilon_0 A}$$

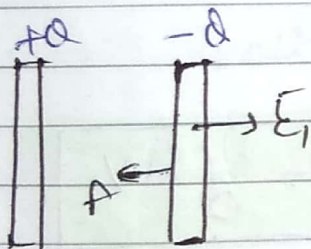
$$V = Ed$$

$$V = \frac{Qd}{\epsilon_0 A}$$

$$C = \frac{Q}{V}$$

$$C = \frac{\epsilon_0 A}{d}$$

\* Force b/w the plates of capacitors:



$$C = \frac{Q}{V}, \quad C = \frac{\epsilon_0 A}{d}$$

$$F = Q\epsilon_1 \\ = Q \cdot \frac{Q}{2\epsilon_0 A}$$

$$F = \frac{Q^2}{2\epsilon_0 A}$$

$$P_{elect} = \frac{\sigma^2}{2\epsilon_0}$$

$$F = P_{elect} \times A = \frac{\sigma^2}{2\epsilon_0} A$$

$$= \frac{1}{2\epsilon_0} \frac{Q^2}{A^2} \cdot A$$

$$F = \frac{Q^2}{2\epsilon_0 A}$$



# \* Energy in Capacitor:

Capacitor stored energy in the electric field b/w its plate

Energy density - Energy/vol. =  $\frac{1}{2} \epsilon_0 E^2$

total energy of capacitor = potential energy capacitor

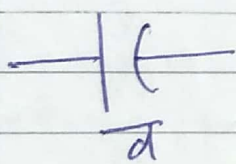
$$U = \frac{1}{2} \epsilon_0 E^2 \times Ad$$

$$= \frac{1}{2} \epsilon_0 \frac{Q^2}{\epsilon^2 A^2} \times Ad$$

$$Q = CV$$

$$= \frac{Q^2 d}{2 \epsilon_0 A}$$

$$U = \frac{Q^2}{2C} = \frac{1}{2} CV^2 = \frac{1}{2} QV$$

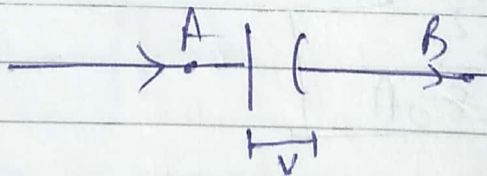


$$C = \frac{\epsilon_0 A}{d}$$

$$E = \frac{Q}{\epsilon_0 A}$$

$$A = \frac{Q^2}{2 \epsilon_0 A}$$

$$U = \frac{Q^2}{2C} = \frac{1}{2} CV^2$$



$$V = \frac{Q}{C}$$

$$V_A - \frac{Q}{C} = V_B$$

$$V_A - V_B = \frac{Q}{C} = V$$

$$C = \frac{\epsilon_0 A}{d}$$



\* work done by battery =  $W_b = \text{charge given by battery} \times \text{EMF}$

$$= CV \times V$$

$$= CV^2.$$

\* Heat =  $W_b - \Delta U$

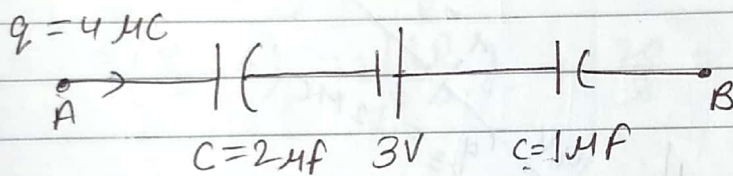
$$= CV^2 - \frac{1}{2} CV^2$$

Heat =  $\frac{1}{2} CV^2$

$$Q = CV$$

$$V = \frac{Q}{C}$$

Ques:



$$Q = CV$$

$$V = \frac{Q}{C}$$

If  $V_A = 10 \text{ volt}$  then find  $V_B$ .

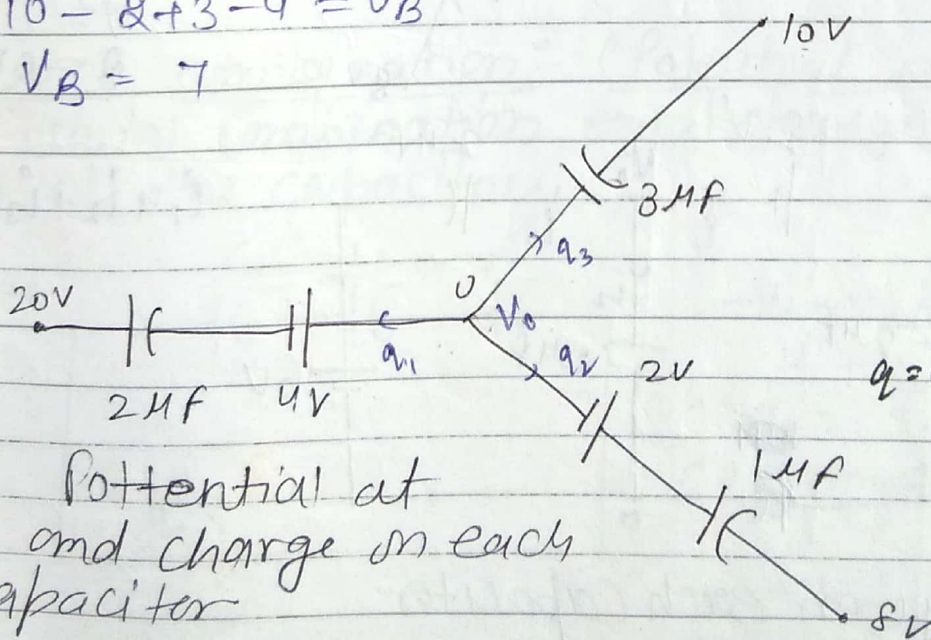
$$Q = CV$$

$$V_A - 2 + 3 - 4 = V_B$$

$$10 - Q + 3 - 4 = V_B$$

$$V_B = 7$$

Ques



$$Q = CV$$

$$V = \frac{Q}{C}$$

$$q_1 + q_2 + q_3 = 0$$

$$Q = CV$$

$$Q = CV$$

$$Q = CV$$

find potential at O and charge on each capacitor



$$q_1 + q_2 + q_3 = 0$$

$$2(V_0 - 24) + 1(V_0 - 6) + 3(V_0 - 10) = 0$$

$$2V_0 - 48 + V_0 - 6 + 3V_0 - 30 = 0$$

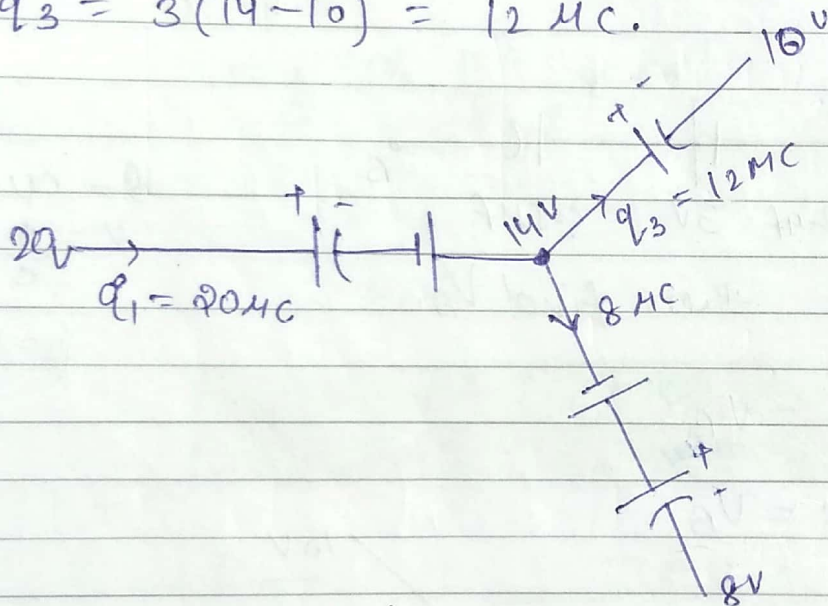
$$6V_0 - 84 = 0$$

$$V_0 = \frac{84}{6} = 14 \text{ V.}$$

$$q_1 = 2(14 - 24) = -20 \mu\text{C}$$

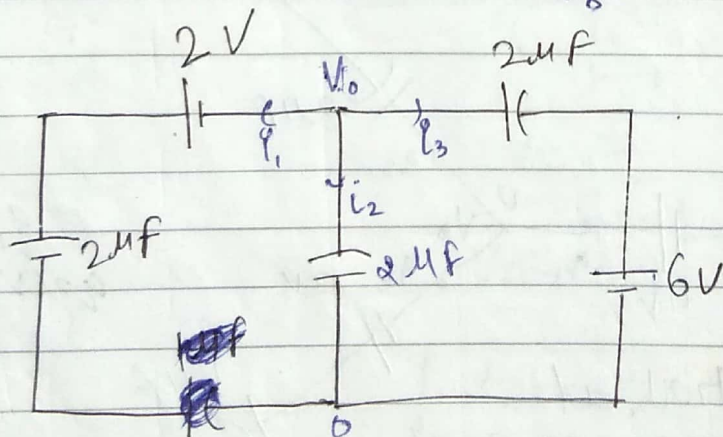
$$q_2 = 1(14 - 6) = 8 \mu\text{C}$$

$$q_3 = 3(14 - 10) = 12 \mu\text{C}$$



$$Q = CV$$

Que:



$$q_1 + q_2 + q_3 = 0$$

$$Q = C$$

Find charge on each capacitor



$$\frac{1}{3} V_0$$

$$q_1 + q_2 + q_3 = 0$$

$$V_0 + 2 + 4 + 2 = 0$$

$$3(V_0 + 2) + 2(V_0 - 6) = 0$$

$$2(V_0 + 2) + 2V_0 + 2(V_0 - 6) = 0$$

$$6V_0 = 8$$

$$V_0 = \frac{8}{6}$$

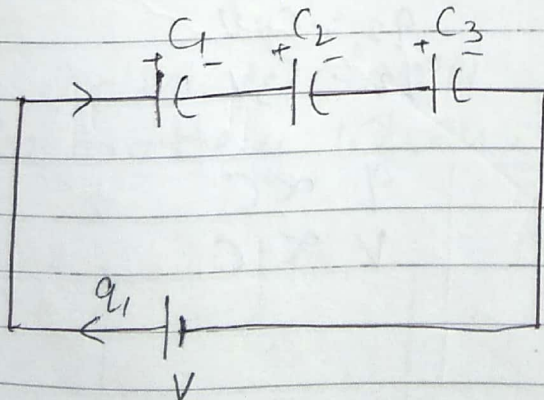
$$V_0 = \frac{4}{3}$$

$$q_1 = 2\left(\frac{4}{3} + 2\right) = 2\left(\frac{10}{3}\right) = \frac{20}{3} = 6.6$$

### \* Combination of capacitor :

#### (1) Series combination : (Potential divider)

In series combination equal charge flow through all the capacitors.



$$-V_1 - V_2 - V_3 + V = 0$$

$$V_1 + V_2 + V_3 = V$$

$$C_1 V_1 = C_2 V_2 = C_3 V_3 = q$$

$$CV = \text{constant}$$

$$V \propto \frac{1}{C}$$



$$V \propto \frac{1}{C}$$

$$\frac{V_1}{V_2} = \frac{C_2}{C_1}$$

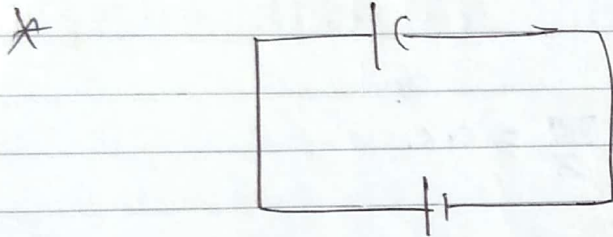
$$Q = CV$$

$$PE = U = \frac{q^2}{2C}$$

$$\text{Energy} = V \propto \frac{1}{C}$$

$$\frac{V_1}{V_2} = \frac{C_1}{C_2}$$

$$\frac{C_2}{C_1}$$



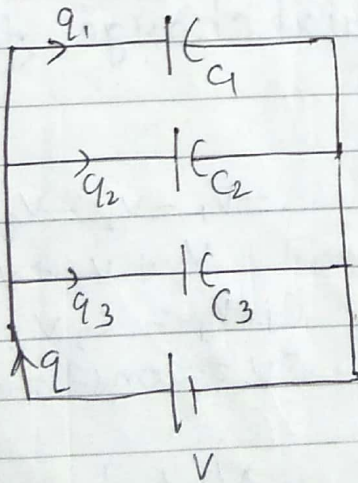
$$V_1 + V_2 + V_3 = V$$

$$\frac{q}{C_1} + \frac{q}{C_2} + \frac{q}{C_3} = \frac{q}{C_{eq}}$$

$$q = C_{eq} V$$

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$$

\* Parallel Combination of (Charge dividers)



$$q = q_1 + q_2 + q_3 + \dots$$

$$q_1 = C_1 V$$

$$q_2 = C_2 V$$

$$q_3 = C_3 V$$

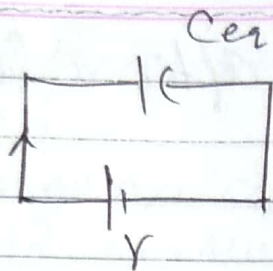
$$q \propto C$$

$$V \propto C$$



J-M  
S-1

$\frac{V}{2}$   
 $\frac{V}{4}$

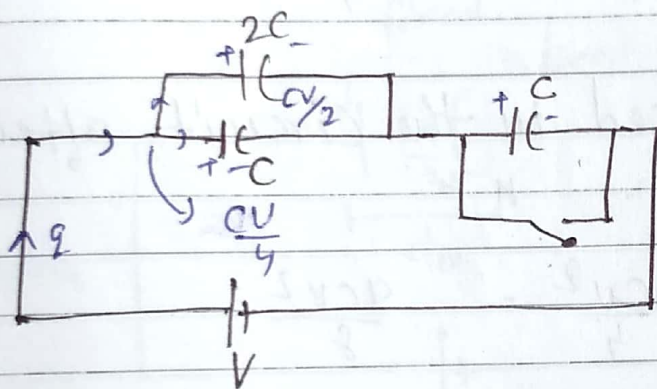


$$q = C_{eq} V$$

$$C_{eq} = C_1 V + C_2 V + C_3 V + \dots$$

$$C_{eq} = C_1 + C_2 + C_3 + \dots$$

Que



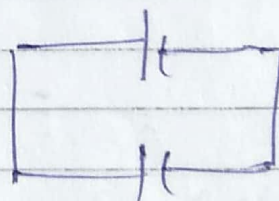
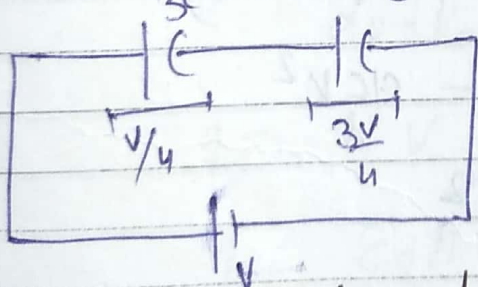
Find charge on each capacitor.

$$\frac{1}{3C} + \frac{1}{C} = \frac{1+3}{3} = \frac{4}{3}$$

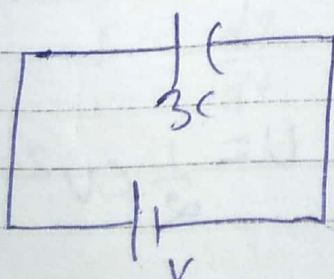
$$\frac{3}{4} C = \frac{3C}{4}$$

$$Q = CV$$

$$= \frac{3CV}{4} = \frac{3CV}{4}$$



(iii) Now switch is closed find charge given by the battery when switch is closed.



Charge given by battery =  $q - q_0$

$$3eV - \frac{3CV}{4}$$

$$= \frac{9CV}{4}$$



(iii) find work done by the Battery after closing the switch.

$$W_B = \frac{1}{2} CV^2$$

= Charge given by battery  $\times$  EMF.

$$= \frac{qCV}{4} \times V = \frac{qCV^2}{4}$$

(iv) find heat produced in the circuit after closing the switch.  $H =$

$$H = \frac{1}{2} \frac{qCV^2}{4} = \frac{qCV^2}{8}$$

$H = 2$

$$H = W_B - \Delta U$$

$$= \frac{qCV^2}{4} - (V_f - V_i)$$

$$= \frac{qCV^2}{4} - \frac{qCV^2}{8}$$

$$= \frac{qCV^2}{8}$$

$$V_f = \frac{1}{2} \frac{3CV^2}{4}$$

$$V_i = \frac{1}{2} \frac{3CV^2}{4}$$

Sup:

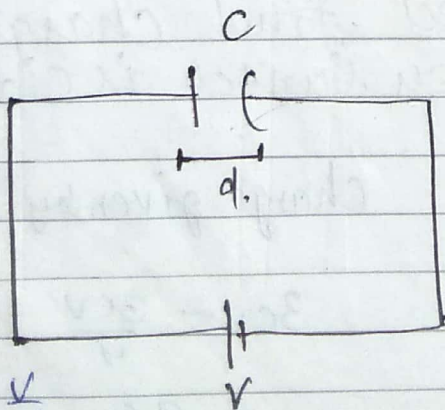


Plate Area = A

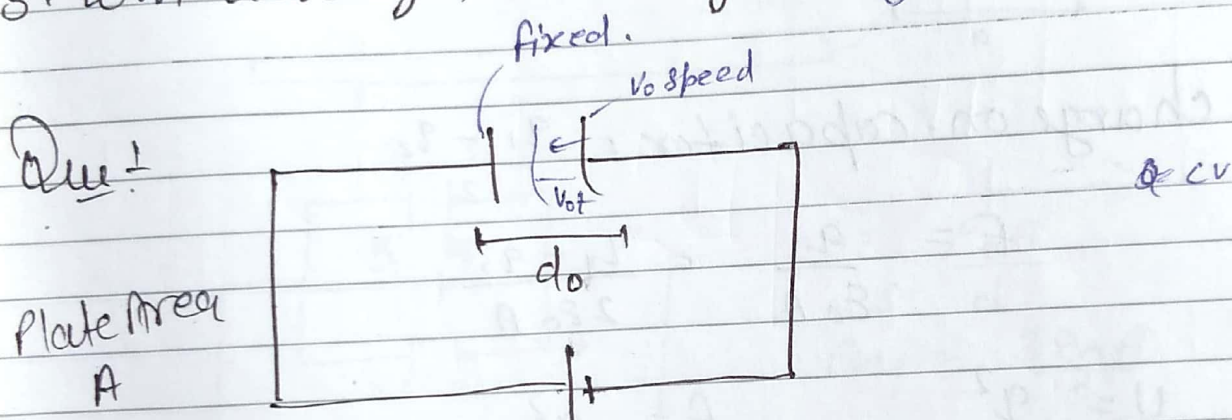
$$U = \frac{1}{2} CV^2$$

$$\epsilon_0 A = \frac{Q}{\epsilon_0 A} = \frac{V}{d}$$



If separation b/w the plates is increased then

1. charge on capacitor  $C = \frac{\epsilon_0 A}{d}$  charge decrease,  $\frac{Q}{\epsilon_0 A}$
2. E. field b/w the plates  $\propto$  decrease.
3. P.E b/w the plates  $\propto$  increase decrease.
4. force of attraction  $\propto$  decrease.  $F = \frac{Q^2}{2\epsilon_0 A}$
5. work done by the battery  $\propto$  Negative.



Find charge on capacitor after time  $t$ .

$$C_t = \frac{\epsilon_0 A}{d_0 - v_0 t}$$

$$q = C_t V$$

$$q = \frac{\epsilon_0 A V}{d_0 - v_0 t}$$

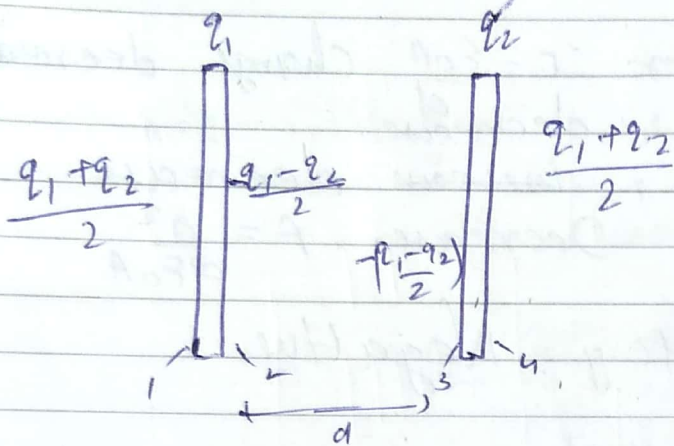
Time  $\uparrow$  Charge  $\uparrow$

\* Find current in the circuit at any time  $t$ .

$$I = \frac{dq}{dt} = \frac{d}{dt} \left( \frac{\epsilon_0 A V}{d_0 - v_0 t} \right)$$



(iii) Capacitor having unequal charge on its plates.



charge on capacitor =  $\frac{q_1 - q_2}{2}$

$$E = \frac{q}{2\epsilon_0 A} = \frac{q_1 - q_2}{2\epsilon_0 A}$$

$$U = \frac{q^2}{2C}$$

$$F = \frac{q^2}{2\epsilon_0 A}$$

$$C = \frac{\epsilon_0 A}{d}$$

$$\frac{50-10}{2} = \frac{30}{2}$$

Que!

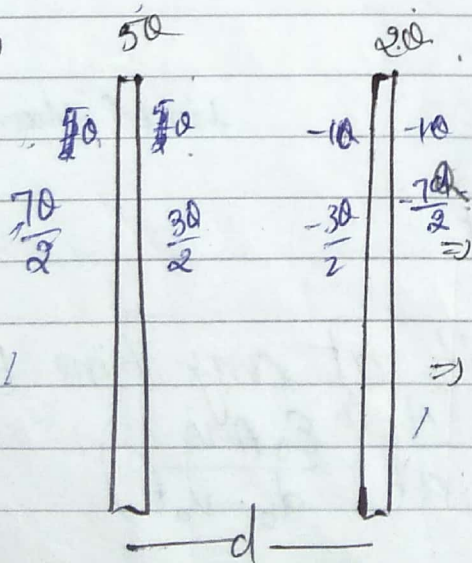


Plate Area A

Find charge on capacitor  $\frac{30}{2}$

$\Rightarrow$  E f b/w the plates.

$$E = \frac{30}{2\epsilon_0 A}$$

W/B

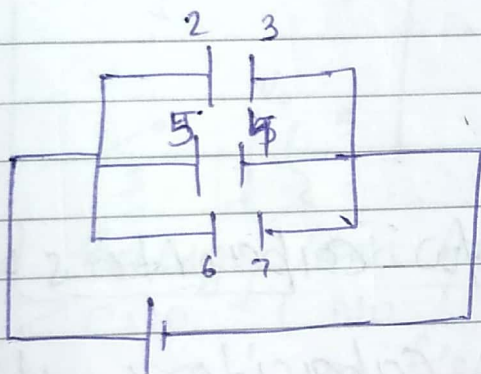
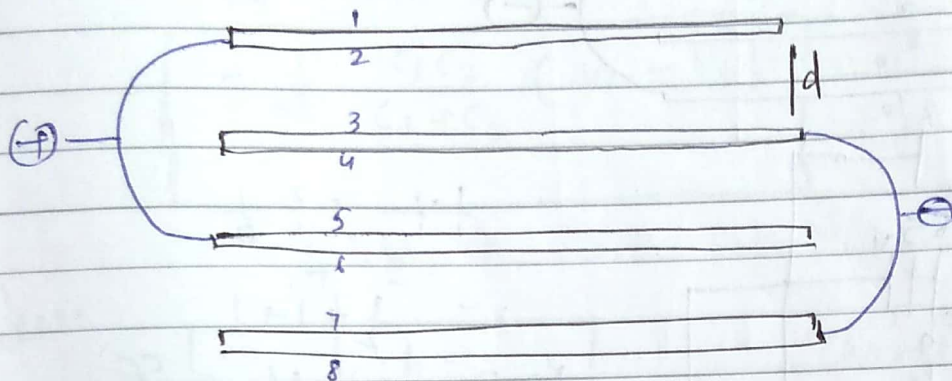


30/06/17

# \* Capacitance of combination of parallel plates:

Ex: Find eq capacitance!  $C_{eq} = ?$

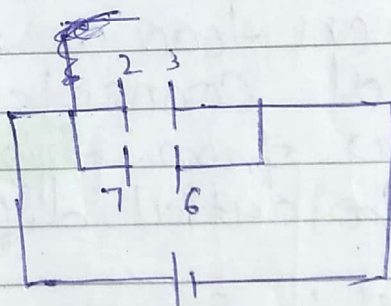
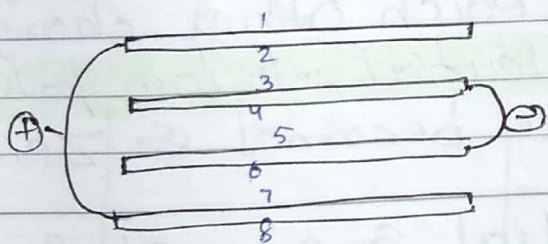
Area = A



$$C = \frac{\epsilon_0 A}{d}$$

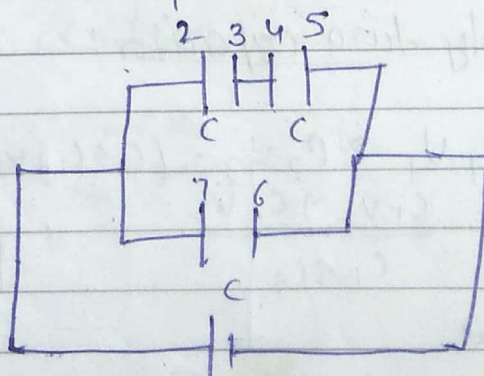
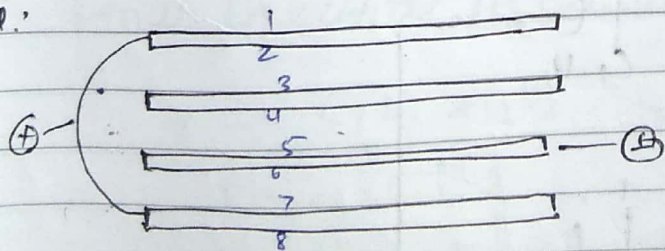
$$C_{eq} = \frac{3\epsilon_0 A}{d}$$

Sol:



$$= \frac{2\epsilon_0 A}{d}$$

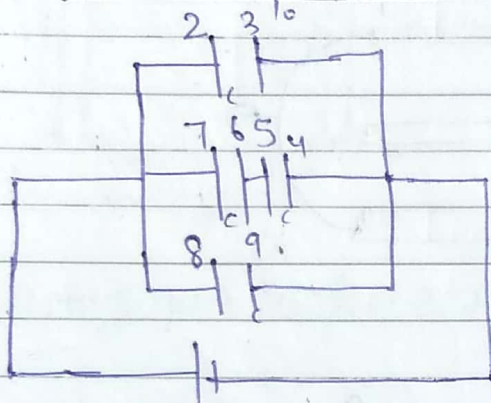
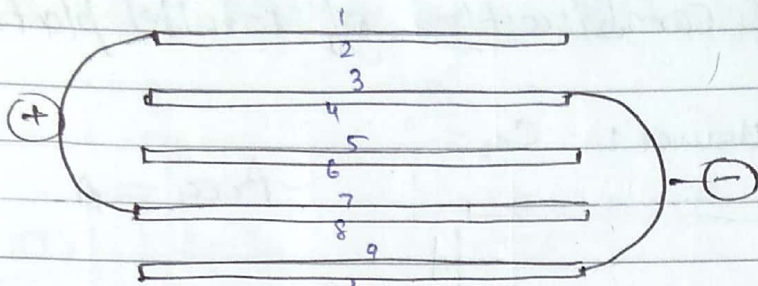
Sol:



$$\frac{3C}{2} = \frac{3\epsilon_0 A}{2d}$$



Que!



$$\frac{1}{1} + \frac{1}{1} = \frac{2}{1} = \frac{1}{\frac{1}{2}}$$

$$R_{eq} = \frac{\frac{1}{2} + 1 + 1}{\frac{1}{2} + 2} = \frac{5C}{2}$$

### \* Charge sharing b/w capacitors :-

When two or more capacitors at different potential connected to each other charge flow from **high potential to low potential** till potential difference becomes zero.

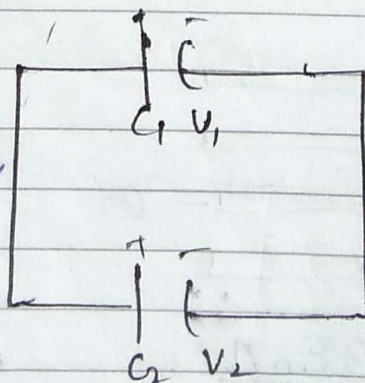
In this process potential energy of system decreases in the form of Heat.

only two capacitor!

$$C_1 V_1 + C_2 V_2 = (C_1 + C_2) V$$

$$V = \frac{C_1 V_1 + C_2 V_2}{C_1 + C_2}$$

Heat



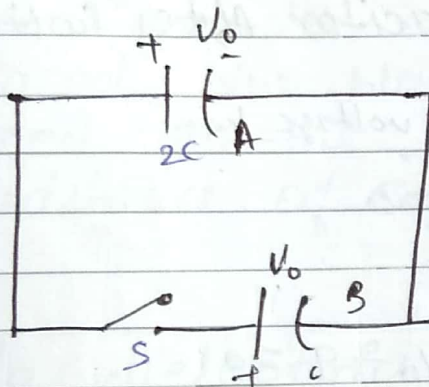


Heat + produced = loss in PE =  $U_i - U_f$

$$= \frac{1}{2} C_1 V_1^2 + \frac{1}{2} C_2 V_2^2 - \frac{1}{2} (C_1 + C_2) V^2$$

$$= \frac{1}{2} \frac{C_1 C_2}{C_1 + C_2} (V_1 - V_2)^2$$

Ques:

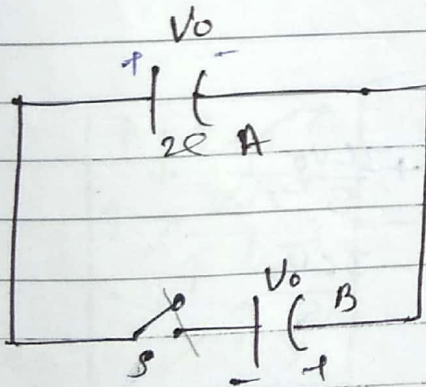


Charge is not flow because potential is same

Final Energy loss After switch the close.

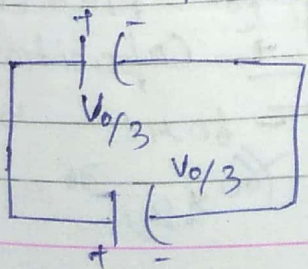
Ans:  $\geq$  zero (No loss energy because no flow of charge)

Q.



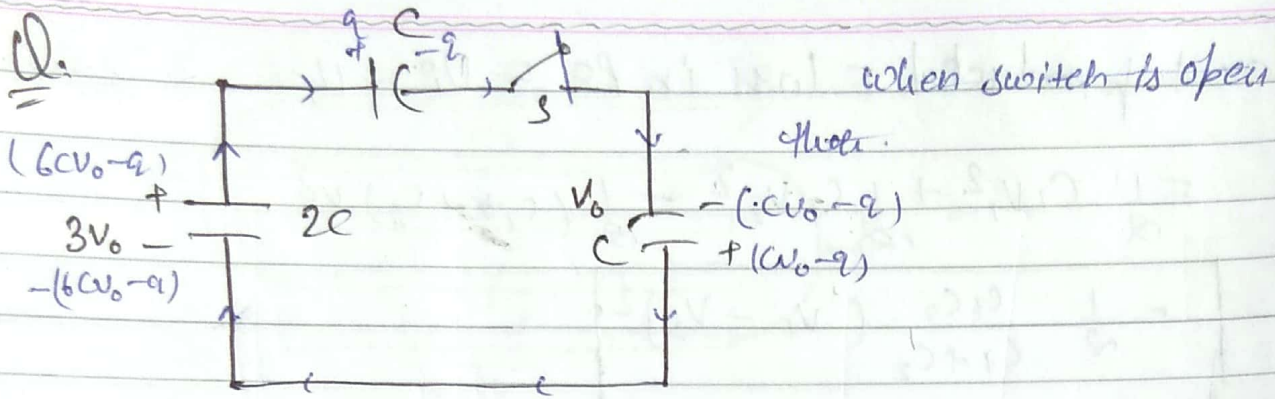
Final potential After switch is closed

$$V = \frac{C_1 V_1 + C_2 V_2}{C_1 + C_2} = \frac{2C V_0 - C V_0}{3C} = \frac{V_0}{3}$$





$$Q = CV \quad V = \frac{Q}{C}$$



Final charge on each Capacitor After switch is closed.

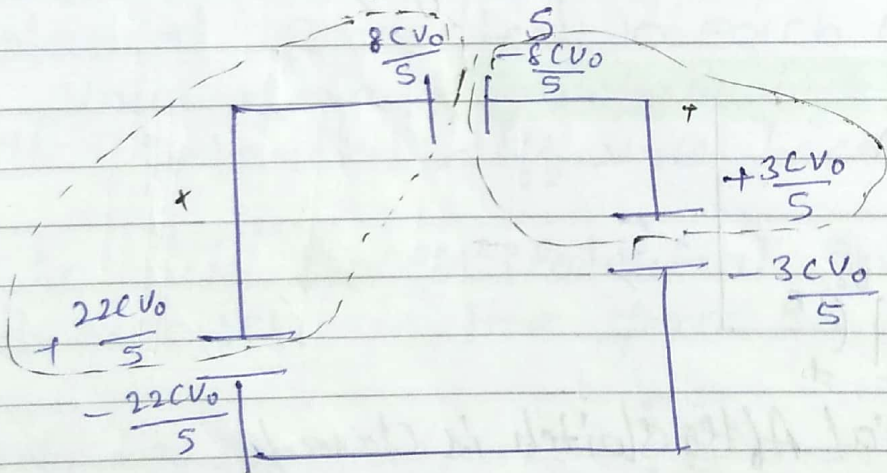
By using Kirchhoff voltage law.

$$-\frac{q}{C} + \frac{CV_0 - q}{C} + \frac{6CV_0}{2C} = 0$$

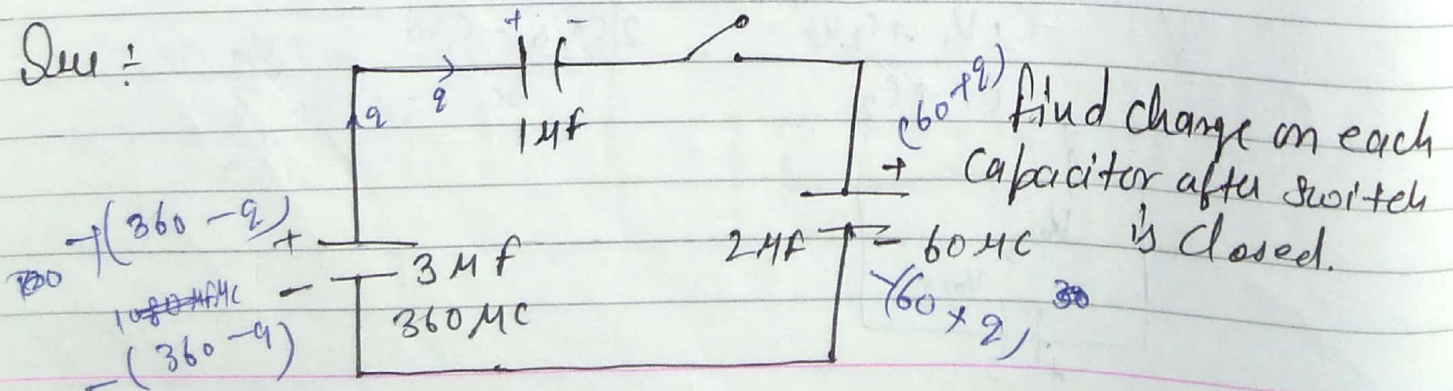
$$-2q + 2CV_0 - 2q + 6CV_0 - q = 0$$

$$8CV_0 = 5q$$

$$q = \frac{8CV_0}{5}$$



Q.2



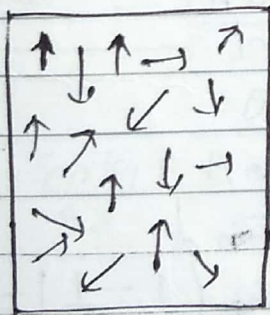


Capu  $\rightarrow$  S-1  $\rightarrow$  1 to 6.  
0-1  $\rightarrow$  1 to 7,  
elec. 0-1, 2, 3, 5

$$\frac{-a}{T} - \frac{60 + a}{2} + \frac{360 - a}{3} = 0$$

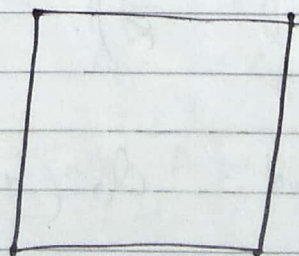
\* Dielectrics : Dielectrics are the materials having low conductivity. Hence basically these are non conductors. When a dielectric medium is placed b/w plates of capacitor charge induced on the face of dielectric and capacitance of capacitor increases.

(i) Polar dielectrics : If protons and electrons are not distributed uniformly then their centre of mass does not coincide and atom behaves as a dipole.



$$P = 0$$

(ii) Non polar dielectric :

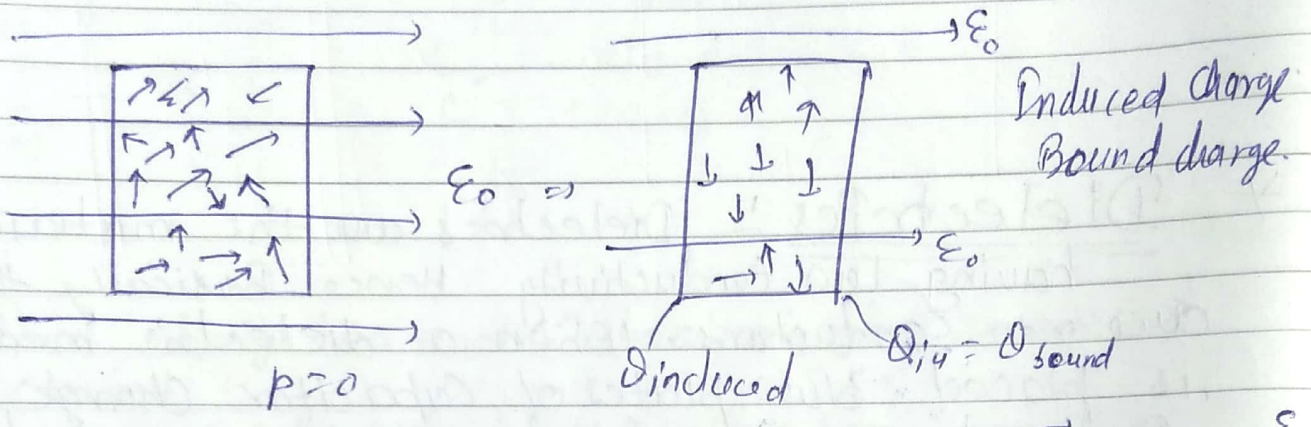


$$P = 0$$



11/07/17

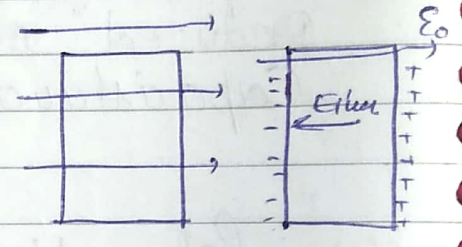
\* Dielectric in External field:



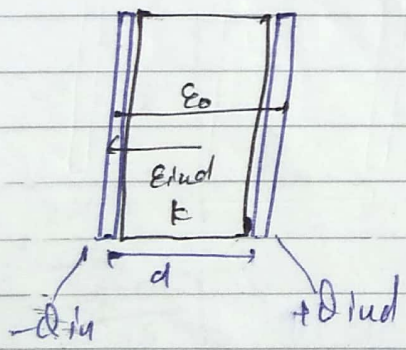
$$E_{net} = E_0 - E_p = \frac{E_0}{K}$$

$$E_{ind} = E_0 \left(1 - \frac{1}{K}\right)$$

Conductor  $K = \infty$



\* Capacitor having dielectric:



$$C_0 = \frac{\epsilon_0 A}{d}$$

$$\epsilon_0 = \frac{Q}{\epsilon_0 A}$$

$$V_0 = E_0 d$$

$$E_{ind} = \epsilon_0 \left(1 - \frac{1}{K}\right) = \frac{Q_{ind}}{\epsilon_0 A}$$

$$\frac{Q_0}{\epsilon_0 A} \left(1 - \frac{1}{K}\right) = \frac{Q_{ind}}{\epsilon_0 A}$$

$$Q_{ind} = Q_0 \left(1 - \frac{1}{K}\right)$$



dir. of charge - area

Net Electric Field b/w the plates after dielectric is inserted

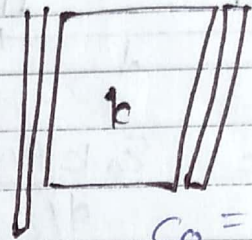
$$E_{net} = \frac{E_0}{k}$$

Pot. diff b/w the plates

$$\Delta V = \underline{E_{net} d}$$

$$\Delta V = \frac{E_0 d}{k}$$

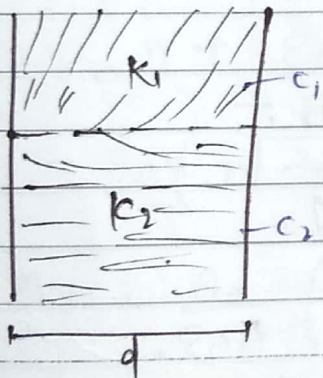
$$C = \frac{\epsilon_0 k A}{d}$$



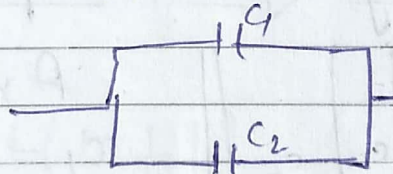
$$C_0 = \frac{\epsilon_0 A}{d}$$

$$C = \frac{\epsilon_0 k A}{d} = k C_0$$

Ques:



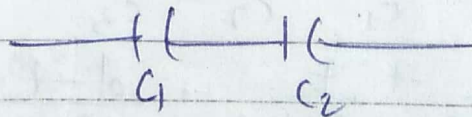
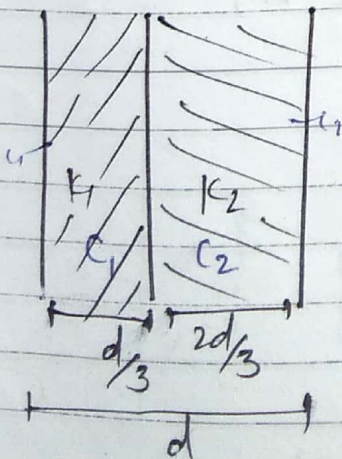
Find Capacitance  
plate Area - A



$$C_{eq} = C_1 + C_2$$

$$C_1 = \frac{\epsilon_0 k_1 A}{2d}, \quad C_2 = \frac{\epsilon_0 k_2 A}{2d}$$

Q.:



$$C_1 = \frac{3\epsilon_0 k_1 A}{d}$$

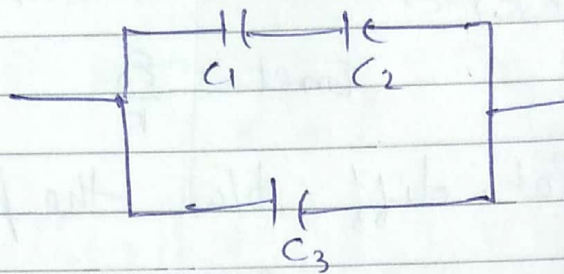
$$C_2 = \frac{3\epsilon_0 k_2 A}{2d}$$



Sol:



Plate Area = A

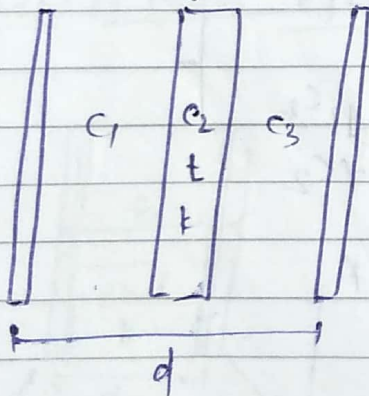


$$C_1 = \frac{\epsilon_0 k A/2}{d/2} = \frac{\epsilon_0 k A}{d}$$

$$C_2 = \frac{\epsilon_0 2k A/2}{d/2} = \frac{2\epsilon_0 k A}{d}$$

$$C_3 = \frac{\epsilon_0 3k A/2}{d}$$

\* Partially filled capacitor:



Area = A.

$$C_1 = \frac{\epsilon_0 A}{n}$$

$$C_2 = \frac{\epsilon_0 k A}{t}$$

$$C_3 = \frac{\epsilon_0 A}{(d-t-n)}$$

$$\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$$

$$\frac{n}{\epsilon_0 A} + \frac{t}{\epsilon_0 k A} + \frac{d-t-n}{\epsilon_0 A}$$

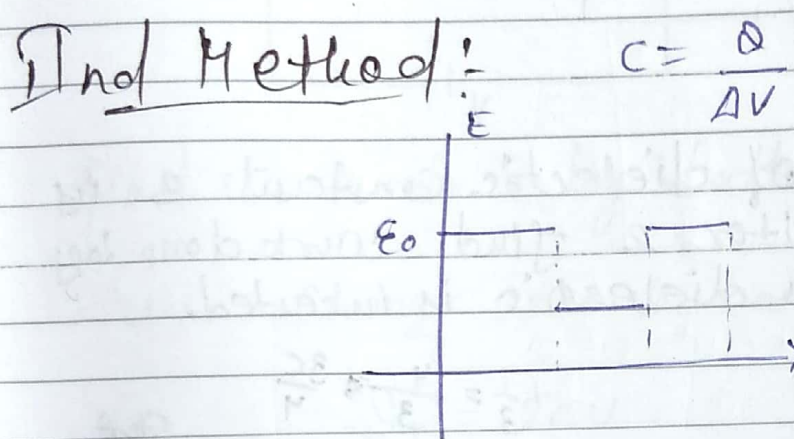
$$= \frac{1}{\epsilon_0 A} \left[ n + \frac{t}{k} + d-t-n \right]$$

$$= \frac{1}{C} = \frac{d-t + \frac{t}{k}}{\epsilon_0 A}$$



Cap -> 8-1 => 7, 8  
 0-1 => upto 15  
 = 25, 26, 27  
 0-2 => 1 to 6. 10 and 11  
 J.M => 1, 10, 11, 12, 13, 14, 15

$$C = \frac{\epsilon_0 A}{d - t \left(1 - \frac{1}{k}\right)}$$



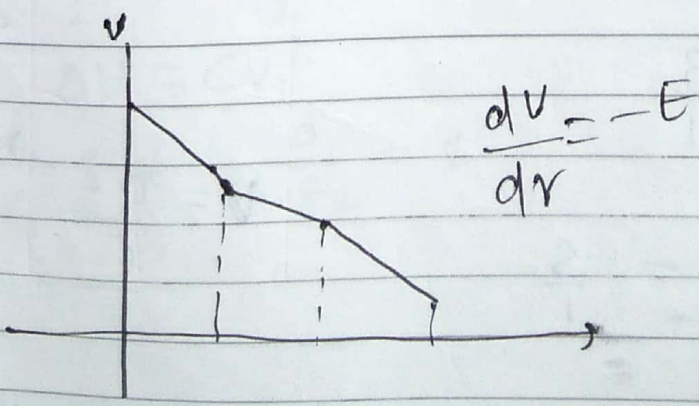
$$\Delta V = E \Delta r$$

$$\Delta V = \epsilon_0 x + \frac{\epsilon_0 t}{k} + \epsilon_0 (d - t - x)$$

$$\Delta V = \epsilon_0 \left( d - t + \frac{t}{k} \right)$$

$$\Delta V = \frac{Q_0}{\epsilon_0 A} \left( d - t \left(1 - \frac{1}{k}\right) \right)$$

$$C = \frac{\epsilon_0 A}{\left( d - t \left(1 - \frac{1}{k}\right) \right)}$$





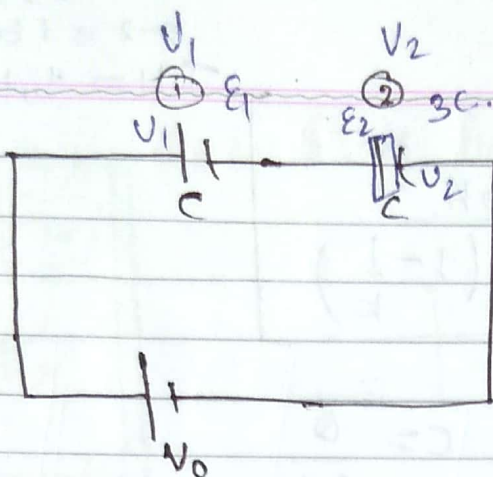
02/07/17

$\epsilon = \frac{Q}{\sigma A}$

Charge given by the battery  $\rightarrow$  final - initial

$Q = CV$   
 $V = \frac{Q}{C}$

\* Que:



$= Q = \frac{CV_0}{2}$

A dielectric slab of dielectric constant 3 is inserted in capacitor 2. find work done by the battery after dielectric is inserted.

$C_{eq} = \frac{3C}{4}$

$\frac{1}{3} = \frac{4}{3} \rightarrow \frac{3C}{4}$

~~cl~~

$Q = \frac{3CV}{4}$

~~cl~~

charge given

by battery  $\frac{3CV}{4} - \frac{CV}{2} = \frac{CV}{4}$

$\epsilon = \frac{Q}{\epsilon_0 k A}$

$W = Q \bar{E}$   
 $= \frac{CV^2}{4}$

\* (ii) find  $\frac{V_1}{V_2} = \frac{C_2}{C_1} = \frac{k}{1} = k$

$E = \frac{V}{d}$

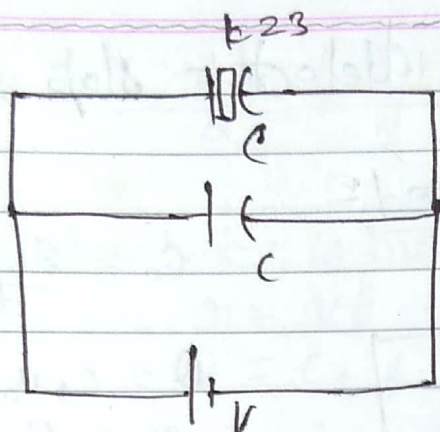
$\frac{E_1}{E_2} = \frac{3}{1}$

$V = \frac{Q_2}{C}$   $\rightarrow$  charge same on both

$\frac{V_1}{V_2} = \frac{C_2}{C_1} = \frac{3}{1}$



Ques:



$$Q = \frac{2C}{V}$$

$$\frac{1}{C} + \frac{1}{C} = \frac{2}{C} = \frac{C}{2}$$

$$C + C = 2C$$

find work done by battery after insert dielectric

$\therefore W_b =$  Charge driven by battery  $= \frac{E_0 \epsilon_0 A}{d}$

$$Q_i = 2CV$$

$$Q_f = 4CV$$

$$Q = 2CV$$

$$\text{work done} = 2CV^2$$

ii) find heat produce in the circuit when dielectric is inserted

$$W_b = 2CV^2$$

$$U_i = CV^2$$

$$U_f = \frac{1}{2} CV^2 + \frac{1}{2} 3CV^2 = 2CV^2$$

$$\Delta U = CV^2$$

$$\frac{U_1}{U_2} = 1$$

$$\frac{\epsilon_1}{\epsilon_2} = 1$$

$$C \text{ or } V = \frac{3}{1}$$

$$4C$$

$$\frac{1}{2} \times 4C \times V^2$$

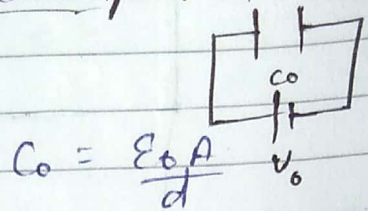
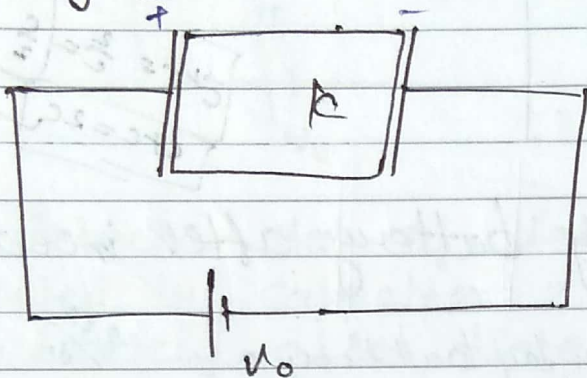
$$= 2CV^2$$



$$\epsilon_0 = 10^{-12}$$

\* Methods of Inserting dielectric slab :-

(i) Battery remains connected :-



$$C_0 = \frac{\epsilon_0 A}{d}$$

$$Q = C_0 V_0$$

$$\epsilon_0 = \frac{V_0}{d}$$

$$U_0 = \frac{1}{2} C_0 V_0^2$$

$$C = k C_0 \quad Q = k C_0 V_0 = k Q_0$$

$$W_b = (k-1) \epsilon_0 V_0^2$$

$$E = \epsilon_0 \quad U = k U_0$$

When battery remains connected potential difference b/w the plates does not change

Imp.

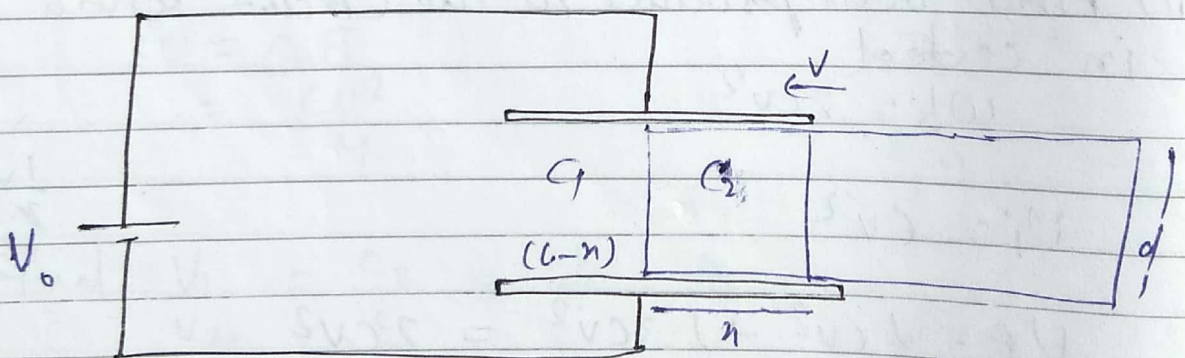


Plate =  $l \times b$

$$C_1 = \frac{\epsilon_0 (L-n) b}{d}$$

$$C_2 = \frac{\epsilon_0 k n b}{d}$$

$$C = C_1 + C_2$$

$$C = \frac{\epsilon_0 b}{d} (L-n + kn)$$



$$C_x = \frac{\epsilon_0 b}{d} (1 + (k-1)x)$$

If dielectric is inserted with fast speed  $v$ .  
 $x = vt$   
 $Q = C_x v$ .

\* Force by External Agent to insert dielectric slowly into the capacitor:

$$U = \frac{1}{2} \frac{\epsilon_0 b V_0^2}{d} (1 + (k-1)x)$$

$$F = \frac{dU}{dx} =$$

$$F = \frac{\epsilon_0 b V_0^2 (k-1)}{2d}$$

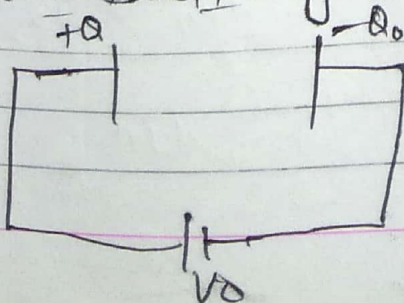
$$a = \frac{\epsilon_0 b V_0^2 (k-1)}{2md}$$

$$l = \frac{1}{2} at^2$$

$$t = \sqrt{\frac{2l}{a}}$$

$$T = 4t$$

\* 2nd Method:  
When Battery is disconnected:



$$C_0 = \frac{\epsilon_0 A}{d}$$

$$Q_0 = C_0 V_0$$

$$E = \frac{V_0}{d}$$

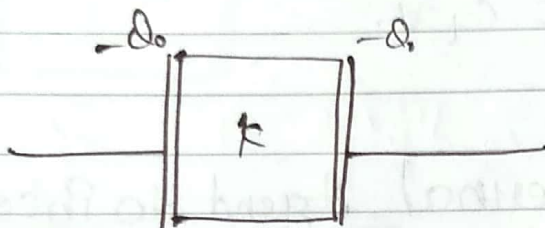


V1.0 Race  
0-1 → 16-20, 28-32, 36

B. Connected =  
Not con - Charge - const.

$$U = \frac{Q_0^2}{2C_0} = \frac{1}{2} C_0 V_0^2$$

When Battery is not connected charge on Capacitor does not change.



$$C = kC_0$$
$$Q_0 = CV$$
$$V = \frac{V_0}{k}$$

$$U = \frac{V_0}{k}$$

$$E = \frac{E_0}{k}$$

# SBG STUDY