

11/07/17

# SBG STUDY

## Thermodynamics

Part : 2

\* Heat Cycle or Heat Engine :

for any heat engine if  $q_1 =$  Heat given to engine (+ve),  $q_2 =$  heat released by engine (Negative (-))

$W =$  work done by engine (-ve).

$$|W| = |q_1| - |q_2| = q_1 + q_2$$

Efficiency

$$\eta = \frac{|W|}{|q_1|} = \frac{-W}{q_1}$$

$$= \frac{|q_1| - |q_2|}{|q_1|} = \frac{q_1 + q_2}{q_1}$$

$$\eta = 1 - \frac{|q_2|}{q_1} = 1 + \frac{q_2}{q_1}$$

\* Efficiency of a reversible engine will be greater than efficiency of irreversible engine.

$$W_{rev} > W_{irrev}$$

$$|W_{rev}| < |W_{irrev}|$$

$$\frac{|W_{rev}|}{|q_1|} < \frac{|W_{irrev}|}{|q_1|}$$

$$\eta_{rev} < \eta_{irrev}$$

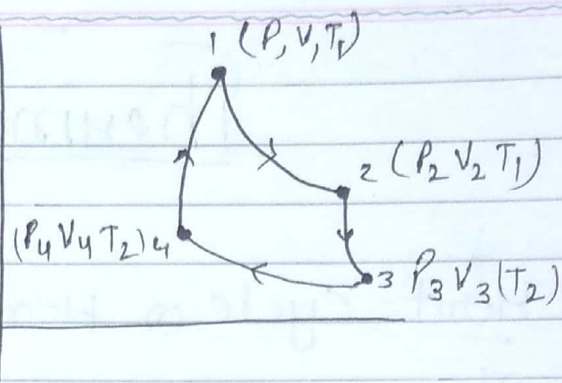
## \* Carnot Cycle:

1-2 rev. Isothermal expansion.

$$q_1 + w = 0$$

$$q_1 = -w$$

$$q_1 = +nRT_1 \ln\left(\frac{V_2}{V_1}\right) \quad \text{--- (i)}$$



2-3 rev. adiabatic expansion

$$T_1 V_2^{\gamma-1} = T_2 V_3^{\gamma-1} \quad \text{--- (ii)}$$

3-4 rev. isothermal compression

$$q_2 + w = 0$$

$$q_2 = -w$$

$$q_2 = +nRT_2 \ln\left(\frac{V_4}{V_3}\right) \quad \text{--- (iii)}$$

4-1 rev. adiabatic compression

$$T_1 V_1^{\gamma-1} = T_2 V_4^{\gamma-1} \quad \text{--- (iv)}$$

$$\eta = \frac{|w|}{|q_1|}$$

$$\eta = 1 - \frac{|nRT_2 \ln\left(\frac{V_4}{V_3}\right)|}{|nRT_1 \ln\left(\frac{V_2}{V_1}\right)|}$$

$$(ii) \div (iv) \Rightarrow \left(\frac{V_2}{V_1}\right)^{\gamma-1} = \left(\frac{V_3}{V_4}\right)^{\gamma-1} \Rightarrow \frac{V_2}{V_1} = \frac{V_3}{V_4}$$



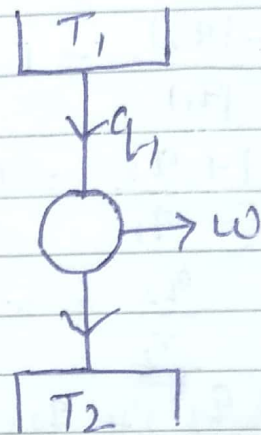
# Adiabatic ball

$$\eta = 1 - \frac{|T_2 \ln(\frac{V_2}{V_1})|}{|T_1 \ln(\frac{V_2}{V_1})|}$$

$$\eta = 1 - \frac{|T_2 \ln \frac{V_2}{V_1}|}{|T_1 \ln(\frac{V_2}{V_1})|}$$

$$\eta = 1 - \frac{|T_2|}{|T_1|}$$

$$\eta = 1 - \frac{T_2}{T_1}$$



$T_2 \Rightarrow$  Temp. of lower temp. sing  
 $T_1 \Rightarrow$  Temp. of higher temp. sing

$$\frac{|W|}{|q_1|} = \frac{|q_1| - |q_2|}{|q_1|} = 1 - \frac{|q_2|}{|q_1|}$$

$$\Rightarrow \eta_{\text{rev}} > \eta_{\text{irr}}$$

$$* \quad 1 - \frac{|q_2|}{|q_1|} = 1 - \frac{T_2}{T_1} \quad \left[ \text{for any reversible engine operating b/w } T_1 \text{ \& } T_2 \text{ temp.} \right]$$

$$1 - \frac{|q_2|}{|q_1|} < 1 - \frac{T_2}{T_1} \quad \left[ \text{for any irreversible engine operating b/w } T_1 \text{ \& } T_2 \right]$$

$$1 - \frac{|q_2|}{|q_1|} > 1 - \frac{T_2}{T_1} \quad \left[ \text{Impossible} \right]$$

\* For any reversible cycle:

$$1 - \frac{|q_2|}{|q_1|} = 1 - \frac{T_2}{T_1}$$

$$1 + \frac{q_2}{q_1} = 1 - \frac{T_2}{T_1}$$

$$\frac{q_2}{T_2} = - \frac{q_1}{T_1}$$

$$\frac{q_1}{T_1} + \frac{q_2}{T_2} = 0$$

$$\oint \frac{dq_{rev}}{T} = 0$$

$$\oint ds = 0$$

$$ds = \frac{dq_{rev}}{T}$$

$$\frac{dq_{rev}}{T} = ds$$

$$\oint \frac{dq}{T} = \frac{q_1}{T_1} + \frac{q_2}{T_2}$$

$$\Rightarrow \frac{dq_1}{T_1} + \frac{dq_2}{T_1} + \frac{q_2}{T_1} = \frac{q_1}{T_1}$$

\* As the cyclic integration of  $\frac{dq_{rev}}{T}$  is zero it

means it will definitely denote a change in a state function this state fn is called entropy

\* For any irreversible cycle:

$$1 - \frac{|q_2|}{|q_1|} < 1 - \frac{T_2}{T_1}$$

$$1 + \frac{q_2}{q_1} < 1 - \frac{T_2}{T_1}$$



$$q + w = \Delta U$$

$$\frac{q_2}{T_2} < -\frac{q_1}{T_1} \quad \text{diss}$$

$$\frac{q_1}{T_1} + \frac{q_2}{T_2} < 0$$

$$\oint \frac{dq_{\text{irr}}}{T} < 0$$

~~Cl~~ Cyclic integration of  $\frac{dq_{\text{irr}}}{T}$  is not

equal to zero it means it will not denote change in any state.

\* Clausius Inequality:-

$$\left\{ ds = \frac{dq_{\text{rev}}}{T} \right\}$$

$$dq_{\text{irr}} < dq_{\text{rev}}$$

$$\frac{dq_{\text{irr}}}{T} < \frac{dq_{\text{rev}}}{T}$$

$$ds > \frac{dq_{\text{irr}}}{T}$$

$$ds = \frac{dq_{\text{rev}}}{T}$$

$$ds \geq \frac{dq}{T}$$

→ Clausius inequality.



Start.

Imp. Points

\* Clausius inequality for an isolated system:

$$(dq = 0)$$

$$\left. \begin{array}{l} ds \geq 0 \\ ds > 0 \end{array} \right\} \begin{array}{l} \text{Possible irreversible process} \\ \text{or spontaneous process} \end{array}$$

$$ds = 0 \quad \text{[reversible process]}$$

$$ds < 0 \quad \left\{ \begin{array}{l} \text{impossible process or non-spontaneous} \\ \text{process} \end{array} \right\}$$

Imp.

$\Rightarrow$  Entropy of an isolated system can never decrease during a process in isolated system.

$\Rightarrow$  Entropy will be maximum at eqb. in a isolated system.

$\Rightarrow$  Universe is an ideal example of isolated system. So all the results of isolated system can be applied for universe.

\* Second law of Thermodynamics:  
Statement given by Clausius:

Total Entropy of a universe during a process can never decrease either it will increase in a spontaneous or remain constant in a reversible process.



$$dq = 0$$

$$\Delta S_{\text{univ}} \geq 0$$

$$\Delta S_{\text{system}} + \Delta S_{\text{surr}} > 0 \left[ \begin{array}{l} \text{Process (irreversible Process)} \\ \text{or Spontaneous process} \end{array} \right]$$

$$\Delta S_{\text{system}} + \Delta S_{\text{surr}} = 0 \left[ \text{reversible process or at Equilibrium} \right]$$

$$\Delta S_{\text{system}} + \Delta S_{\text{surr}} < 0 \left[ \begin{array}{l} \text{Impossible process or non-} \\ \text{Spontaneous process} \end{array} \right]$$

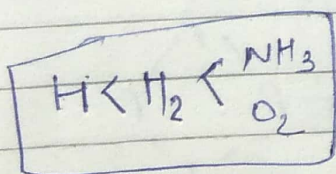
Although individual value of Entropy of system or Entropy of Surrounding can decrease.

\* Entropy  $^{\circ} (S)$  :

Entropy is a measurement of dispersion of energy, Unuseful energy or Randomness of particles of the system.

Important Point:-

gaseous molecules which have higher value of atomicity will have value of entropy as



$$S_{NH_3} > S_{H_2}$$

$$S_H < S_{H_2}$$

$$S_{H_2} < S_{O_2}$$

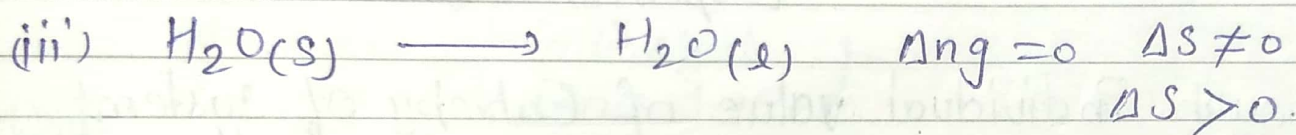
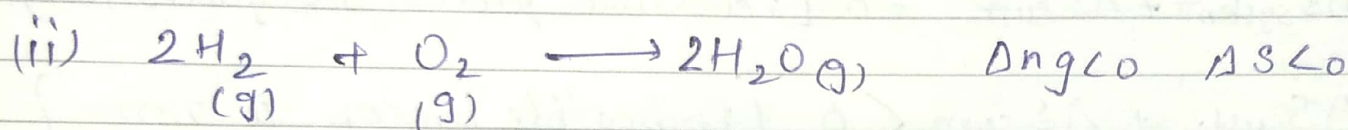
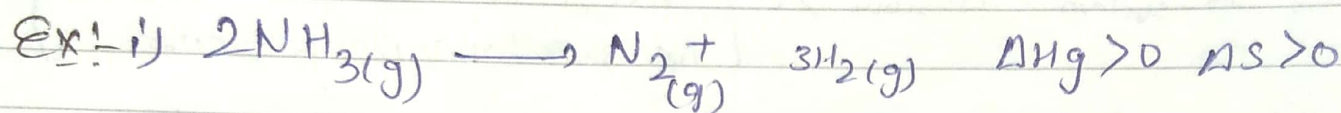
2) If atomicity are equal we will compare by size of molecules

$$\text{Size} \uparrow \quad S \uparrow$$



3] Entropy of gas  $\gg$  Entropy of liquid  $\gg$  Entropy of solid

$$S_{\text{gas}} \gg S_{\text{liquid}} \gg S_{\text{solid}}$$

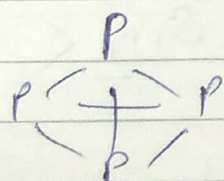


4] On mixing of two gases or two liquids or two solids Entropy will increase.

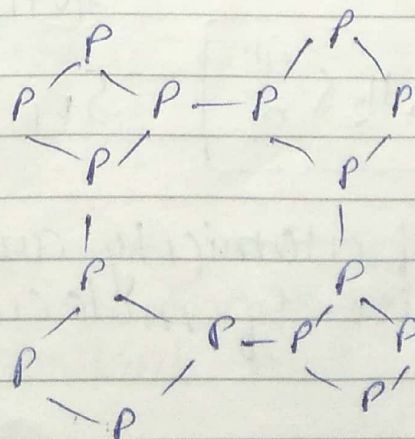
5] Allotropic form of a substance which have better arrangement of particles ~~which~~ have lower value of Entropy.

$$S_{\text{C(diamond)}} < S_{\text{C(graphite)}}$$

$$S_{\text{P(white)}} > S_{\text{P(red)}}$$



white



red



$$C_m = \frac{c}{m}$$

$$H - W \neq J - A$$

Ques: In which of the following options Entropy will decrease.

- 1) during precipitation process  $\downarrow$
- 2) during stretching of Rubber.  $\uparrow \downarrow$
- 3) Boiling of Egg.  $\uparrow$
- 4) Absorption of a gas on a solid  $\downarrow$  due to denaturation of Protein.
- 5) Dissolution of a solid in a liquid.  $\uparrow$

\* Calculation of entropy change:

\* for non reacting substances:

(i) If molar heat capacity of process is provided:

$$ds = \frac{dq_{rev}}{T}$$

$$\Delta S = \int_{T_1}^{T_2} \frac{dq_{rev}}{T}$$

$$\Delta S = \int_{T_1}^{T_2} \frac{m c_m dT}{T}$$

(ii) If  $C_m$  is constant:

$$\Delta S = m c_m \ln \left( \frac{T_2}{T_1} \right)$$

$$\Delta S = c \ln (T_2/T_1)$$

\* for non reacting ideal gas:

$$dq + w = du$$

$$dq - PdV = n c_m dT$$



$$\frac{dq}{T} - \frac{pdv}{T} = n c_{vm} \frac{dT}{T}$$

$$ds = \frac{pdv}{T} + n c_{vm} \frac{dT}{T}$$

$$\Delta S = \int_{v_1}^{v_2} \frac{nR}{v} dv + \int_{T_1}^{T_2} \frac{n c_{vm} dT}{T}$$

Learn

$$\Delta S = nR \ln \left( \frac{v_2}{v_1} \right) + n c_{vm} \ln \left( \frac{T_2}{T_1} \right)$$

If  $c_{vm}$  is const.

$$\Delta S = nR \ln \frac{\frac{nRT_2}{P_2}}{\frac{nRT_1}{P_1}} + n c_{vm} \ln \left( \frac{T_2}{T_1} \right)$$

$$\Delta S = nR \ln \left( \frac{P_1}{P_2} \right) \left( \frac{T_2}{T_1} \right) + n c_{vm} \ln \left( \frac{T_2}{T_1} \right)$$

$$\Delta S = nR \ln \left( \frac{P_1}{P_2} \right) + nR \ln \left( \frac{T_2}{T_1} \right) + n c_{vm} \ln \left( \frac{T_2}{T_1} \right)$$

$$\Delta S = nR \ln \left( \frac{P_1}{P_2} \right) + n (c_{vm} + R) \ln \left( \frac{T_2}{T_1} \right)$$

Learn

$$\Delta S = nR \ln \left( \frac{P_1}{P_2} \right) + n c_{pm} \ln \left( \frac{T_2}{T_1} \right)$$

Always Add

$$\Delta S = nR \ln \left( \frac{v_2}{v_1} \right) + n c_{vm} \ln \left( \frac{T_2}{T_1} \right)$$

Valid for non reacting ideal gas in every process



$$Pv = nRT$$

$\downarrow$   
 $\leftarrow$

(0.0821)

$V \uparrow$	$S \uparrow$
$P \uparrow$	$S \downarrow$
$T \uparrow$	$S \uparrow$
$n \uparrow$	$S \uparrow$

Ques: molar heat capacity for an ideal gas in a isochoric process is  $C_{vm} = (1 + 0.17) \text{ Joule/mol} \cdot \text{K}$ .  
 If isochorically this gas heated from  $27^\circ\text{C}$  to  $127^\circ\text{C}$  then calculate change in molar Entropy for this ideal gas.

$$\Delta S = \int_{T_1}^{T_2} \frac{dq}{T} = \int_{300}^{400} \frac{n C_{vm} dT}{T} = \int_{300}^{400} \frac{(1 + 0.17) dT}{T}$$

Ques: A gas is taken from 2 atm to 30 litre to (4 atm, 90 litre) by a certain process then calculate change in molar Entropy,  $\Delta S$  of gas. Suppose gas is a diatomic ideal gas.

$$C_{vm} = \frac{5}{2} R$$

$$\Delta S = nR \ln\left(\frac{V_2}{V_1}\right) + n C_{vm} \ln\left(\frac{T_2}{T_1}\right)$$

$$\Delta S = (1)R \ln\left(\frac{90}{30}\right) + (1) \left[\frac{5}{2} R\right] \ln\left(\frac{P_2 V_2}{P_1 V_1}\right) \quad P_1 V_1 = P_2 V_2$$



## \* Entropy Change for Surrounding:

1. If process is a reversible process in the system

$$\Delta S_{\text{system}} + \Delta S_{\text{surr}} = 0$$

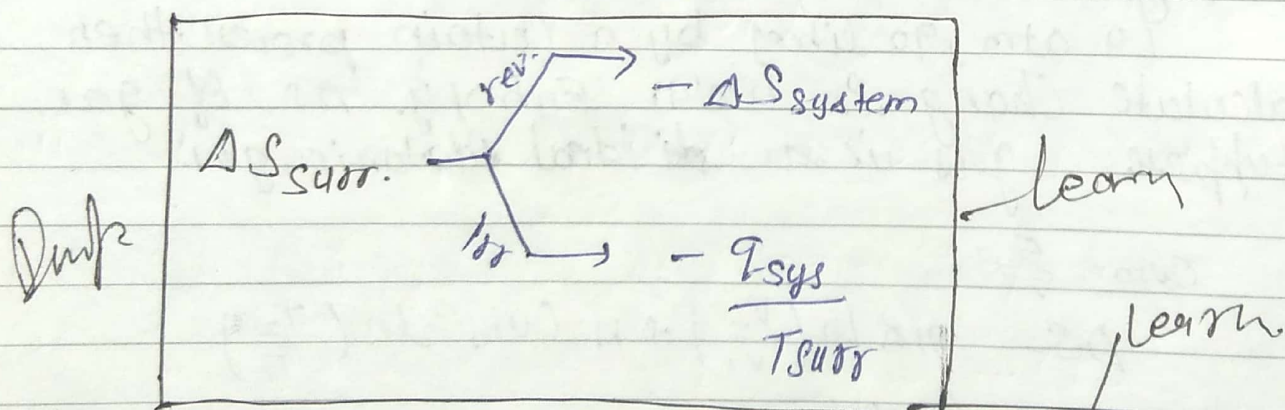
$$\Delta S_{\text{surr}} = -\Delta S_{\text{system}} \quad \text{Learn.}$$

2) If process is irreversible process in the system.

$$\Delta S_{\text{system}} + \Delta S_{\text{surr}} > 0$$

$$\Delta S_{\text{surr}} = \int \frac{dq_{\text{surr}}}{T_{\text{surr}}} = \int \frac{dq_{\text{surr}}}{T_{\text{surr}}} = \frac{q_{\text{surr}}}{T_{\text{surr}}}$$

$$\Delta S_{\text{surr}} = \frac{-q_{\text{sys}}}{T_{\text{surr}}}$$



Ques

$$\Delta S_{\text{sys}} = nR \ln \left( \frac{V_2}{V_1} \right) + nC_{\text{vm}} \ln \left( \frac{T_2}{T_1} \right)$$

$$\Delta S_{\text{sys}} = nR \ln \left( \frac{P_1}{P_2} \right) + nC_{\text{pm}} \ln \left( \frac{T_2}{T_1} \right)$$



Isobaric

$$P \text{ bar } q = \Delta H = n C_p \Delta T$$

$$q = \Delta U - W$$

\* Calculation of  $\Delta S_{\text{system}}$ ,  $\Delta S_{\text{surr}}$  and  $\Delta S_{\text{universe}}$  for different process:

(i) In Isochoric Process:

(ii)  $\Delta S_{\text{sys}}$  for molar isochoric process:

$$\Delta S_{\text{sys}} = n C_{vm} \ln \left( \frac{T_2}{T_1} \right)$$

(ii)  $\Delta S_{\text{surr}}$  if process is rev. process =  $-\Delta S_{\text{sys}}$ .

(iii)  $\Delta S_{\text{surr}}$  if process is irrev. process =

$$\Delta S_{\text{surr}} = \frac{-q_{\text{sys}}}{T_{\text{surr}}} = - \frac{(\Delta U - W)}{T_{\text{surr}}}$$

$$\Delta S_{\text{surr}} = - \frac{n C_{vm} \cdot (T_2 - T_1)}{T_{\text{surr}}}$$

\*  $T_{\text{surr}} = T_2$  if value of  $T_{\text{surr}}$  not given in question.

\* In Isobaric process:

(i)  $\Delta S_{\text{sys}}$  for molar isobaric process:

$$\Delta S_{\text{sys}} = n C_{pm} \ln \left( \frac{T_2}{T_1} \right)$$

(ii)  $\Delta S_{\text{surr}}$  if process is rev. process =  $-\Delta S_{\text{sys}}$ .

(iii)  $\Delta S_{\text{surr}}$  if process is irrev. process =



$$P_{\text{isotherm}} = W = -P_{\text{ext}} (V_2 - V_1)$$

$$\Delta S_{\text{surr}} = \frac{-q_{\text{sys}}}{T_{\text{surr}}} = \frac{-(\Delta U - W)}{T_{\text{surr}}}$$

$$= \frac{-(nC_{\text{vm}} \Delta T + nR \Delta T)}{T_{\text{surr}}}$$

$$= \frac{-n(C_{\text{vm}} + R) \Delta T}{T_{\text{surr}}}$$

$$= \frac{-nC_{\text{pm}} (T_2 - T_1)}{T_{\text{surr}}}$$



\* In isothermal process:

(i)  $\Delta S_{\text{sys}}$  for reversible process?

$$\Delta S_{\text{sys}} = nR \ln \left( \frac{V_2}{V_1} \right) = nR \ln \left( \frac{P_1}{P_2} \right)$$

(ii)  $\Delta S_{\text{surr}}$  if process is reversible process =  $-\Delta S_{\text{sys}}$

(iii)  $\Delta S_{\text{surr}}$  if process is irreversible process =

$$\Delta S_{\text{surr}} = \frac{-q_{\text{sys}}}{T_{\text{surr}}} = \frac{-(\Delta U - W_{\text{irr}})}{T_{\text{surr}}}$$

$$\Delta S_{\text{surr}} = \frac{W_{\text{irr}}}{T_{\text{surr}}}$$

$$\Delta S_{\text{surr}} = \frac{-P_{\text{ext}} (V_2 - V_1)}{T_{\text{surr}}}$$



$$S_{\text{surr}} = -P_{\text{ext}} \left( \frac{nRT}{P_2} - \frac{nRT}{P_1} \right)$$

$$T_{\text{surr}}$$

$$T_{\text{surr}} = T_2 = T$$

\* ~~In ~~the~~ ~~reversible~~ ~~process~~!~~

\* In ~~the~~ Adiabatic Process

$$\Delta S = nC_{V,m} \ln \left( \frac{T_2}{T_1} \right) + nR \ln \left( \frac{V_2}{V_1} \right)$$

$$\Delta S = nC_{p,m} \ln \left( \frac{T_2}{T_1} \right) + nR \ln \left( \frac{P_1}{P_2} \right)$$

These formulas are also applicable for adiabatic process if we solve for reversible adiabatic process then

$$\Delta S_{\text{sys}} = 0.$$

If we solve for irreversible adiabatic process then

$$\Delta S_{\text{sys}} > 0$$

Proof!  $\Delta S = nC_{V,m} \left[ \ln \left( \frac{T_2}{T_1} \right) + \left( \frac{R}{C_{V,m}} \right) \ln \left( \frac{V_2}{V_1} \right) \right]$

$$\Delta S = nC_{V,m} \left[ \ln \left( \frac{T_2}{T_1} \right) + \ln \left( \frac{V_2}{V_1} \right)^{\frac{R}{C_{V,m}}} \right]$$

$$\Delta S = nC_{V,m} \left[ \ln \frac{T_2 V_2^{\frac{R}{C_{V,m}}}}{T_1 V_1^{\frac{R}{C_{V,m}}}} \right]$$



(vi)  $\Delta S_{\text{surr}}$  If process is rev process  $= -\Delta S_{\text{sys}} = 0$

(iii)  $\Delta S_{\text{surr}}$  if process is irr process =

$$\Delta S_{\text{surr}} = -\frac{q_{\text{sys}}}{T_{\text{surr}}} = 0$$

### \* Free Expansion of Ideal gas :

Free Expansion of Ideal gas is a irr. adiabatic and irr. isothermal process simultaneously.

$$\Delta S_{\text{sys}} = nR \ln\left(\frac{V_2}{V_1}\right) + nC_{\text{vm}} \ln\left(\frac{T_2}{T_1}\right) = 0$$

In free expansion

$$\Delta S_{\text{sys}} > 0$$

$$\Delta S_{\text{surr}} = -\frac{q_{\text{sys}}}{T_{\text{surr}}} = 0$$

$$\Delta S_{\text{surr}} = 0$$

### \* For Cyclic Process In System :

(i) For rev/ irr cyclic process!  
 $\Delta S_{\text{sys}} = 0$



611 Pascal

T.D-2 0-1 = 1 to 10

T.D-1 J-II = 1 to 5

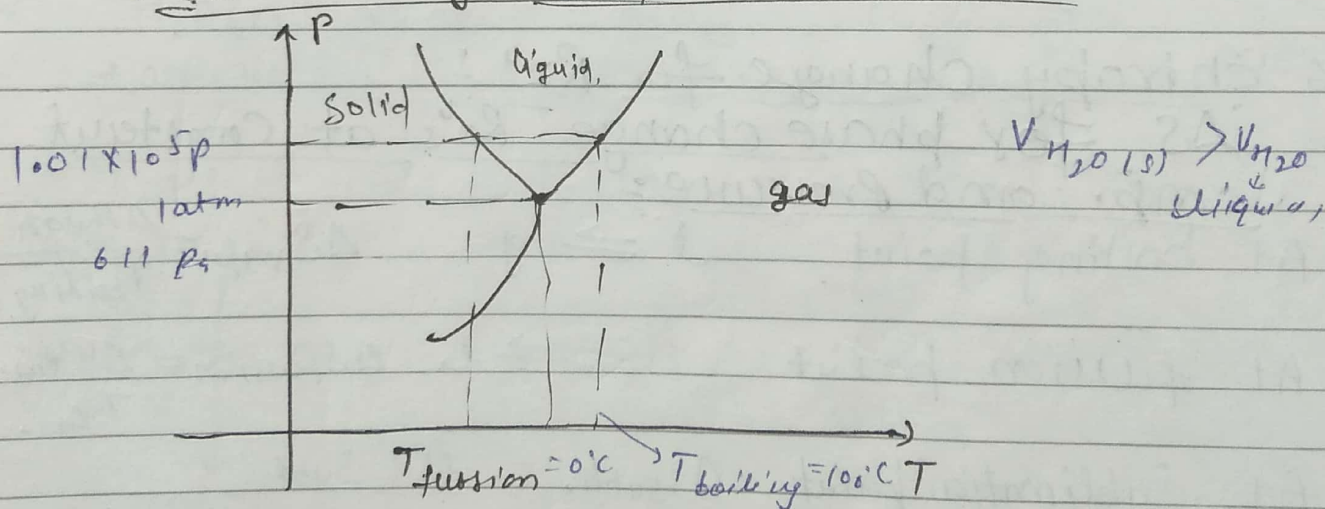
(ii)  $\Delta S_{\text{surr}}$  if process is rev process =  $-\Delta S_{\text{sys}} = 0$

(iii)  $\Delta S_{\text{surr}}$  if process is irr. process:

$$\Delta S_{\text{surr}} = \frac{-q_{\text{sys}}}{T_{\text{surr}}} = -\frac{(\Delta U - w)}{T_{\text{surr}}} = \frac{w_{\text{irr}}}{T_{\text{surr}}}$$

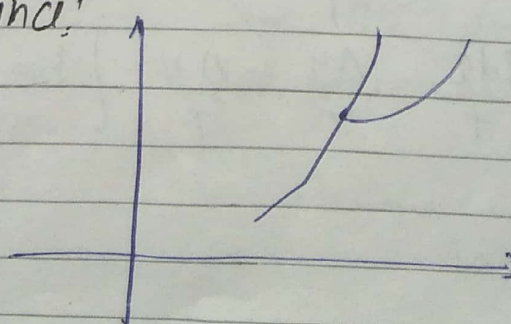
\* If system restored to its initial position in a cyclic process then it is not compulsory that surrounding will also restored to its initial position.

\* Phase diagram for water



Phase diagram for  $\text{H}_2\text{O}$

for a general substance:



$V(\text{Solid}) < V(\text{Liq})$



\* At Boiling point liquid will be in eq with gas/vapour.

\* Boiling point at 1 atm pressure called normal boiling point.

\* Boiling point at 1 bar pressure called standard boiling point.

\* At fusion point solid will be in eq with liquid.

for general <sup>substance</sup> solid ~~point~~  $T_{\text{fusion}} \uparrow$   $P \uparrow$

for  $H_2O$  substance ~~for~~  $T_{\text{fusion}} \uparrow$   $P \uparrow$

\* Entropy change for  $Rx^n$  :

(1)  $\Delta S$  for phase change  $Rx^n$ s at constant temp. and pressure :

\* At boiling point  $l \rightleftharpoons g$ .  $\Delta S_{\text{vap}} = \frac{\Delta H_{\text{vap}}}{T_{\text{boiling point}}}$

\* At fusion point  $s \rightleftharpoons l$ .  $\Delta S_{\text{fusion}} = \frac{\Delta H_{\text{fus.}}}{T_{\text{fus.}}}$

\* At Sublimation point  $\Delta S_{\text{subli.}} = \frac{\Delta H_{\text{Subli.}}}{T_{\text{sub.}}}$

$s \rightleftharpoons g$ .

$$\Delta S = \int \frac{dq}{T}$$

\*  $\Delta S = \int \frac{dq}{dT} = \frac{dq}{T} = \frac{\Delta q}{T} = \frac{\Delta H}{T}$  [because pressure  $\approx P_s$  constant]



1526

Comm

# Counseling

1526  
2011

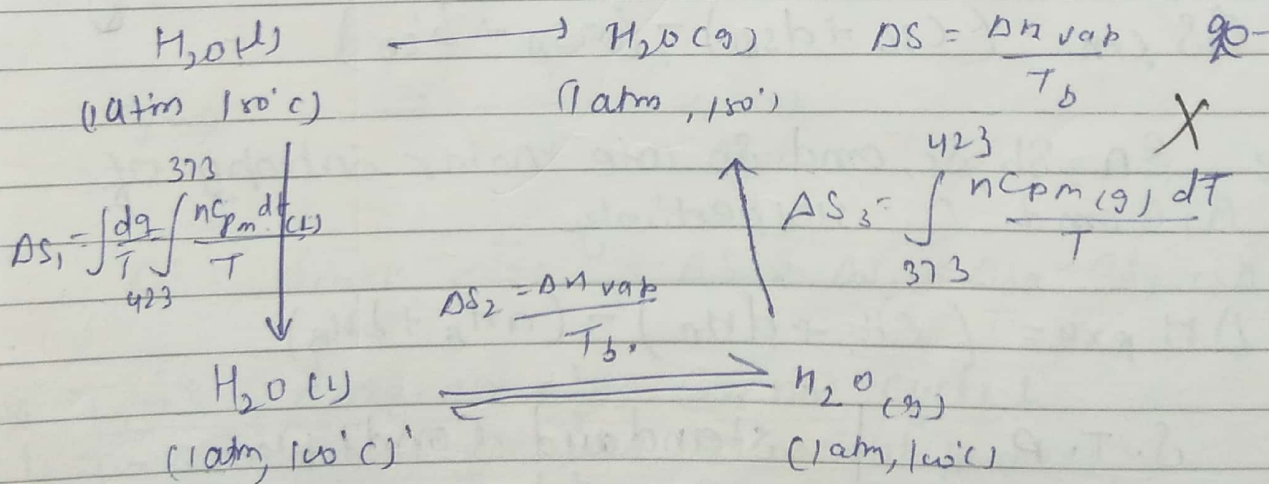
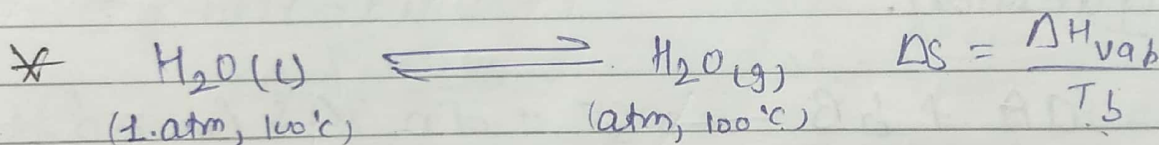
Ques: Enthalpy of vaporisation for H<sub>2</sub>O liquid is 40 kcal per gram. if condensation of 1 mol. H<sub>2</sub>O vapour occurs at 100°C and 1 atm pressure then calculate value of ΔS condensation for 1 mol of H<sub>2</sub>O.

Ans:

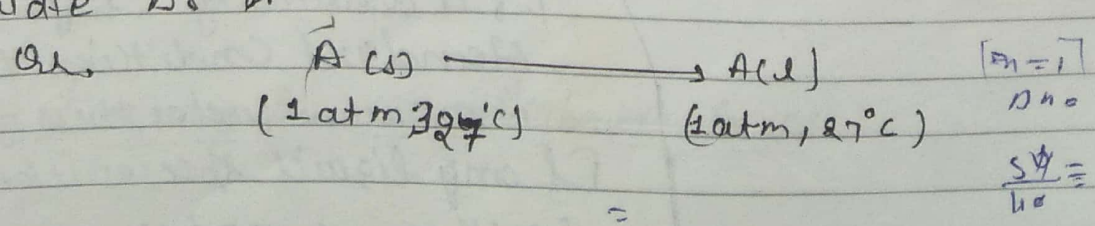
$$\Delta S_{\text{vap}} = \frac{\Delta H_{\text{vap}}}{T_{\text{boiling point}}}$$

$$\Delta S_{\text{vap}} = \frac{40 \times 18}{373}$$

$$\Delta S_{\text{condensation}} = - \frac{40 \times 18}{373}$$

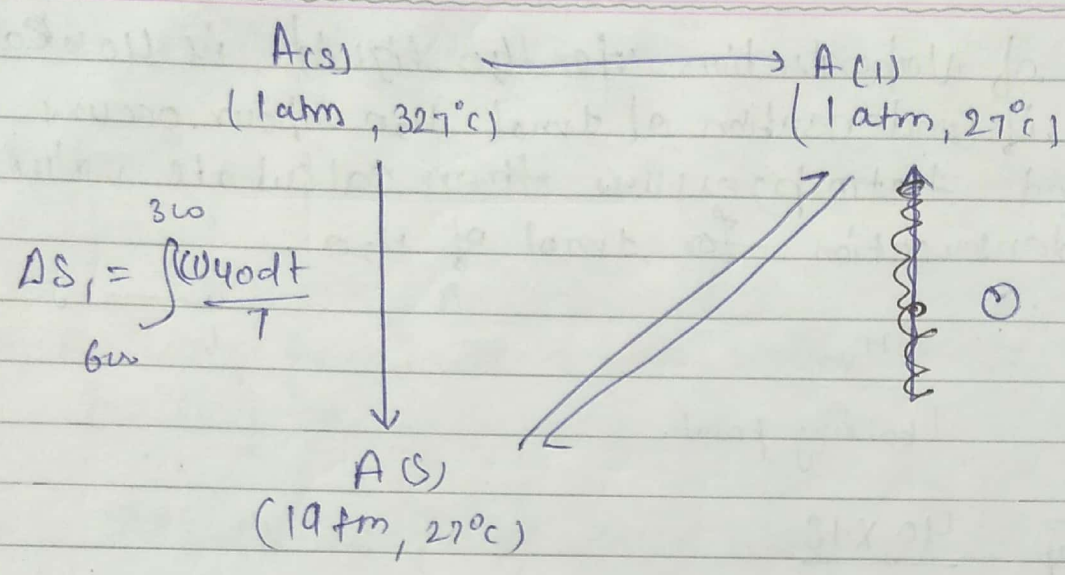


Ques: For a solid C<sub>p,m</sub> 40 J/mol. ΔH fusion = 50 kJ/mol. n = 1 mol, Normal fusion = 27°C. then calculate ΔS

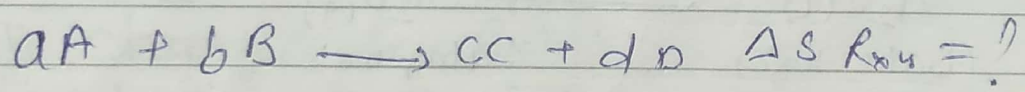




5/10/23



(2) If exact value of Molar Entropy of different reactant or product given in the question.



$$\Delta S_{rxn} = (cS_C + dS_D) - (aS_A + bS_B)$$

Here  $S_A, S_B, S_C,$  and  $S_D$  are molar Entropy of A, B, C and D respectively.

$$\Delta H_{rxn} = (cH_C + dH_D) - (aH_A + bH_B)$$

S. T. P  
 P = 1 bar  
 T = 273

standard Condition  
 P = 1 bar  
 T = any definite Temp.

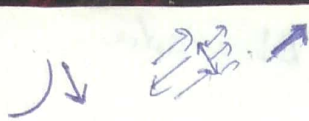
If a quantity is given under standard condition then this is measure under these given condition.

If any liquid species is present then  $C_{molar} = 1 \text{ molar}$

Ex:  $S^\circ, H^\circ, \Delta S^\circ, \Delta G^\circ$



$$dz = -w$$



T.O = Part 1 (1st) 0-2

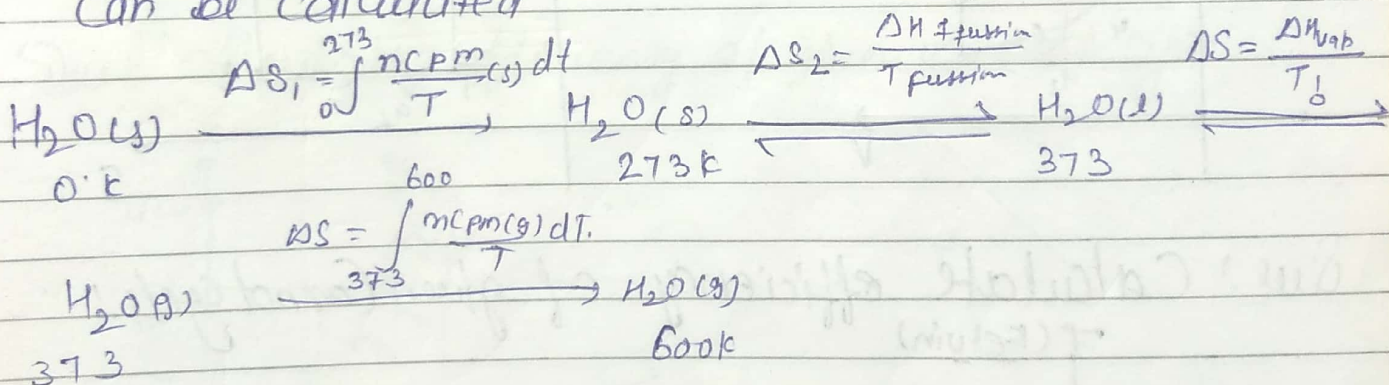
↑ 50  
101

## \* Third Law of Thermodynamics!

At 0 K temp Entropy of a perfectly crystalline solid will be minimum and this minimum value can be assumed to equal to zero

$$S_{0 \text{ Kelvin}} = 0$$

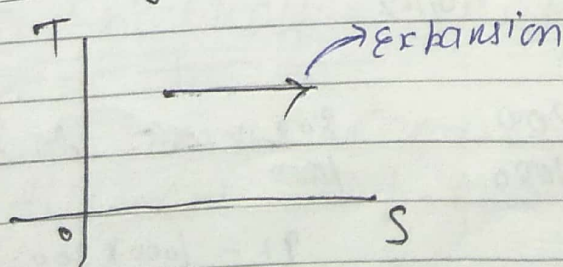
with the help of Third Law of Thermodynamics ~~exact~~ exact value of entropy of a substance can be calculated



$$\Delta S = S_{600 \text{ K}} - S_{0 \text{ K}} = \Delta S_1 + \Delta S_2 + \Delta S_3 + \Delta S_4 + \Delta S_5$$

\* T-s diagram for Carnot cycle!

(i) T-s diagram for rev. isothermal process?

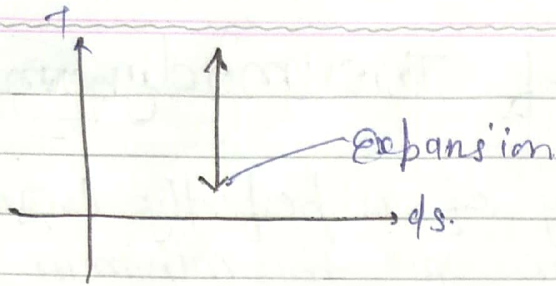


(ii) T-s diagram for rev. adiabatic process?



NVIM

$\omega^T = 0$        $Bb = ada.$



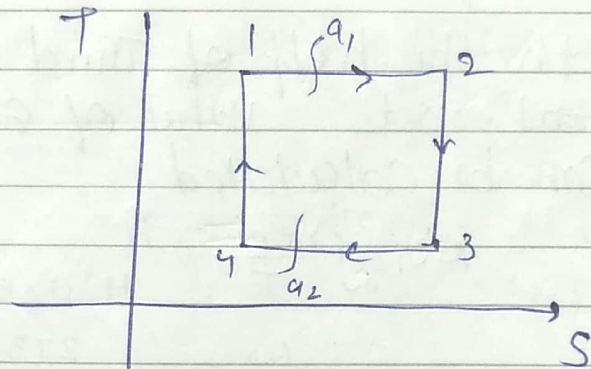
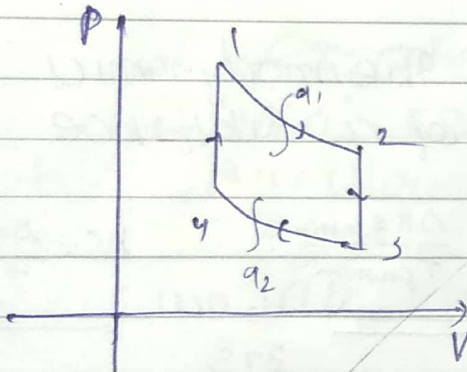
$$= \int y dx$$

$$= \int T ds$$

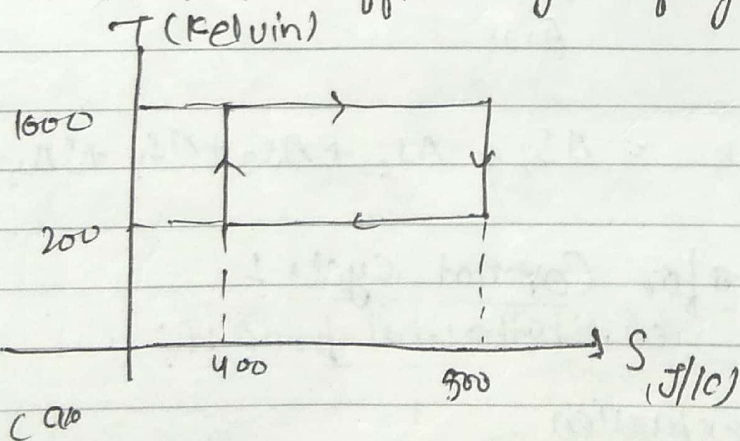
$$= \int dQ$$

\* If rev. adiabatic process entropy of system remain constant so it is also called isentropic process

\* Area Under T-s curve denote magnitude of heat change in the process



Ques: Calculate efficiency of given Carnot cycle:



M.1.  $\eta = 1 - \frac{T_2}{T_1} = 1 - \frac{200}{1600} = \frac{800}{1600} \times 100 = 50\%$

$$q_1 = 1000 \times 200 =$$

M.2  $\eta = \frac{|w|}{|q_1|} = \frac{|q_1| - |q_2|}{|q_1|}$



~~Topic~~  
~~Not Very~~  
~~Important~~

Habron - release

Ques: Calculate work done by engine per cycle

$$|Q_1| = 100000 \text{ Joule.}$$

$$|Q_2| = 20000 \text{ Joule}$$

$$|W| = |Q_1| - |Q_2| = 80000 \text{ J.}$$

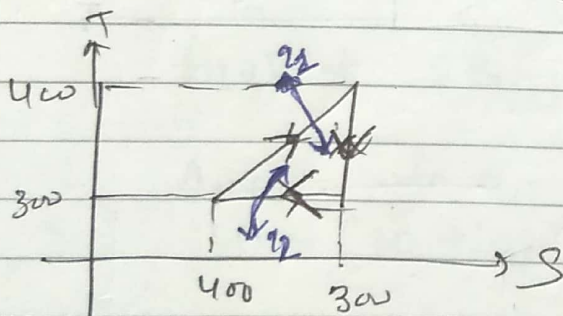
(iii) If be eliminate 10000 bulb each of 40 watt capacity by given Carnote engine then calculate no. of cycle that are required to eliminate these bulb.

~~40000~~  
~~20000~~  
 = 5 no

$$40 \times 10000 = 80000 \times n$$

$$n = 5 \text{ cycle}$$

Ques: Calculate efficiency of given ~~Carnot~~ cycle



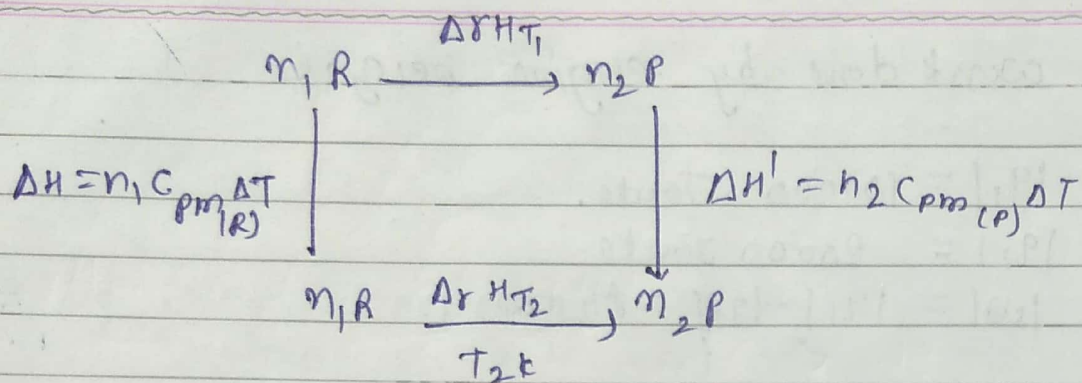
$$|Q_2| = 100 \times 300$$

$$|Q_1| = \frac{1}{2} (700) (100)$$

\* @ Knichhoff's equation,

Let a  $rx^4$  occurs Const. Pressure and two different temp.  $t_1$  and  $t_2$





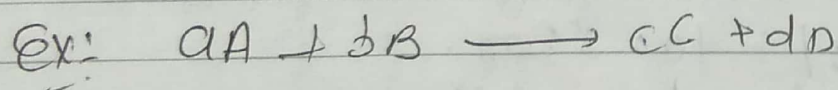
$$\Delta_r H_{T_2} + n_1 C_{pm(R)} \Delta T = \Delta_r H_{T_1} + n_2 C_{pm(P)} \Delta T$$

$$\Delta_r H_{T_2} - \Delta_r H_{T_1} = n_2 C_{pm(P)} \Delta T - n_1 C_{pm(R)} \Delta T$$

$$\Delta_r H_{T_2} - \Delta_r H_{T_1} = [n_2 C_{pm(P)} - n_1 C_{pm(R)}] \Delta T$$

$$\Delta_r H_{T_2} - \Delta_r H_{T_1} = \Delta_r C_p \Delta T \Rightarrow \Delta_r H_{T_2} - \Delta_r H_{T_1} = \int_{T_1}^{T_2} \Delta_r C_p dT$$

m



$$\Delta_r C_p = (c C_{pm(C)} + d C_{pm(D)}) - (a C_{pm(A)} + b C_{pm(B)})$$

\* for internal energy change at different temp.  $T_1$  and  $T_2$

$$\Delta_r U_{T_2} - \Delta_r U_{T_1} = \Delta_r C_v (\Delta T)$$

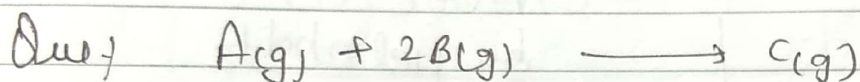


Note: for a rxn if  $\Delta_r C_p = 0$  then  $\Delta_r H$  will be independent from temp

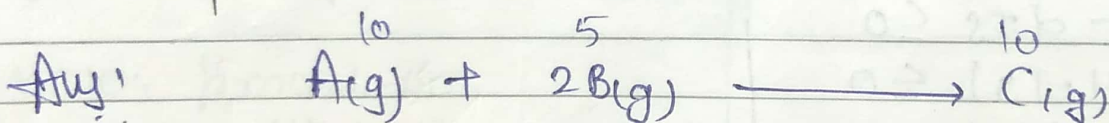
$\Delta_r C_p$

then  $\Delta_r H$

$$\frac{d(\Delta_r H)}{dT} = 0$$



Enthalpy change for rxn at 27°C is -10 kJ then calculate enthalpy change for rxn at 127°C. if molar heat capacity at constant pressure for a, b, and c are in ratio of 1:0.5:1 and  $C_p$  for A gas is 10 J/mol.k.



$$\Delta_r C_p = -10 \text{ J}$$

$$10 - (10 + 10) = -10 \text{ J/mol.k}$$

$$27^\circ\text{C} = 300 \text{ K}$$

$$\Delta_r C_p' = -10 \text{ J/mol.k}$$

$$\Delta_r H_{400} - \Delta_r H_{300} = \Delta_r C_p (T_2 - T_1)$$

$$\Delta_r H_{400} - (-10000) = -10(400 - 300)$$

$$\Delta_r H_{400} = -11000 \text{ Joule}$$

Q: Inorganic  $C_p$  for A gas is  $(1 + 0.02T)$  J/mol.k. then calculate  $\Delta_r H$  at 127°C



## \* Gibbs free Energy †

$$ds \geq \frac{dq}{T}$$

by Gibbs

$$P=C, T=C$$

$$dq = dH$$

$$ds \geq \frac{dH}{T}$$

$$T ds \geq dH$$

$$dH - T ds \leq 0$$

$$dH - dTS \leq 0$$

$$d(H - TS) \leq 0$$

$$dG \leq 0$$

by Helmholtz

$$V=C, T=C$$

$$dq = dU$$

$$d(U - TS) \leq 0$$

$$dA \leq 0$$

↳ Helmholtz energy

## \* Gibbs free energy: (G) =

$$G = H - TS$$

at constant temp. & Pressure

$$\Delta G = \Delta H - T \Delta S$$

## \* Relation b/w $\Delta G$ and $\Delta S_{universe}$ ∴

at  $P=C$  &  $T=C$

$$\Delta S_{universe} = \Delta S_{system} + \Delta S_{surr}$$



Therm: Part-1: S-2 + 6 to 11 + S-7: 23-24

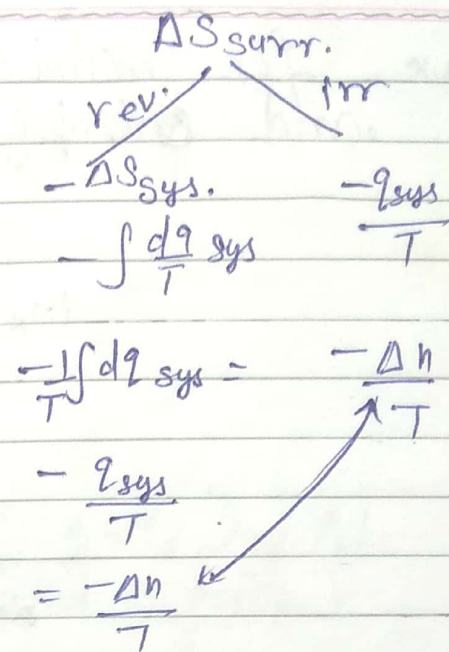
Part 2. 1 to 6. S-1  
9 to 11

$$\Delta S_{\text{universe}} = \Delta S_{\text{sys.}} - \frac{\Delta H}{T}$$

$$T \Delta S_{\text{univ.}} = T \Delta S_{\text{sys.}} - \Delta H.$$

$$-T \Delta S_{\text{univ.}} = \Delta H - T \Delta S_{\text{sys.}}$$

$$\boxed{-T \Delta S_{\text{universe}} = \Delta G}$$



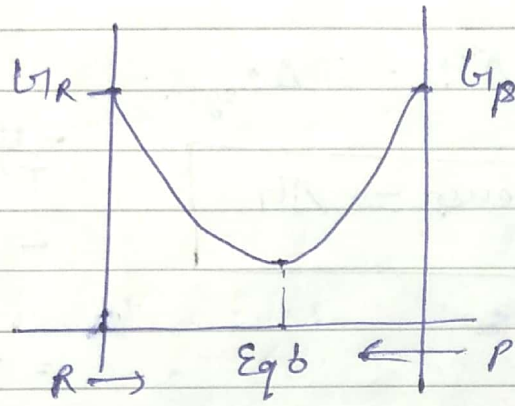
$\Delta S_{\text{univ.}}$		$\Delta G$
Spontaneous process	$> 0$	$< 0$
revers. process or at Equilibrium	$= 0$	$= 0$
non-spontaneous process	$< 0$	$> 0$

\* Spontaneity criteria can be defined by  $\Delta S_{\text{univ.}}$  in every condition but spontaneity criteria can be defined by  $\Delta G$  only at const. P & const. Temp

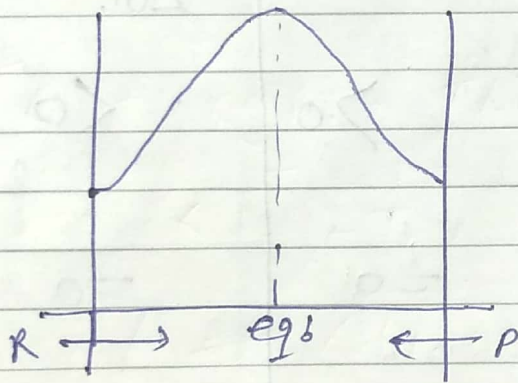
During a process gibbs free energy (G) will be minimum at eqb. and  $\Delta S_{\text{univ.}}$  will be maximum at eqb.



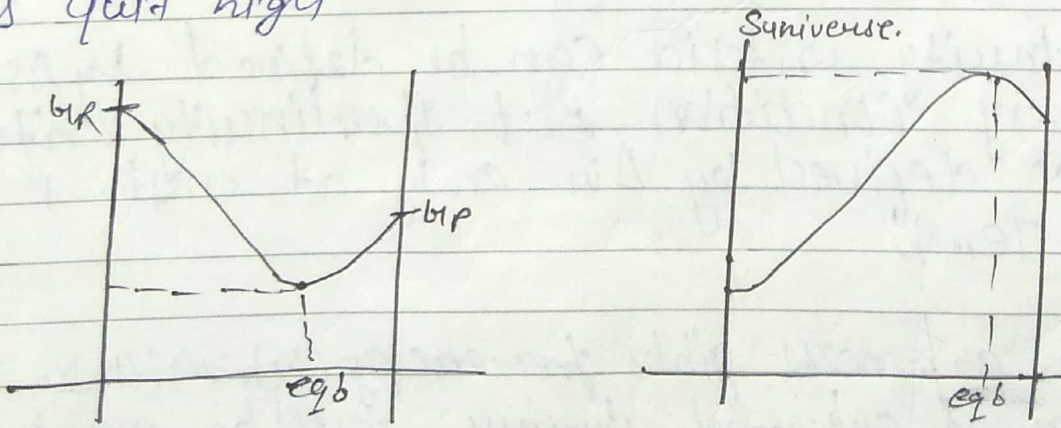
32x for chemical eqb  $Rx^y$  graph of gibbs energy and entropy of universe can be plotted as



$\Phi$  universe:



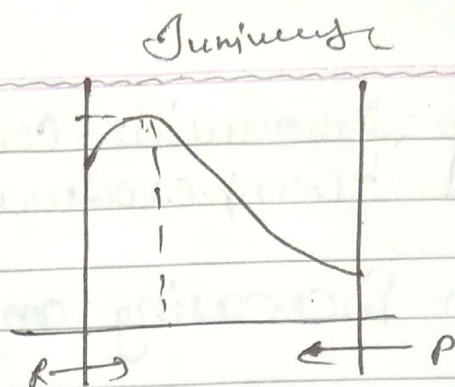
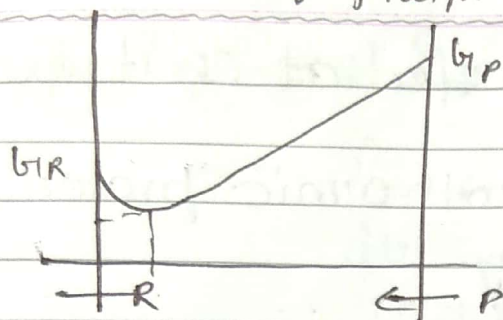
for a chemical eqb  $Rx^y$  if value of  $eqb$  const is quite high





Spontaneous! Possible.

for eq const.  $e^{\Delta G}$  high.



$$K_{eq} = \frac{[P] \downarrow}{[R] \uparrow}$$

\* Analysis of Spontaneity of Rxns by  $\Delta G$ .  
Occurs at Const. Pressure and Temp? -

$$\Delta G = \Delta H - T\Delta S$$

$\Delta H$	$\Delta S$	$\Delta G$	
-ve	+ve	-ve	always spontaneous.
+ve	-ve	+ve	always non-spontaneous.
+ve	+ve	$T \uparrow, -ve$	spontaneous at high temp
		$T \downarrow, +ve$	nonspontaneous at low temp
-ve	-ve	$T \uparrow, +ve$	
		$T \downarrow, -ve$	spontaneous at low temp.



\* Most favourable condition for at const Pressure and temperature is exothermic process with increasing entropy.



$\Delta S = 1000 \text{ cal/mol} \cdot K$

$\Delta U = 99.8 \text{ kcal/mol}$

\* Calculate the temp above which reaction will be spontaneous

$\Delta G < 0$

$\Delta G = \Delta H - T\Delta S$

$\Delta H = \Delta U + \Delta n_g RT$   
 $\Delta H = 99.8 \text{ kcal/mol}$

$\Delta G =$

$\Delta U + \Delta n_g RT - T\Delta S < 0$

$99.8 \times 1000 - (2)T - T(1000) < 0$   
 $99800 < 1002T$

\* Calculation of  $\Delta G$  if Temp. & Pressure is not constant:

This calculation can be done only for a rev. process.

$G = H - TS$

$G = U + PV - TS$

$dG = dU + PdV + VdP - TdS - SdT$   
 $= dq + VdP - dq - SdT$

$dG = VdP - SdT$

$dq + w = dU$   
 $dq - PdV = dU$   
 $dq = dU + PdV$   
 $dS = \frac{dq}{T}$   
 $TdS = dq$



Pressure.

\* Only if ~~temp~~ is constant: (In Isobaric Process).

$$P = \text{constant}$$

$$dU = -SdT$$

$$\left(\frac{dU}{dT}\right)_P = -S$$

\* If constant pressure slope of  $U$  vs  $T$  curve will be equal to  $-S$

$$S_{\text{gas}} \gg S_{\text{liquid}} > S_{\text{solid}}$$

$$-S_{\text{gas}} \ll -S_{\text{liquid}} < -S_{\text{solid}}$$

2) Only if temperature is constant

(In Isothermal Process):

$$dU = vdp$$

$$\left(\frac{dU}{dP}\right)_T = v \quad \text{slope of}$$

$$V_{\text{gas}} \gg V_{\text{liquid}} > V_{\text{solid}}$$

Case: (1)  $\Delta U$  for solid & liquid in an isothermal process:

$$dU = v dP$$

$$\Delta U = \int_{P_1}^{P_2} v dP$$

$$\Delta U = V(P_2 - P_1) \quad P_1 = \boxed{\Delta U = V \Delta P}$$



Case 2:  $\Delta G$  for Ideal gas in an Isothermal Process!

$$\Delta G = \int_{P_1}^{P_2} v dP$$

$$\Delta G = \int_{P_1}^{P_2} \frac{nRT}{P} dP$$

$$\Delta G = nRT \ln(P_2/P_1)$$

$$\Delta G = -nRT \ln\left(\frac{P_1}{P_2}\right) = W_{\text{isothermal}}$$

Ques: Calculate sign of  $\Delta H$ ,  $\Delta U$ ,  $\Delta S$ ,  $\Delta G$ ,  $\Delta S_{\text{surr}}$ ,  $\Delta S_{\text{universe}}$  for given process.



$$\Delta H > 0$$

$$\Delta U > 0$$

$$\Delta S > 0$$

Physical state  
(g) > (l) > (s)

$$\Delta S_{\text{surr}} = -\frac{q_{\text{system}}}{T} \quad q > 0 \quad T > 0$$

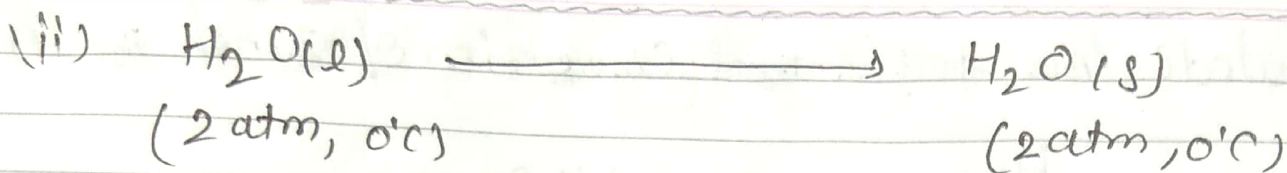
$$\Delta S_{\text{surr}} < 0$$

$\Rightarrow$  Process will be spontaneous

$$\Delta G < 0$$

$$\Delta S_{\text{universe}} > 0$$





$$\Delta H < 0$$

$$\Delta U < 0$$

$$\Delta S < 0$$

$$\Delta S_{\text{surr}} \geq 0$$

$$\Delta S_{\text{surr}} = -\frac{q_{\text{sys}}}{T} < 0$$

Non-spontaneous

\* Process will be non spontaneous

$$\Delta G > 0$$

$$\Delta S_{\text{universe}} < 0$$

Ques! Boiling at freezing point

$$\Delta H > 0$$

$$\Delta U > 0$$

$$\Delta S > 0$$

$$\Delta S_{\text{surr}} = -\frac{q_{\text{system}}}{T}$$

$$q > 0$$

$$\Delta S_{\text{surr}} < 0$$

\* process will be non-spontaneous.

$$\Delta G > 0$$

$$\Delta S_{\text{universe}} < 0$$

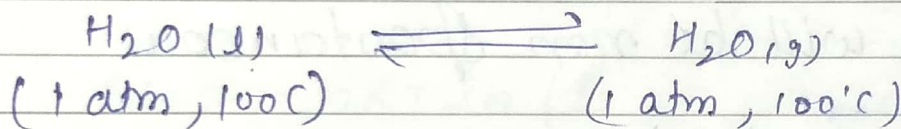
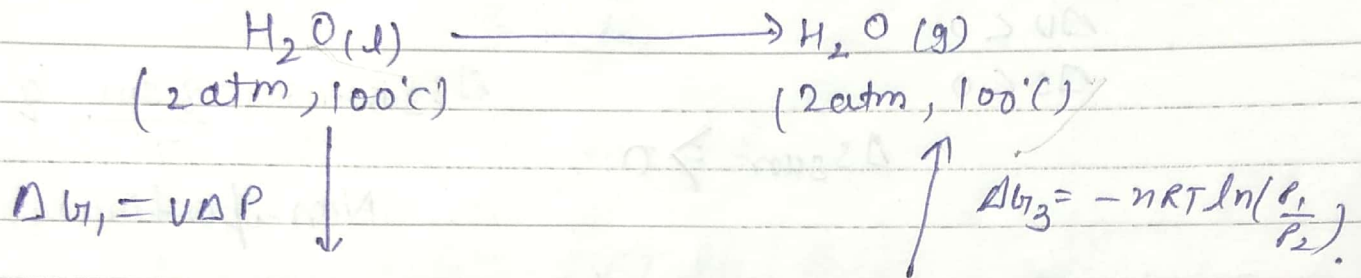
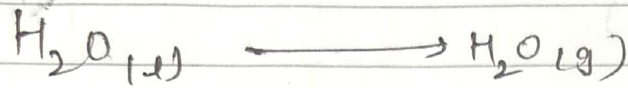
$$\Delta G = \Delta H - T\Delta S$$

Solid & liquid  $\Delta G = \Delta P \Rightarrow T \text{ constant.}$

gas  $= -nRT \left( \frac{P_1}{P_2} \right) = T = \text{const}$



\* Calculate  $\Delta G$  for ~~total~~ conversion of 1 mol  $H_2O(l)$



$$\Delta G_1 = V\Delta P = \frac{18}{1000} (1-2) \text{ atm.litre.}$$

$$\Delta G_3 = -1(R)(373) \ln\left(\frac{1}{2}\right)$$

$$\Delta G = \frac{-1.8}{1000} (101.3) - (8.3)(373) \ln\left(\frac{1}{2}\right)$$

\* Relation b/w  $\Delta G$ ,  $\Delta G^\circ$  and  $Q$ :

$$\text{J. Dupr} \left[ \Delta G = \Delta G^\circ + RT \ln Q \right]$$

$$Q = \frac{P}{P^\circ}$$

at eq<sup>b</sup>

$$\Delta G = 0$$

$$Q = K_{eq}$$

$K_p =$  gaseous equilibrium

$K_c =$  liquid eq<sup>b</sup>.

$$0 = \Delta G^\circ + RT \ln K_{eq}$$

$$\Delta G^\circ = -RT \ln K_{eq}$$



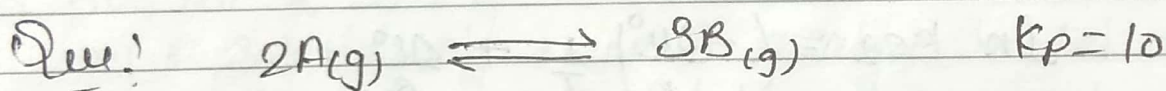
$$\Delta G = -RT \ln K_{eq} + RT \ln Q$$

$$\Delta G = RT \ln \left( \frac{Q}{K_{eq}} \right)$$

$\Delta G < 0$       Spontaneous  
 Rxn in forward  
 direction       $Q < K_{eq}$  [Forward]

$\Delta G = 0$       Equilibrium       $Q = K_{eq}$   
 (backward)

$\Delta G > 0$       Non-spontaneous  
 in forward dir<sup>n</sup>.       $Q > K_{eq}$   
 [backward]



In at any instant  $P_A = 0.01 \text{ kPa}$  &  $P_B = 1 \text{ kPa}$   
 then calculate value of  $\Delta G$  at  $27^\circ\text{C}$  and what  
 will be direction of rxn to achieve  
 equilibrium?

$$1 \text{ bar} = 10^5 \text{ Pa}$$

Ans!

$$Q = \frac{P_B^3}{P_A^2} = \frac{(1000 \times 10^{-5})^3}{(0.01 \times 1000 \times 10^{-5})^2}$$

$$\frac{10^3}{10^2} = 10$$

$$Q = 100$$

$$\Delta G = \Delta G^\circ + RT \ln Q$$



$$\Delta G = -RT \ln K_{eq} + RT \ln Q$$

$$\Delta G = RT \ln(Q/K_{eq})$$

~~$$\Delta G = -RT \ln 10 + RT \ln 100$$~~

$$\Delta G = RT \ln \frac{100}{10}$$

$$\Delta G = RT \ln 10$$

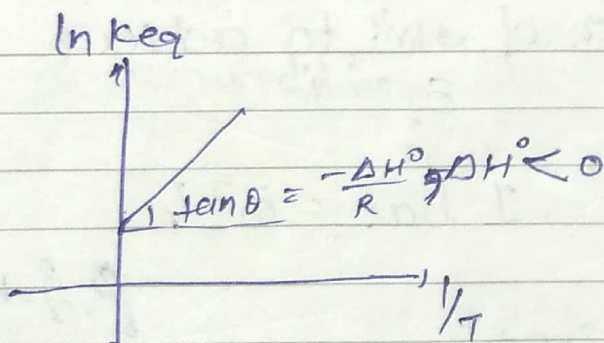
backward direction

\* Relation b/w  $\Delta H^\circ$ ,  $\Delta S^\circ$  &  $\ln K_{eq}$ !

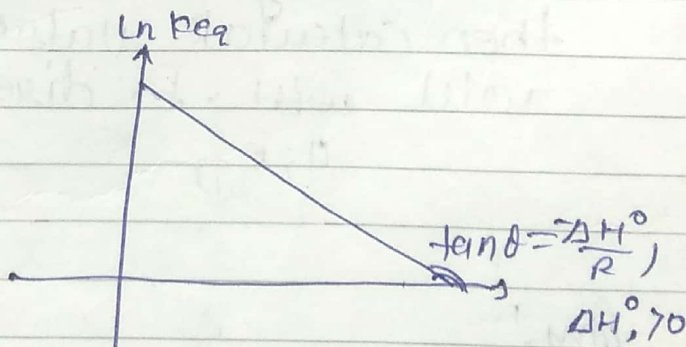
$$\begin{aligned} \Delta G^\circ &= \Delta H^\circ - T\Delta S^\circ \\ -RT \ln K_{eq} &= \Delta H^\circ - T\Delta S^\circ \end{aligned}$$

$$\ln K_{eq} = \left( \frac{-\Delta H^\circ}{R} \right) \frac{1}{T} + \frac{\Delta S^\circ}{R}$$

$$y = m \cdot x + c$$



Exothermic  $R_{xy}$



Endothermic  $R_{xy}$

\* Physical Significance of  $\Delta G$  :

At constant Pressure and Temp. in a Rev. Process  $\Delta G$  will be equal to non-PV work.



Q. useful work in the process  
useful work is also called available energy  
of system.

$$dq + w = du$$

$$dq + w_{pv} + w_{non-pv} = du$$

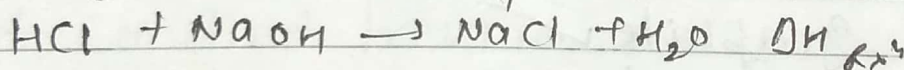
$$dq - PdV + w_{non-pv} = du$$

$$w_{non-pv} = \underline{du + PdV} - dq$$

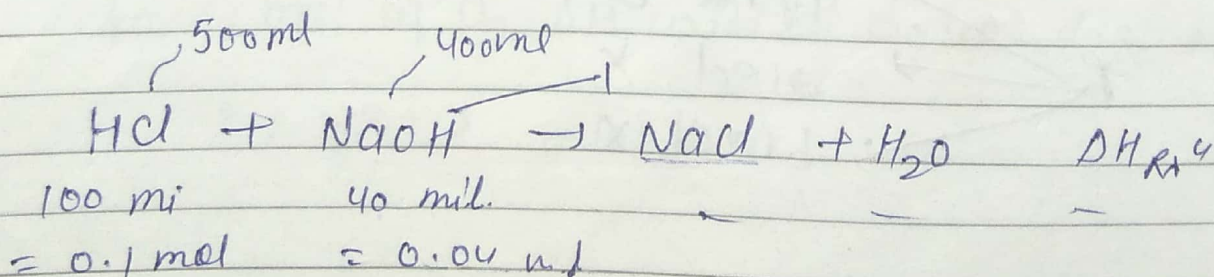
$$w_{non-pv} = dH - TdS$$

$$w_{non-pv} = dg$$

Q. 500 ml of 0.2 M HCl solution is mixed with 400 ml  
0.1 M solution of NaOH in a calorimeter due to  
the reaction temp. of solution increase by  $0.6^\circ\text{C}$ .  
then calculate  $\Delta H$  for given rxn.



Suppose density of resulting sol<sup>n</sup> is  $1\text{ g/ml}$  and  
specific heat capacity of sol<sup>n</sup> is  $1\text{ cal/g}^\circ\text{C}$   
and heat capacity of container is zero.



$$= \frac{\Delta H}{S.P} = \frac{\Delta H \times 0.04}{1} = -mC_s\Delta T$$

$$\Delta H_{\text{rxn}} \times 0.04 = -(400)(1)(0.6)$$

$$\Delta H_{\text{rxn}} = -13500\text{ cal.}$$



## \* Definition of different types of Enthalpies

### 1. Enthalpy of formation ( $\Delta H_f^\circ$ ) :

Define for formation of 1 mole substance from its elements and elements must be present in their standard state.

Most abundance of element in nature considered its standard state

